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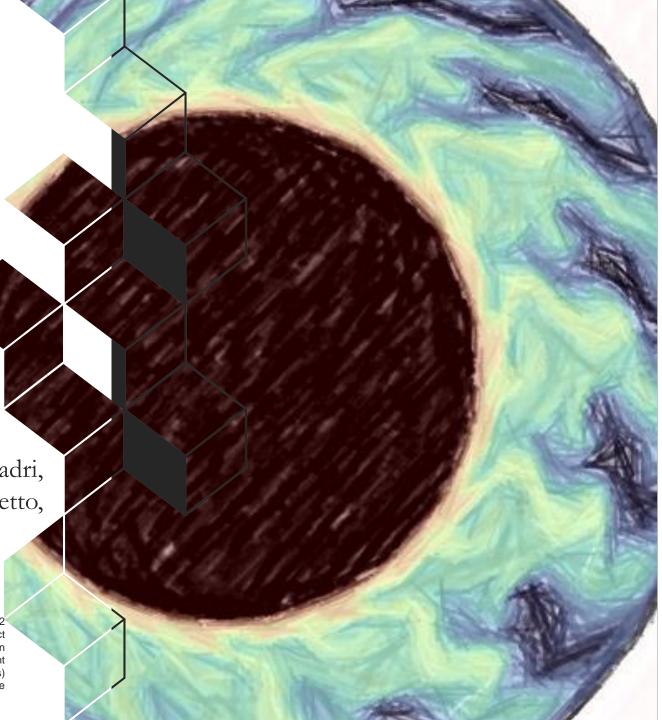
#### Introducing electromagnetic effects in Soledge3X

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#### **Outline**

- 1. Electrostatic versus Electromagnetic models
  - 2. A new vorticity system for Soledge3X
  - 3. Verification and validation of the model
- 4. First electromagnetic turbulent simulations
- 5. Conclusions and perspectives

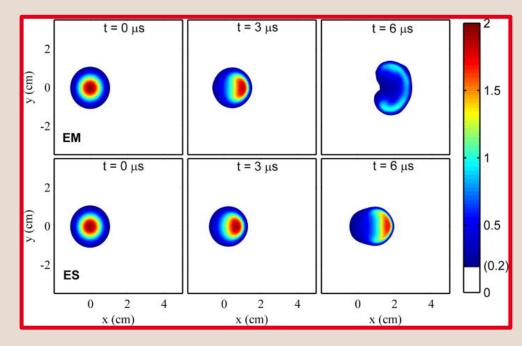


# Electrostatic versus electromagnetic models





- Non-negligeable effects on the plasma
  - Existence of drift Alfvén turbulence [Scott, PPCF 1997]
  - Impact on filament shape in turbulent blob propagation [Lee et al, JNM 2015]
  - Stronger effects for high- $\beta$  plasmas
- Electron inertia effects are also needed
  - Constrain the shear Alfvén wave speed to physical values [Dudson et al, PPCF 2021]
  - Improvement of the numerical stability [Stegmeir et al, PoP 2019]
- Turbulent simulations on large machines (e.g. ITER) require electromagnetic effects



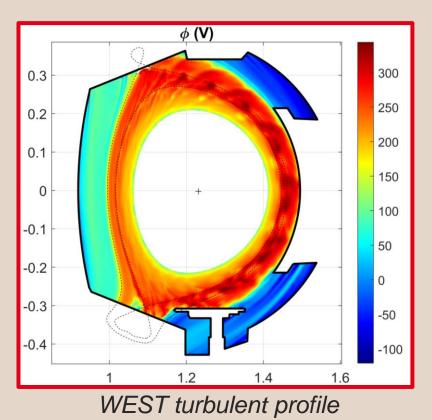
Propagation of a plasma blob from [Lee et al, JNM 2015]

top: electromagnetic, bottom: electrostatic

Key parameter: 
$$\beta = \frac{p}{p_{mag}} = \frac{enT}{B^2/2\mu_0}$$







The electric field for  $E \times B$  drifts is obtained from the potential:  $E_{\perp} = -\nabla_{\perp} \Phi$ 

