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► **To cite this version:**

Julien Jurczak, Benjamin Rapp, jean-marc bordy, Stéphanie Josset, Stephane Dufreneix. Defining field output factors in small fields based on dose area product measurements: a feasibility study. *Medical Physics*, 2024, 51, pp.3677-3686. 10.1002/mp.16950 . cea-04457936

**HAL Id: cea-04457936**

**<https://cea.hal.science/cea-04457936v1>**

Submitted on 14 Feb 2024

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# 1 Defining field output factors in small fields based on dose area 2 product measurements: a feasibility study

3 J. Jurczak<sup>1,2</sup>, B. Rapp<sup>1</sup>, J-M. Bordy<sup>1</sup>, S. Josset<sup>3</sup>, S. Dufreneix<sup>1,3,\*</sup>

4 <sup>1</sup>CEA, List, Laboratoire National Henri Becquerel (LNE-LNHB), Palaiseau, France

5 <sup>2</sup>Institut Curie, Medical Physics Department, F-75005, Paris

6 <sup>3</sup>Institut de Cancérologie de l'Ouest, Angers/Saint-Herblain, France

7 \*Corresponding author. E-mail: stephane.dufreneix@ico.unicancer.fr

8  
9 **Background:** Dose area product in water ( $DAP_w$ ) in small fields rely on the use of detectors  
10 with a sensitive area larger than the irradiation field. This quantity has recently been used  
11 to establish primary standards down to 5 mm field size with an uncertainty smaller than  
12 0.7%. It has the potential to decrease the uncertainty related to field output factors but it is  
13 not currently integrated into treatment planning systems.

14 **Purpose:** The aim of this study was to explore the feasibility of converting a  $DAP_w$  into a  
15 point dose in small fields through the determination of a volume averaging correction  
16 factor. By determining the field output factors, a comparison between the so-called “ $DAP_w$   
17 to point dose” approach and the IAEA TRS483 methodology was performed.

18 **Method:** Diodes, diamonds and a micro ionization chamber were used to measure field  
19 output factors following the IAEA TRS483 methodology on two similar linacs equipped  
20 with circular cones down to 6 mm diameter. For the “ $DAP_w$  to point dose” approach,  
21 measurements were performed with a dedicated and built-in-house 3 cm diameter plane-  
22 parallel ionization chamber calibrated in terms of  $DAP_w$  in the French Primary Dosimetry  
23 Standards Laboratory LNE-LNHB. Beam profile measurements were performed to  
24 generate volume averaging correction factors enabling the conversion of an integral  $DAP_w$   
25 measurement into a point dose and the determination of the field output factors. Both sets  
26 of field output factors were then compared.

27 **Results:** By following the IAEA TRS483 methodology, field output factors agreed within  
28  $\pm 3\%$  for all detectors on both linacs. Large variation were observed for the volume  
29 averaging correction factors with a maximum spread between the detectors of 26% for the  
30 smallest field size. Consequently, deviations up to 15% between the “IAEA TRS483” and  
31 the “ $DAP_w$  to point dose” methodologies were found for the field output factor of the  
32 smallest field size. It was attributed to the difficulty of accurately determine beam profiles  
33 in small fields.

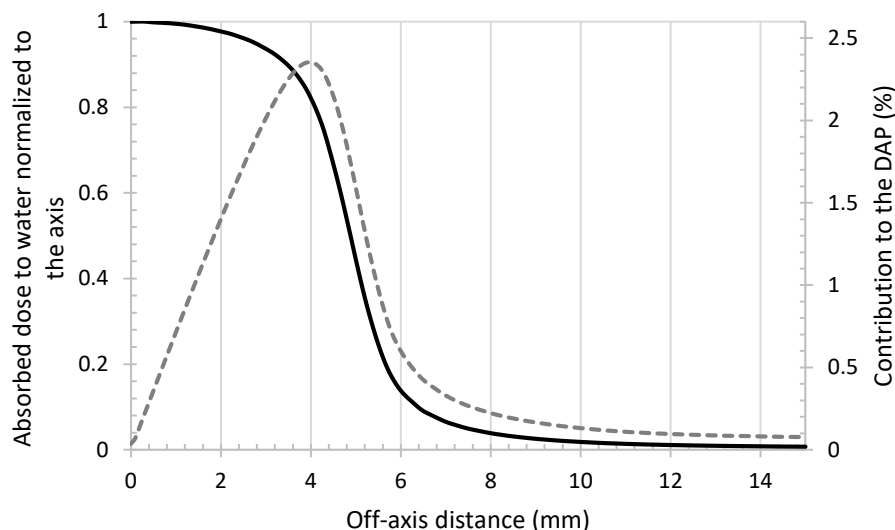
34 **Conclusion:** Although primary standards associated to small uncertainties can be  
35 established in terms of  $DAP_w$  in a primary laboratory, the “ $DAP_w$  to point dose”  
36 methodology requires a volume averaging correction to derive a field output factor from  
37  $DAP_w$  measurements. None of the point detector studied provided satisfactory results and  
38 additional work using other detectors such as film is still required to allow the transfer of a  
39  $DAP$  primary standard to users in terms of absorbed point dose.

40  
41 **Keywords:** *small field, output factor, dose area product*

## 42 43 44 **1. Introduction**

45 Small field measurements remain challenging due to the loss of lateral charged particle equilibrium,  
46 the occlusion of the primary photon source and the size of the detector relative to the size of the radiation  
47 field which generates volume averaging over the detector sensitive area and perturbation of the particle  
48 fluences<sup>1,2</sup>. In a primary dosimetry standards laboratory, calorimetric measurements could be performed  
49 in terms of absorbed dose at a point in water for field sizes down to 2 cm x 2 cm<sup>3,4</sup>. In radiation oncology  
50 departments, small field output factors are measured with dedicated detectors following the IAEA  
51 TRS483 code of practice<sup>1</sup>.