- The potential appears in:
  - the vorticity  $\Omega = \nabla \cdot \left[ \frac{m_i n_i}{e Z_i B^2} \nabla_{\perp} \Phi + \frac{m_i}{e Z_i^2 B^2} \nabla_{\perp} p_i \right]$ for the polarization current  $\nabla \cdot j_{\parallel} \boldsymbol{b} = -\partial_t \Omega + \nabla \cdot \boldsymbol{j}_{\Omega}$
  - the parallel electric field  $E_{\parallel} \boldsymbol{b} = -\boldsymbol{\nabla}_{\parallel} \Phi$  for Ohm's law  $j_{\parallel} = \sigma_{\parallel} \left( E_{\parallel} + \frac{1}{en_e} (\mathbf{b} \cdot \boldsymbol{\nabla}_{\parallel} p_e + R_{e,\parallel}) \right)$
- The quasineutral assumption  $\nabla \cdot j^{tot} = 0$  leads to the "vorticity" equation on  $\Phi$ :

$$\nabla \frac{m_i n_i}{e Z_i B^2} \partial_t \nabla_{\perp} \Phi + \nabla \cdot (\sigma_{\parallel} \nabla_{\parallel} \Phi) \boldsymbol{b} = \nabla \cdot \left( \sigma_{\parallel} \frac{1}{e n_e} (\nabla_{\parallel} p_e + R_{e,\parallel}) \right) \boldsymbol{b} + \nabla \cdot (\boldsymbol{j}^* + \boldsymbol{j}_S + \boldsymbol{j}_{\Omega}) \boldsymbol{b}$$

Ratio between diffusion coefficients:  $> 10^6$ 

High anisotropy → poor numerical condition!

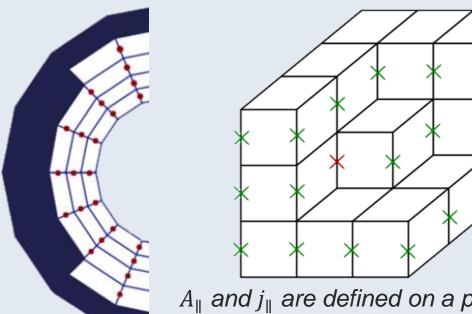
# A new vorticity system for Soledge3X





Implicit system on 3 fields: electric potential  $\Phi$ ; parallel magnetic vector potential  $A_{\parallel}$ ; parallel current density  $j_{\parallel}$ 

$$\nabla \cdot \left[ \frac{m_{\alpha} n_{\alpha}}{B^{2}} \partial_{t} \nabla_{\perp} \Phi \right] = \nabla \cdot (j_{\parallel} \vec{b}) - \partial_{t} \Omega_{\pi}$$
 (1) Vorticity equation 
$$j_{\parallel} + \frac{\sigma_{\parallel} m_{e}}{n_{e} e^{2}} \left( \frac{\partial j_{\parallel}}{\partial t} - \vec{\nabla} \cdot \left( v_{e} \vec{\nabla}_{\perp} j_{\parallel} \right) \right) = \sigma_{\parallel} \left( -\nabla_{\parallel} \Phi - \partial_{t} A_{\parallel} + \frac{T_{e}}{e} \nabla_{\parallel} \log(n_{e}) + \frac{1.71}{e} \nabla_{\parallel} T_{e} \right)$$
 (2) Ohm's law 
$$\Delta_{\perp} A_{\parallel} = -\mu_{0} j_{\parallel}$$
 (3) Ampère's law



 $A_{\parallel}$  and  $j_{\parallel}$  are defined on a poloidally and toroidally staggered grid

No points for  $A_{\parallel}$  and  $j_{\parallel}$  needed on the sheath:

- Dirichlet  $A_{\parallel}^{BC}$ =0 on the sheath and tangential wall BC
- The sheath current is directly enforced in the vorticity equation

$$\left(1 + \frac{\sigma_{\parallel} m_e}{n_e e^2} \partial_t\right) j_{\parallel}^{BC} = j_{sat} \left(1 - e^{\Lambda - \Phi/T_e}\right)$$

Neumann  $\nabla^{BC} j_{\parallel} = 0$  for the perpendicular diffusion operator on  $j_{\parallel}$ 

### Implementation details



A coupled implicit system is solved on the potentials  $\Phi$  and  $A_{\parallel}$ , the current  $j_{\parallel}$  is updated a posteriori

$$\begin{pmatrix} \hat{\partial}_{t} \hat{\nabla} \cdot \begin{bmatrix} \hat{D}_{\perp} \hat{\nabla}_{\perp} \circ \end{bmatrix} + \hat{\nabla} \cdot \begin{bmatrix} \hat{D}_{\parallel} \hat{\nabla}_{\parallel} \circ \vec{b} \end{bmatrix} & \beta_{0} \hat{\partial}_{t} \hat{\nabla} \cdot \begin{bmatrix} \hat{D}_{\parallel} \circ \vec{b} \end{bmatrix} \\ \hat{D}_{\parallel} \hat{\nabla}_{\parallel} \circ & \beta_{0} \hat{D}_{\parallel} \hat{\partial}_{t} \circ - \hat{\nabla} \cdot \begin{bmatrix} \hat{\nabla}_{\perp} \circ \end{bmatrix} \end{pmatrix} \begin{pmatrix} \hat{\Phi}^{n+1} \\ \hat{A}_{\parallel}^{n+1} \end{pmatrix} = \begin{pmatrix} \hat{\nabla} \cdot \begin{bmatrix} \hat{D}_{t} \hat{J}_{\parallel}^{n} \vec{b} \end{bmatrix} + RHS^{\Phi} \\ \hat{D}_{t} \hat{J}_{\parallel}^{n} + RHS^{A_{\parallel}} \end{pmatrix}$$

with the coefficients 
$$\widehat{D}_{\perp}=rac{\widehat{m}_i\,\widehat{n}_i}{\widehat{B}^2}$$
,  $\widehat{D}_{\parallel}=rac{\widehat{\sigma}_{\parallel}}{1+\widehat{\tau}/\mu}$  and  $\widehat{D}_t=rac{\mu}{1+\widehat{\tau}/\mu}$ 

and the plasma parameters  $\beta_0 = \frac{e n_0 T_0}{B^2/\mu_0}$  and  $\mu = \frac{\widehat{\sigma}_{\parallel} \widehat{m}_e}{\widehat{n}_e \widehat{m}_i}$  for a timestep size  $\widehat{\tau}$ .

	Ф	$\Phi - j_{\parallel}$	$\mathbf{\Phi} - \mathbf{A}_{\parallel}$	$\Phi - j_{\parallel} - A_{\parallel}$
Number of iterations	165	35	660	117
Solve time per iteration [s]	0.45	0.11	6.36	1.15
Total time [s]	2268	1599	14275	3841

Simulation results for different combinations of equations (1) – (3) on a 3D limiter case with ~500.000 cells PETSc: LGMRES scheme with GAMG preconditioner on 96 computing cores. No drifts

### **Electromagnetic flutter**

Definition of the electromagnetic potential:

$$\nabla \times A = B$$

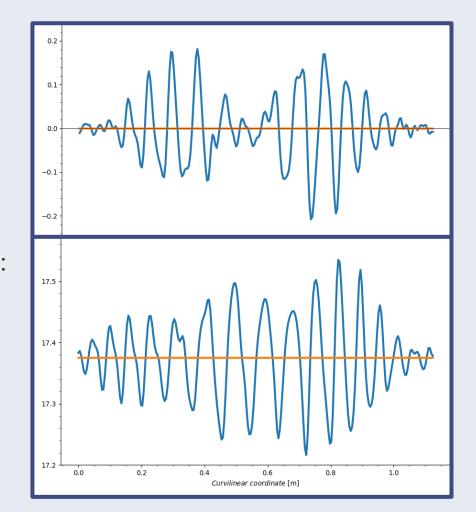
Assume small perturbations of the equilibrium magnetic field:

$$\boldsymbol{B} = \boldsymbol{B}_{eq} + \widetilde{\boldsymbol{B}}$$

From the value of the toroidal perturbation field  $ilde{A}_{\parallel}$  :

$$\widetilde{B} = (\nabla \times b_{eq})\widetilde{A}_{\parallel} - \mathbf{b}_{eq} \times \nabla \widetilde{A}_{\parallel}$$

- The perturbation field  $\widetilde{{\pmb b}}$  is calculated from  $\tilde{A}_{\parallel}$  at the previous timestep
- $\tilde{b}$  is considered for the advection and the parallel diffusion of the conserved fluid quantities:
  - ion density n<sub>i</sub>
  - ion momentum  $n_i v_i$
  - electron and ion temperature  $T_e$  and  $T_i$



 $b^{\psi}$  [ $m^{-1}$ ]