52 An alternative approach to point dose measurements in small fields was proposed by performing  
53 integral measurements with detectors larger than the irradiation field<sup>5-7</sup>. A new metric, the dose area  
54 product in water ( $DAP_w$ ) was introduced. It represents the energy per mass deposited by the beam over  
55 the sensitive area of the detector and is expressed in Gy.cm<sup>2</sup>. It can be interpreted as the integral of the  
56 absorbed dose distribution over the sensitive area of the detector. As a consequence, the absorbed dose  
57  $D_{abs}$  at a point located at (x,y) distance from the axis has a contribution to the dose integral depending  
58 on (x,y) distances. An example in a circular field and assuming a cylindrical geometry is given in Figure  
59 1: the most important contribution to the DAP comes from the penumbra region of the beam profile and  
60 profile tails have a contribution that cannot be neglected.  $DAP_w$  properties were investigated<sup>8-10</sup> and  
61 primary standards were established in terms of  $DAP_w$  for field sizes ranging from 5 mm to 15 mm<sup>11,12</sup>  
62 using a new designed large section graphite calorimeter. Dedicated and built-in-house large section  
63 plane-parallel ionization chambers were then calibrated, with a relative standard uncertainty smaller  
64 than 0.7 % for all calibration coefficients in small fields<sup>12</sup>.



65

66

67

Figure 1 : Example of the variation of absorbed dose to water with off-axis distance (solid line, left axis) and its corresponding contribution to the dose integral (dotted line, right axis) in a 10 mm diameter field.

68 The clinical implementation of the  $DAP_w$  based on measurements with a large section plane-parallel  
 69 ionization chamber has however not yet been investigated. The most direct option to exploit DAP  
 70 primary standards would be to introduce  $DAP_w$  in treatment planning systems (TPS). This would require  
 71 a formalism modification in TPS at least the for output factor input data, considering an integrated  
 72 measurement instead of a point dose. Another and easier solution would be to convert  $DAP_w$   
 73 measurements into point dose thanks to a volume averaging correction factor ideally generated from a  
 74 2D dose mapping of the beam. A 1.2% difference was previously observed between a calibration  
 75 coefficient derived from  $DAP_w$  measurements and one directly established in terms of absorbed dose to  
 76 water at a point in a square 2 cm field<sup>13</sup>. However, no other studies investigated the link between  $DAP_w$   
 77 and point dose for smaller field sizes and the transfer of primary standards measurements to radiation  
 78 oncology departments is still to be formalized.

79 The aim of this study was to explore the feasibility of using the  $DAP_w$  quantity in a radiation  
 80 oncology department for small fields through a conversion into point dose. Measurements were  
 81 performed in circular field sizes down to 6 mm diameter using a large section plane-parallel ionization  
 82 chamber calibrated in terms of  $DAP_w$  at the French Primary Dosimetry Standards Laboratory LNE-  
 83 LNHB. Several solid point detectors were used to define the field output factors following the IAEA  
 84 TRS483 methodology<sup>1</sup>. Assuming an axial symmetry, the volume averaging factors were determined  
 85 based on profile measurements with the different point detectors. Field output factors derived from the  
 86 large section plane-parallel ionization chamber measurements and combined with the volume averaging  
 87 correction factors were compared to field output factors derived from the IAEA TRS483 methodology<sup>1</sup>.

88

## 89 2. Materials and methods

### 90 2.1. Plane-parallel ionization chamber and formalism

91 The large section plane-parallel ionization chamber, denoted reference chamber afterwards was  
 92 designed and built in-house at the French primary dosimetry standards laboratory LNE-LNHB <sup>12</sup>.  
 93 Developed for measurements in small fields up to 15 mm, its collection area has a diameter of 30 mm  
 94 enabling the integration of the energy deposited by the beam over its sensitive area.

95 For the purpose of this study, the reference ionization chamber was calibrated in terms of absorbed  
 96 dose to water  $D_w$  (Gy.C<sup>-1</sup>) in a 10 cm x 10 cm field in a 6 MV FFF beam at the laboratory, using water  
 97 calorimetry as a primary standard, according to the expression:

$$98 \quad N_{D,w,fref} = \left[ \frac{D_w}{Q_w^*} \right]_{fref} \quad (1)$$

99 Where:

- 100 -  $N_{D,w,fref}$  (in Gy.C<sup>-1</sup>) is the calibration coefficient in terms of absorbed dose to water at a point
- 101 -  $D_w$  is the absorbed dose to water at a point measured by water calorimetry
- 102 -  $Q_w^*$  is the collected charge measured by the reference ionization chamber and corrected from
- 103 the influence quantities (temperature, pressure, polarity, recombination and volume averaging
- 104 over its collection area)

105 This reference chamber was also calibrated in terms of dose area product in water DAP<sub>w</sub>  
 106 (Gy.cm<sup>2</sup>.C<sup>-1</sup>) in a 6 MV FFF beam for various circular field sizes (denoted  $f_{clin}$ ) ranging from 5 to 15  
 107 mm diameter, using graphite calorimetry as a primary standard, according to the expression:

$$108 \quad N_{DAP,w,fclin} = \left[ \frac{DAP_w}{Q_w^*} \right]_{fclin} = \left[ \frac{D_{core}}{Q_w^*} \right]_{fclin} \left[ \frac{D_w}{D_{core}} \right]_{MC,fclin} S_{core} k_i \quad (2)$$

109 Where:

- 110 -  $N_{DAP,w}$  (in Gy.cm<sup>2</sup>.C<sup>-1</sup>) is the calibration coefficient in terms of DAP<sub>w</sub>
- 111 - DAP<sub>w</sub> is the dose-area product in water
- 112 -  $D_{core}$  is the average absorbed dose in the core (sensitive part) of the calorimeter
- 113 -  $\left[ \frac{D_w}{D_{core}} \right]_{MC}$  is the graphite to water dose conversion factor calculated by Monte Carlo
- 114 -  $S_{core}$  is the core area
- 115 -  $k_i$  an impurity correction factor taking into account the effects on the absorbed dose of all the
- 116 impurities within the core that are different from graphite (mainly thermistors for temperature
- 117 measurement). This correction was considered here dosimetrically negligible because
- 118 thermistors are located at the periphery of the core and are not in the direct beam.

119 Details on the reference chamber and its calibration coefficients can be found in <sup>12</sup>. Since  
 120  $N_{DAP,w,fclin}$  was found slightly dependent on field size, calibration coefficients in terms of DAP<sub>w</sub> were  
 121 defined for each field size studied by linearly interpolating to the corresponding measured FWHM.

122 Derived from equation (2), the absorbed dose to water at a point located on the beam axis, in a  
 123 clinical field, can be expressed as:

$$124 \quad D_{w,fclin} = \frac{N_{DAP,w,fclin} Q_w^*}{S_{core} k_i} \quad (3)$$

125 A field output factor  $\Omega_{Q_{clin}, Q_{ref}}^{f_{clin}, f_{ref}}$  measured by the reference chamber can then be defined as:

$$126 \quad \Omega_{Q_{clin}, Q_{ref}}^{f_{clin}, f_{ref}} = \frac{D_{w, f_{clin}}}{D_{w, f_{ref}}} = \frac{1}{S_{core} k_i} \frac{N_{DAP, w, f_{clin}} Q_{w, f_{clin}}^*}{N_{D, w, f_{ref}} Q_{w, f_{ref}}^*} \quad (4)$$

127 The numerator of the formula for  $f_{clin}$  is based on the  $DAP_w$  formalism whereas the denominator of  
 128 the formula for  $f_{ref}$  is based on the usual point dose formalism.  $N_{DAP, w, f_{clin}}$ ,  $N_{D, w, f_{ref}}$ ,  $S_{core}$  and  $k_i$  were  
 129 provided by the primary standards laboratory.  $Q_{w, f_{clin}}^*$  and  $Q_{w, f_{ref}}^*$  were measured with the reference  
 130 chamber in two radiation oncology departments. Those last quantities are the collected charge corrected  
 131 from influence quantities: temperature, pressure, polarity, recombination and volume averaging over its  
 132 collection area. Details and formulas for the correction factors for the influence quantities can be found  
 133 in the IAEA TRS398<sup>14</sup> and IAEA TRS483<sup>1</sup>. Of specific interest for this study is the volume averaging  
 134 correction factor. It can be expressed as<sup>1,15</sup>:

$$135 \quad k_{vol} = \frac{\iint_A dx dy}{\iint_A OAR(x, y) dx dy} \quad (5)$$

136 Where:

- 137 -  $x$  and  $y$  are the coordinates on the axes orthogonal to the beam central axis
- 138 -  $A$  is the area of the projection of the sensitive volume of the reference chamber on a plane  
 139 orthogonal to the beam axis
- 140 -  $OAR(x, y)$  is the off-axis ratio, which is the 2-D lateral beam profile at the measurement depth  
 141 normalized to unity on the central axis

142 In a 10 cm x 10 cm reference field, the volume averaging correction factor is close to unity, even  
 143 for a large sensitive area in a FFF beam: for example,  $k_{vol, f_{ref}} = 1.0067$  for the 30 mm diameter sensitive  
 144 area of the reference chamber in a 6 FFF beam. However, for fields  $f_{clin}$  smaller than the sensitive area  
 145 of the reference chamber, it strongly increases with decreasing field size since the sensitive area is no  
 146 longer homogeneously irradiated. Measurement of the off-axis ratio  $OAR(x, y)$  in the radiotherapy  
 147 departments for the small fields studied is then needed. Ideally, the determination of  $k_{vol, f_{clin}}$  requires  
 148 a complete 2D mapping of the beam over the sensitive area and radiochromic films seem to be good  
 149 candidates considering their water equivalency and high spatial resolution. However, they are associated  
 150 to a potential penumbra blurring that need to be taken into account<sup>2</sup>. Their use also remain challenging  
 151 to perform accurate dose measurements<sup>16</sup>. Point detectors can also be used by assuming the axial  
 152 symmetry of the circular cones. Only a hemi-profile could be used to determine  $k_{vol, f_{clin}}$  following the  
 153 equation:

$$154 \quad k_{vol} \approx \frac{\int_0^{R_A} r dr}{\int_0^{R_A} OAR(r) dr} \quad (6)$$

155 Where  $R_A$  is the radius of the sensitive area of the reference chamber.

156

157 *2.2. Detectors and setup*

158 Measurements were performed on two Varian TrueBeam STx (Varian Medical Systems, Palo Alto,  
 159 CA, USA) named Linac1 and Linac2 in a 6 MV FFF beam (1400 MU/min), at 10 cm depth in water and  
 160 90 cm SSD. Field sizes were defined by circular cones of 15, 12.5, 10, 7.5 and 6 mm nominal diameter  
 161 manufactured by Brainlab (Brainlab AG, Munich, Germany) while the jaws were set to a 20 mm x  
 162 20 mm square field. Each Linac had its own set of cones.

163 Five consecutive charge measurements, each over 20 s, were performed with the reference chamber  
 164 for each circular cone, in a single measurement session. A 10 cm x 10 cm reference field was measured  
 165 before and after each cone measurement to correct from a potential drift of the accelerator.

166 Detectors used in this study for field output factor and  $k_{vol,f_{clin}}$  determination are summarized in  
 167 Table 1. All solid dosimeters were positioned with their axis parallel to the beam axis. Reference  
 168 chamber measurements were performed perpendicular to the beam. The IBA\_Razor\_Nano chamber axis  
 169 was positioned parallel to the beam for the profile measurement to avoid any stem effect while it was  
 170 positioned perpendicular to the beam for the field output factor determination to minimize the  $k_{pol}$  and  
 171  $k_{rec}$  corrections<sup>17</sup>. Some models (PTW\_60018 and PTW\_60019) were doubled to evaluate the intra-  
 172 model reproducibility.

173

Table 1 : Detectors used in this study

| Name                       | Linac1 | Linac2 | Type                        | Active material /<br>additional<br>components                                  | Diameter of<br>the sensitive<br>area (mm) | Typical<br>sensitivity<br>(nC/Gy)     |
|----------------------------|--------|--------|-----------------------------|--|---|---------------------------------------|
| Reference chamber          | x      | x      | Ionization<br>chamber       | Air cavity<br>Electrodes:<br>graphite<br>Wall: cross-<br>linked<br>polystyrene | 30  | NA<br>(depending<br>on field<br>size) |
| IBA_Razor<br>Nano chamber  | x      |        | Ionization<br>chamber       | Air cavity<br>Central<br>electrode:<br>Graphite<br>Wall: Shonka<br>(C-552)     | 2   | 0.11                                  |
| IBA_SFD                    | x      | x      | Stereotactic<br>field diode | Silicon<br>Wall: ABS +<br>Epoxy resin  | 0.6                                       | 6                                     |
| PTW_60017                  | x      | x      | Diode E                     | Silicon<br>Wall: RW3 +<br>Epoxy resin  | 0.6                                       | 9                                     |
| PTW_60018_1<br>(SN 000186) | x      | x      | Diode SRS                   | Silicon<br>Wall: RW3 +<br>Epoxy resin  | 0.6                                       | 175                                   |
| PTW_60018_2<br>(SN 000434) | x      |        |                             |  |   |                                       |

|                            |   |   |         |                            |     |   |
|----------------------------|---|---|---------|----------------------------|-----|---|
| PTW_60019_1<br>(SN 122271) | x | x |         | Carbon                     |     |   |
| PTW_60019_2<br>(SN 123788) | x |   | Diamond | Wall: RW3 +<br>Epoxy resin | 2.2 | 1 |

174

175 *2.3. Field output factors*

176 Field output factors were determined for point detectors listed in Table 1. For each detector, a pre-  
 177 irradiation of at least 1000 MU was performed before acquiring two profiles in the crossline and inline  
 178 directions for centering with the smallest 6 mm diameter cone. A 10 cm x 10 cm reference field was  
 179 measured before and after each cone measurement. Each time a cone was set up, two profiles were  
 180 performed to verify (and correct if necessary) the alignment of the detector on central axis before  
 181 performing the point dose measurement. On the beam axis, an average over 3 charge readings was  
 182 considered.

183 The  $k_{Q_{clin}, Q_{msr}}^{f_{clin}, f_{msr}}$  correction factors defined in the IAEA TRS-483 <sup>1</sup> were applied for the diodes and  
 184 diamond detectors. Since the IBA Razor Nanochamber was not listed in the IAEA TRS-483, no  
 185 correction factor was applied. For this detector, Partanen *et al.* reported a 1.034 correction factor in a  
 186 5 mm field at 6 MV FFF <sup>18</sup> but Lopez-Sanchez *et al.* reported a 1.005 correction factor for similar  
 187 conditions <sup>19</sup>.

188 The field output factor derived from the reference chamber measurements was compared to the  
 189 average field output factor over all point detectors. Data were reported respective to the equivalent  
 190 square field size defined as:

$$191 \quad S_{clin} = r\sqrt{\pi}$$

192 Where r is the circular field radius defined by the points where, on average, the dose level amounts to  
 193 50% of the maximum dose at the measurement depth <sup>1</sup>. Profiles measured with the PTW\_60018\_1  
 194 detector were arbitrarily taken for the determination of r but all detectors gave r values within 0.1 mm.

195

196 *2.4. Determination of  $k_{vol, f_{clin}}$* 

197 Profiles measured by point detectors listed in Table 1 were used, with a 0.1 mm resolution between  
 198 -15mm and +15mm in the crossline and inline directions. Minimum acquisition time was 1s per step  
 199 and beam profiles were normalized on the axis. For each cone, the mean  $k_{vol, f_{clin}}$  over the 4 hemi-  
 200 profiles was considered and the standard deviation was reported.

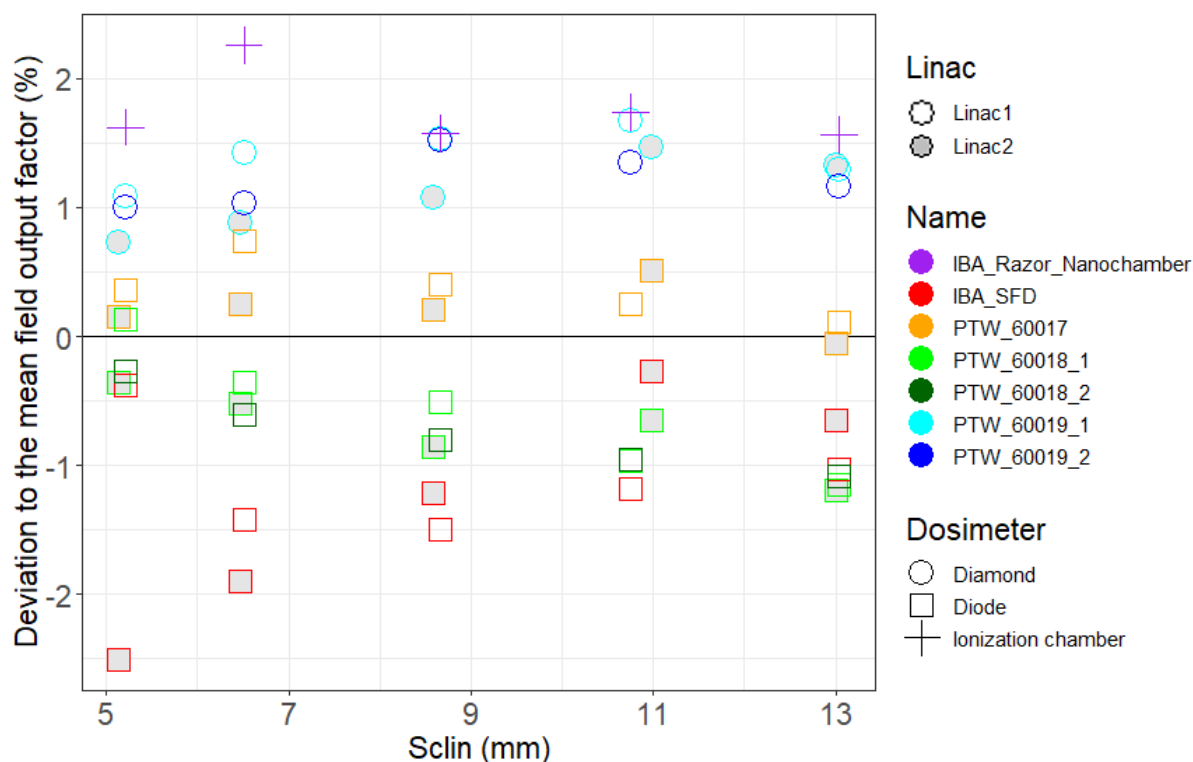
201 A  $k_{vol, f_{clin}}$  value was thus determined for each cone and each detector (i.e. 40  $k_{prof}$  values).  
 202 Following equation (4), a field output factor was derived and compared to the average field output factor  
 203 over all point detectors defined in section 2.3.

204

205 **3. Results**206 *3.1. Field output factors*



207 Deviation of individual field output factors per detector compared to the mean value over all  
 208 detectors is visible in Figure 2 for the different  $S_{clin}$  studied. The correspondence between field size and  
 209  $S_{clin}$  is provided in Table 2. All measurements agree with  $\pm 3\%$ , even for the uncorrected values of the  
 210 IBA Razor Nanochamber. A good reproducibility is observed between two detectors of the same type  
 211 (PTW 60018 and PTW 60019) with a maximum deviation of 0.4%. A good reproducibility is also  
 212 observed between the two linacs: except for the measurement with the IBA SFD in the smallest circular  
 213 field (2.2%), the maximum deviation is 0.5%.



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Figure 2 : deviation of field output factors compared to the mean value over all detectors.

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The average field output factors taken as a reference for the comparison of the  $DAP_w$  and point dose approaches are given in Table 2. The mean relative standard deviation associated is 1.2%. A comparison with Monte Carlo field output factors calculated by Hermida-Lopez *et al.*<sup>20</sup> shows a maximum deviation of 3.2% which is similar to the deviations observed by these authors in their literature review. These authors also provided an experimental field output factor for a 7.5 mm diameter cone based on measurements with PTW\_60019 SFD and EBT3 films. They found a value of 0.65 in agreement with our study (0.4% deviation).

Table 2 : mean field output factor and their associated standard deviation.

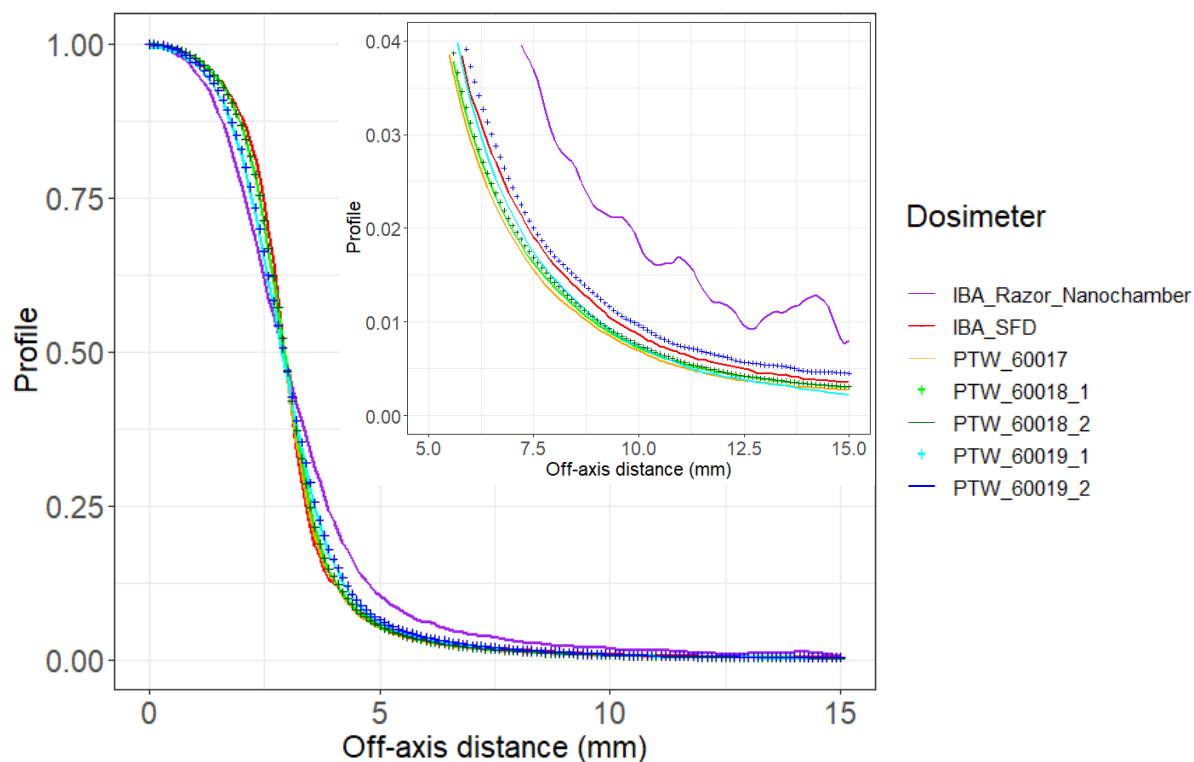
| Field size (mm) | $S_{clin}$ (mm) | Mean $\Omega_{Q_{clin}, Q_{ref}}^{f_{clin}, f_{ref}}$ (1 SD) | Hermida-Lopez <i>et al.</i> <sup>20</sup> MC value | Deviation (ref: <sup>20</sup> ) |
|-----------------|-----------------|--|--|---------------------------------|
| 15              | 13.0            | 0.760 (0.009)  | 0.78   | -2.6%                           |
| 12.5            | 10.9            | 0.736 (0.008)  | 0.76   | -3.1%                           |
| 10              | 8.6             | 0.701 (0.008)  | 0.72   | -2.6%                           |

|     |     |               |      |       |
|-----|-----|---------------|------|-------|
| 7.5 | 6.5 | 0.653 (0.008) | 0.67 | -2.6% |
| 6   | 5.2 | 0.608 (0.007) | 0.62 | -1.9% |

224

225 3.2.  $k_{vol,f_{clin}}$  values

226 An example of measured relative profile in the 6 mm circular cone is shown in Figure 3. As expected,  
 227 differences are observed in the penumbra region: the IBA\_Razor\_Nanochamber gives the smoothest  
 228 penumbra whereas the IBA\_SFD gives the sharpest. An overall good reproducibility between the 2  
 229 PTW\_60018 is observed. The 2 PTW\_60019 detectors are in agreement in the penumbra region but  
 230 slightly differ in the profile tails: at 15 mm from the axis, the dose measured by the PTW\_60019\_2  
 231 (0.5%) is approximatively twice the one measured by the PTW\_60019\_1 (0.2%). Fluctuations of 0.05%  
 232 are observed for the IBA\_Razor\_Nanochamber in the profile tails probably linked to the small sensitive  
 233 volume of the ionization chamber and its associated poor sensitivity (Table 1). The integration time was  
 234 not increased to reduce the noise for this detector in order to keep the overall measurement session  
 235 duration reasonable (approximately 2 hours for the 5 small profiles, without considering the output  
 236 factor measurements).



237

238 Figure 3 : Hemi beam profiles normalized on the axis measured with various point detectors in the 6 mm circular cone on  
 239 Linac1.

240 For each detector and field size, the mean  $k_{vol,f_{clin}}$  values calculated from the relative profiles are  
 241 reported in Table 3 with their associated standard deviations  $k_{vol,f_{clin}}$  values increases when the field  
 242 size decreases enlightening the importance of the contribution of profile penumbra and tail to the dose

243 integral. Standard deviations range between 0.1% and 2.7% and generally increase when the field size  
244 decreases. These values confirmed the hypothesis that an axial geometry can be assumed.

245 A large variability of the  $k_{vol,f_{clin}}$  is observed depending on the detector considered: for a specific  
246 linac and field size, the spread of  $k_{vol,f_{clin}}$  values increases from 4.4% for the 15 mm circular cone to  
247 25.8% for the 6 mm circular cone.  $k_{vol,f_{clin}}$  values for the IBA\_Razor\_Nanochamber are noticeably  
248 smaller than the values derived from solid detectors. Some profiles measured with the same detector on  
249 both linacs either give relatively close  $k_{vol,f_{clin}}$  values (PTW\_60017 and PTW\_60018\_1), or give  
250 differences up to 17% (IBA\_SFD and PTW\_60019\_1). Profile measurements on Linac1 with the  
251 PTW\_60018\_1 and PTW\_60018\_2 give  $k_{vol,f_{clin}}$  values in agreement within 1% whereas differences up  
252 to 13% are observed between PTW\_60019\_1 and PTW\_60019\_2.

253 *Table 3 :  $k_{vol,f_{clin}}$  values derived from profiles or 2D dose map measurements for several detectors. Standard deviations are*  
254 *given in parenthesis.*

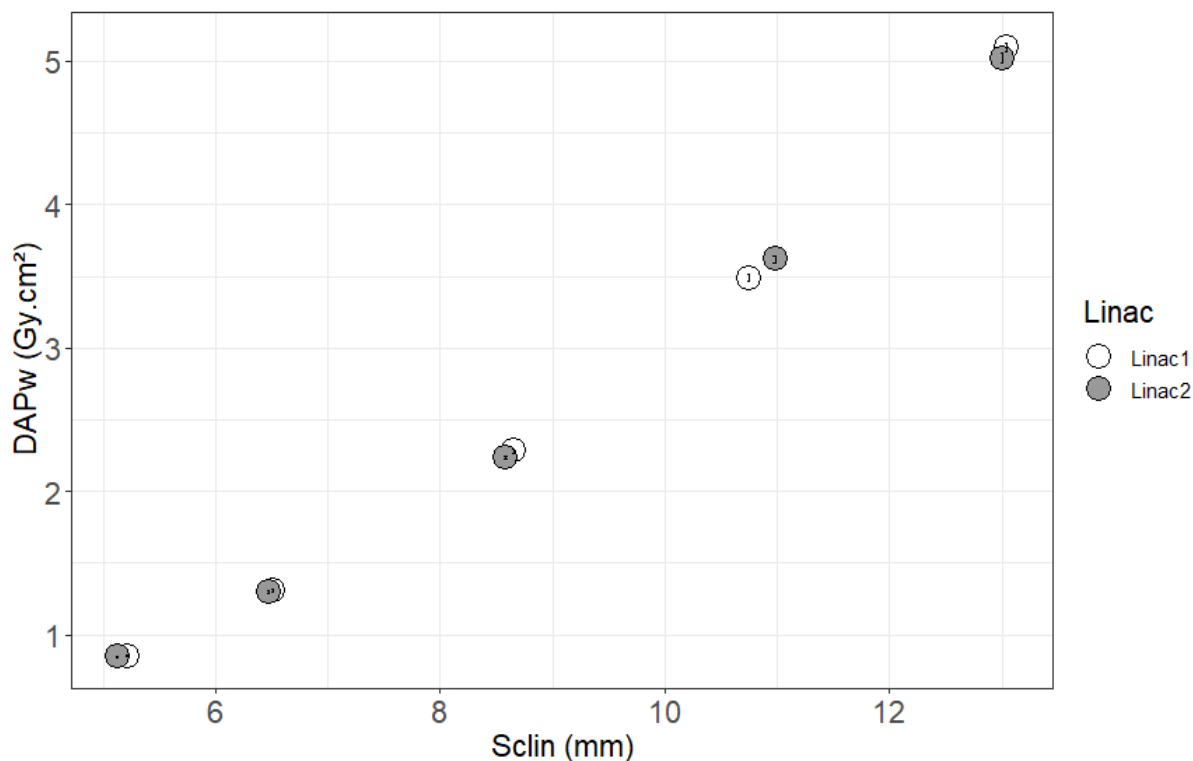
| Detector                                  | Linac                              | Cone diameter / $S_{clin}$ (mm) |             |             |            |            |
|---|------------------------------------|---------------------------------|-------------|-------------|------------|------------|
|   |                                    | 15 / 13.0                       | 12.5 / 10.9 | 10 / 8.6    | 7.5 / 6.5  | 6 / 5.2    |
| IBA_SFD                                   | Linac1                             | 3.84 (0.05)                     | 5.43 (0.04) | 8.02 (0.08) | 13.1 (0.1) | 18.9 (0.2) |
|   | Linac2                             | 3.85 (0.01)                     | 5.20 (0.01) | 8.08 (0.08) | 13.1 (0.2) | 18.9 (0.2) |
|   | <i>Deviation<br/>Linac2/Linac1</i> | 0.3%                            | -4.2%       | -0.8%       | -0.3%      | -0.1%      |
| PTW_60017                                 | Linac1                             | 3.87 (0.01)                     | 5.48 (0.04) | 8.17 (0.04) | 13.4 (0.2) | 19.8 (0.4) |
|   | Linac2                             | 3.91 (0.01)                     | 5.33 (0.02) | 8.33 (0.03) | 13.6 (0.2) | 20.0 (0.2) |
|   | <i>Deviation<br/>Linac2/Linac1</i> | 1.2%                            | -2.8%       | 2.0%        | 2.2%       | 1.4%       |
| PTW_60018_1                               | Linac1                             | 3.85 (0.01)                     | 5.46 (0.02) | 8.07 (0.04) | 13.3 (0.1) | 19.3 (0.2) |
|   | Linac2                             | 3.85 (0.01)                     | 5.23 (0.04) | 8.16 (0.04) | 13.3 (0.2) | 19.6 (0.2) |
|   | <i>Deviation<br/>Linac2/Linac1</i> | 0.0%                            | -4.2%       | 1.2%        | 0.2%       | 1.3%       |
| PTW_60018_2                               | Linac1                             | 3.83 (0.02)                     | 5.46 (0.04) | 8.07 (0.05) | 13.2 (0.1) | 19.2 (0.0) |
| <i>Deviation PTW_60018_1/ PTW_60018_2</i> |                                    | 0.7%                            | 0.1%        | -0.1%       | 0.4%       | 0.8%       |
| PTW_60019_1                               | Linac1                             | 3.90 (0.06)                     | 5.53 (0.04) | 8.17 (0.10) | 13.4 (0.1) | 19.3 (0.1) |
|   | Linac2                             | 3.78 (0.02)                     | 5.08 (0.02) | 7.83 (0.06) | 12.3 (0.2) | 17.2 (0.3) |
|   | <i>Deviation<br/>Linac2/Linac1</i> | -3.1%                           | -8.1%       | -4.1%       | -8.6%      | -10.7%     |
| PTW_60019_2                               | Linac1                             | 3.83 (0.01)                     | 5.40 (0.02) | 7.95 (0.07) | 12.9 (0.2) | 18.3 (0.1) |
| <i>Deviation PTW_60019_1/ PTW_60019_2</i> |                                    | -0.6%                           | -0.9%       | 5.9%        | 9.1%       | 12.6%      |
| IBA_Razor_Nanochamber                     | Linac1                             | 3.74 (0.01)                     | 5.27 (0.05) | 7.49 (0.15) | 11.5 (0.2) | 15.2 (0.4) |

255

### 256 3.3. Comparison of the $DAP_w$ and point dose approaches

257 Figure 4 shows the  $DAP_w$  measured with the reference chamber on the two linacs. Errors bars are  
258 plotted considering a 0.63% uncertainty on the  $N_{DAP,w,f_{clin}}$ <sup>12</sup> and a repeatability of 0.05% but they are

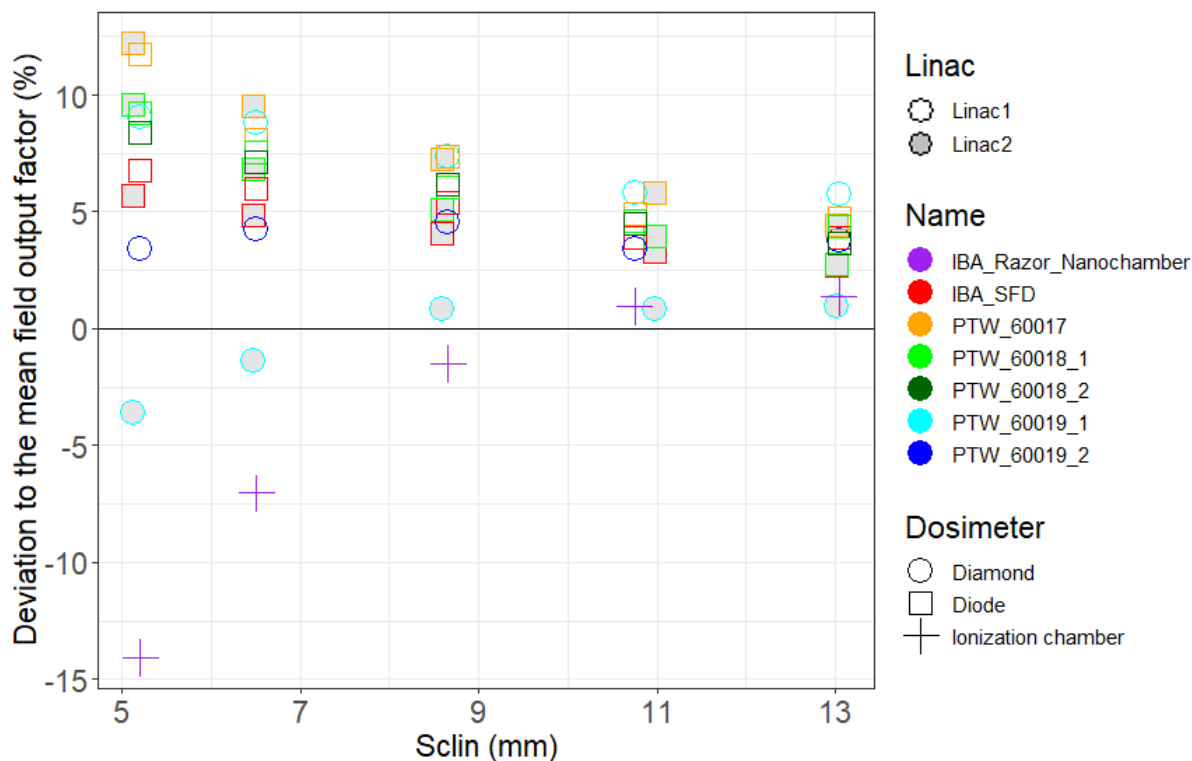
259 smaller than the symbols. This confirms that DAP measurements associated to a small uncertainty can  
 260 be performed in radiation oncology departments in small fields.



261  
 262 *Figure 4 : DAP<sub>w</sub> measured by the reference chamber on two linacs*

263 Using  $k_{vol,clin}$  values, field output factors were derived from the DAP<sub>w</sub> measurement with the  
 264 reference chamber associated to profiles measurements for each detectors. The comparison against the  
 265 mean field output factors defined in section 3.1. is shown in Figure 5. Large deviations (up to 14% for  
 266 the smallest field size) are observed and no detector used for the determination of the  $k_{vol,clin}$  value  
 267 gives a field output factor in agreement with the reference within 5 % for all field sizes. For the two  
 268 largest fields (15 and 12.5 mm diameter), a mean deviation of 4% is found between the “DAP to dose  
 269 point” and the IAEA TRS 483 methodologies. Deviation then increases with decreasing field size with  
 270 a quasi-systematic overestimation of the value derived from DAP<sub>w</sub> measurements for solid detectors  
 271 whereas a large underestimation is observed for the IBA\_Razor\_Nanochamber. Results for the  
 272 PTW\_60019 show a large variability between the 2 linacs and between PTW\_60019\_1 and  
 273 PTW\_60019\_2. This is attributed to the variability of the measurements in the profile tails: for the 6 mm  
 274 field size, at 15 mm from the axis, the relative dose measured by the PTW\_60019\_1 is 0.2% on Linac1  
 275 and 0.8% on Linac2 whereas the dose measured with the PTW\_60019\_2 is 0.5% on Linac1. On the  
 276 contrary, the profile penumbra and tail measured by the IBA\_SFD and PTW\_60018 are much more  
 277 reproducible: 0.4% for the IBA\_SFD at 15 mm from the axis on both linacs and 0.3% for the  
 278 PTW\_60018\_1 on both linacs and PTW\_60018\_2. These small differences have a non-negligible impact  
 279 on the volume averaging correction factor since the integration is performed on a 15 mm radius circle.

280 The surface covered by the profile penumbra and tail is thus important as their contribution to the dose  
 281 integral.



282  
 283 *Figure 5 : Field output factors derived from a  $DAP_w$  measurement and a  $k_{vol,f_{clin}}$  value for various detectors. Deviation*  
 284 *against the mean field output factor defined in 3.1. is plotted.*

285

#### 286 4. Discussion

287 This study evaluated the feasibility of deriving a field output factor in small fields from  
 288 measurements with a reference chamber calibrated in terms of  $DAP_w$ . The formalism to do so requires  
 289 a volume averaging correction factor to determine the dose integral over the sensitive area of the  
 290 reference chamber. Results show that this correction factor is critical and that none of the detectors  
 291 studied provide a satisfactory “ $DAP_w$  to point dose” conversion based on such profile measurements. A  
 292 large spread of the  $k_{vol,f_{clin}}$  values is observed stressing that the commercial detectors studied could not  
 293 be used for the “ $DAP_w$  to point dose methodology”. The intra-model reproducibility for the PTW\_60018  
 294 and PTW\_60019 shows contrasted results: a relative good agreement is observed for the PTW\_60018  
 295 (4.2 % maximal dispersion on the  $k_{vol,f_{clin}}$  values for both detectors and linacs) but a maximum 12.6 %  
 296 dispersion is observed for the PTW\_60019. This adds a difficulty to transfer  $DAP_w$  primary standards  
 297 to radiation oncology departments in terms of point dose since the conversion should not depend on the  
 298 specific detector used for the profile measurement. Although robust for the establishment of primary  
 299 standards in small fields, the  $DAP_w$  approach suffer difficulties to be transferred to users in terms of point  
 300 dose. The variation between detectors for field output factor measurements ( $\pm 3\%$ ) in the IAEA TRS483  
 301 approach is replaced and magnified in the  $DAP_w$  approach by the variation between detectors for beam

302 profile measurements. This study highlights the difficulty to accurately determine a beam profile in  
303 small fields and especially the scatter dose far from the axis where the energy dependence of the  
304 detectors is of primary importance <sup>21</sup>. The ideal detector for profile measurements in small fields should  
305 have a small sensitive volume to avoid incorrect determination of the width of the penumbra and be the  
306 least perturbing tissue equivalent <sup>2</sup>. Francescon *et al.* calculated with Monte Carlo correction factors for  
307 profile measurements as a function of off-axis distance <sup>22</sup>. Large correction factors (up to 1.3) were  
308 reported after the geometric field edge depending on the detector. The PTW\_60019 showed the smallest  
309 correction factors but still underestimated the dose up to 5 % at 8 mm from the central axis (for a  
310 geometric field edge at 4 mm). Lopez-Sanchez *et al.* also reported correction factors between 0.8 and  
311 1.1 in the penumbra region of a 5 mm circular cone for two ionization chambers including the  
312 IBA\_Razor\_NanoChamber <sup>19</sup>. Similarly, Underwood *et al.* reported large variation of the correction  
313 factor with off-axis distance for a PTW\_60003 Diamond detector and a PTW\_31006 PinPoint ionization  
314 chamber <sup>23</sup>. No current commercially available point detector seems to be adequate for profile  
315 measurements in small fields.

316 One default of the formalism applied to the solid detectors used in this study is that the beam profile  
317 is normalized to the beam axis without considering the fact that each detector has its own and different  
318 response on the beam axis for a given field size. However, as observed by Underwood *et al.* <sup>23</sup>, the  
319 under- or over-response of a detector on the beam axis could be compensated by an over- or under-  
320 response on the tails by normalizing the beam profiles to the detector's response in a 10 cm x 10 cm  
321 beam. At the end, such calibrated beam profiles could lead to a unique dose area product without any  
322 detector effect. Here, by normalizing the beam profile on the axis, the under- or over-response on the  
323 beam axis is ignored and there cannot be a compensation between the beam axis and the tails. The over-  
324 response at the tails can be even amplified or the under-response reduced, thus affecting the  $k_{vol}$   
325 calculation. However, the calibrated beam profiles described by Underwood *et al.* <sup>23</sup> are not compatible  
326 with the formalism proposed here : a normalized profile is needed to calculate the dose on the beam axis  
327 and consequently the detector used to measure the beam profile needs to be energy-independent on the  
328 beam axis and off axis. Solid detectors remain useful to check the consistency of the  $k_{vol}$  calculation.

329 Future work will include the investigation of radiochromic films and the development of an in-house  
330 film optical reader compatible with metrological applications. The 2D dose mapping of the beam could  
331 then be measured and the cylindrical symmetry of the circular cones would not be needed.  $k_{vol}$  could  
332 then be determined using equation (5). Other tissue equivalent point detectors like plastic scintillator  
333 could also be evaluated.

334

## 335 5. Conclusion

336 Two methodologies were compared to determine field output factor in small fields: the first  
337 described in the IAEA TRS483 based on point dose measurements and the second based on dose area  
338 product measurements with a large reference chamber, associated to volume averaging correction

339 derived from profiles or 2D dose map measurements. Reference field output factors based on point  
 340 measurements were determined on two linacs with several detectors. A standard deviation over all  
 341 detector smaller than 1.4% was achieved. Volume averaging correction factors were determined with  
 342 numerous detectors and showed large variations depending on the detector with a spread up to 26% for  
 343 the smallest field size. Due to this large variability depending on the detector used for the profile  
 344 measurement, the  $DAP_w$  to point dose methodology can not easily be transferred to users in terms of  
 345 absorbed dose at a point although it is promising to establish dosimetric standards in a primary  
 346 laboratory.

347

348

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