 $b^{\theta} [m^{-1}]$ 

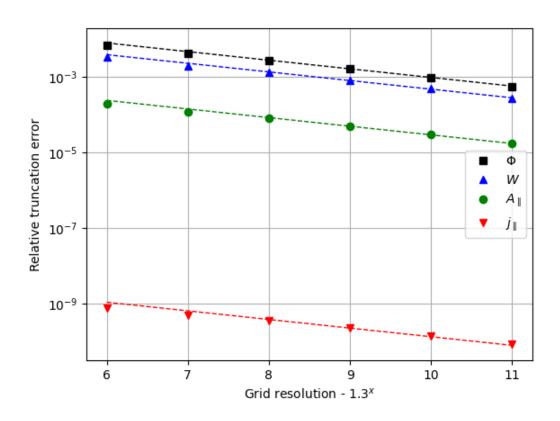
Fluctuations of the contravariant components of **b**Profile along the poloidal direction in the core

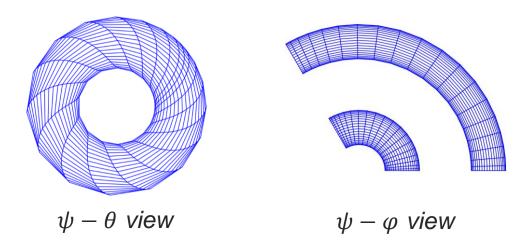
Limiter scenario with developed turbulence

## Model verification and validation

#### **MMS** verification

Use the method of manufactured solutions [Roache, SFMA 2019] to check the new system on  $\Phi$ ,  $A_{\parallel}$  and  $j_{\parallel}$  Define arbitrary initial profiles and apply analytic source terms to maintain a steady-state solution The change within one timestep estimates the numerical error





Estimated numerical errors for different 3D mesh resolutions.

The total number of points was increased by a factor ~2.2 between each run.

The dashed lines indicate the theoretical 2<sup>nd</sup> order convergence.

#### **Linear verification**

Consider the four-field model on a SLAB domain with uniform magnetic field. Only evolve  $n_e$ ,  $\Phi$ ,  $j_{\parallel}$  and  $A_{\parallel}$ 

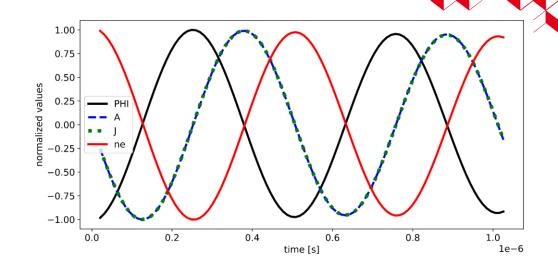
$$\begin{split} \partial_t n_e &= \frac{1}{e} \boldsymbol{\nabla} \cdot \boldsymbol{j}_{\parallel} \boldsymbol{b} \\ \boldsymbol{\nabla} \cdot \left[ \frac{m_i n_i}{B^2} \partial_t \boldsymbol{\nabla}_{\perp} \boldsymbol{\Phi} \right] &= \boldsymbol{\nabla} \cdot (\boldsymbol{j}_{\parallel} \boldsymbol{b}) \\ \frac{1}{\sigma_{\parallel}} \boldsymbol{j}_{\parallel} + \frac{m_e}{n_e e^2} \partial_t \boldsymbol{j}_{\parallel} &= \left( \frac{T_e}{e} \boldsymbol{\nabla}_{\parallel} \ln n_e - \boldsymbol{\nabla}_{\parallel} \boldsymbol{\Phi} \right) \cdot \boldsymbol{b} - \partial_t A_{\parallel} \\ \boldsymbol{\nabla} \cdot \boldsymbol{\nabla}_{\perp} A_{\parallel} &= -\mu_0 \boldsymbol{j}_{\parallel} \end{split}$$

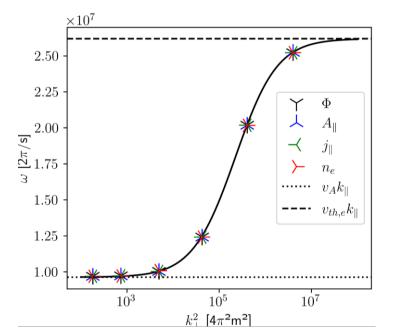
We expect a decaying standing wave with frequency:

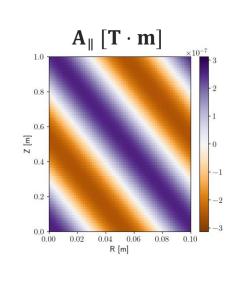
$$\omega_0^2 \approx \frac{v_A^2 + Kk_\perp^2}{1 + Ck_\perp^2} k_\parallel^2$$

The parallel wave speed is bound by:

- Alfvén wave group velocity  $v_A^2 = \frac{B^2}{m_i n_i \mu_0}$  for low  $k_\perp$
- Electron thermal speed  $v_{th,e}^2 = \frac{K}{C} = \frac{eT_e}{m_e}$  for high  $k_{\perp}$





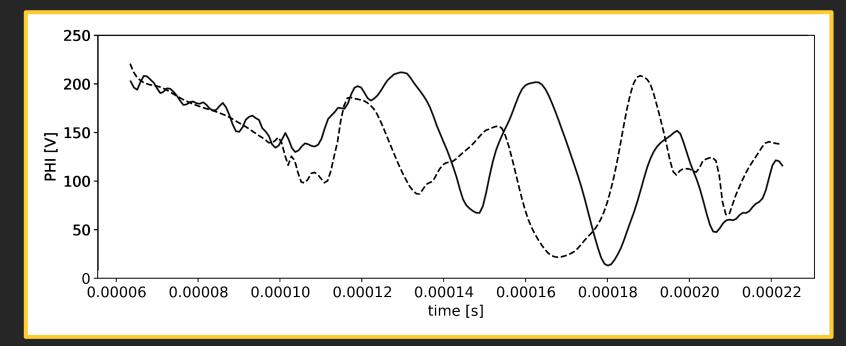


Simulation on a 3D SLAB with 63 points per dimension Good agreement with [Stegmeir et al, PP 2019]

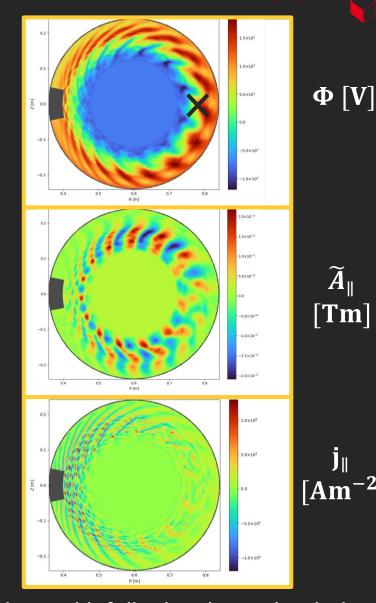


### Electromagnetic profiles

 Simulations on a limiter geometry with a constant density and energy source at the core



Time evolution of the electric potential at one point in the domain dashed line: electrostatic scenario full line: electromagnetic scenario



Snapshots at the first poloidal plane with fully developped turbulence

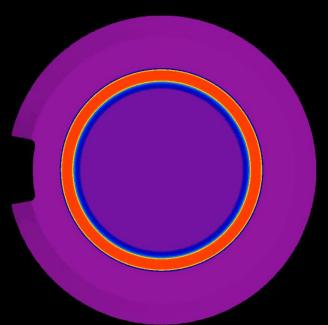
### Videos of a turbulent run

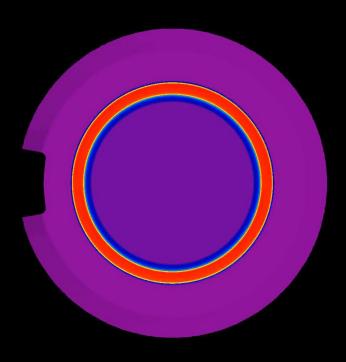


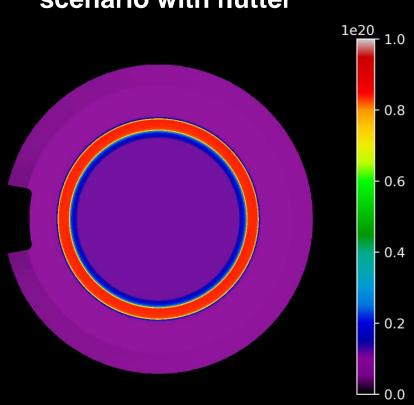


Electromagnetic scenario

Electromagnetic scenario with flutter







Evolution of the ion density  $n_i[m^{-3}]$ 

# Conclusions and perspectives

## **Conclusions and perspectives**

- Addition of two new fields to the Soledge3X model:
  - the parallel electromagnetic vector potential  $A_{\parallel}$
  - the parallel current density  $j_{\parallel}$  with finite electron mass
    - improves the numerical stability
    - constrains the Alfvén wave speed
- Validation of the new model
  - Verification via the Method of Manufactured Solutions
  - Dispersion relation verified by simulations
- Perspectives for future work
  - Extensive investigation of electromagnetic effects on the turbulent transport
  - **E** Evaluate the impact of  $\beta$  on the plasma
  - Extend to X-point geometry

