

Challenges in MHD modelling in fusion devices Guido T. A. Huijsmans

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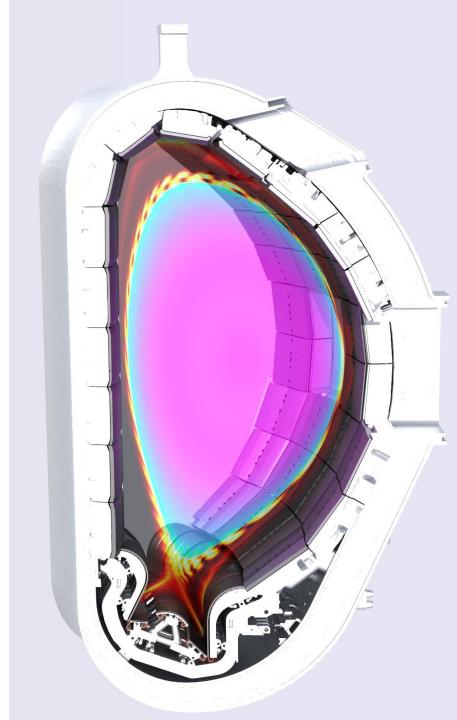
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Challenges in MHD modelling in fusion devices

Guido Huijsmans





Outline

• Fusion –Tokamak, ITER

• Magnetohydrodynamic (MHD) Instabilities –Edge localised modes (ELMs)

Nonlinear MHD code JOREK

- finite elements
- implicit time evolution
- parallelisation

Particles

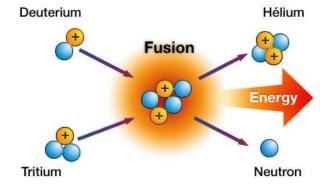
- neutrals, impurity transport

Conclusion



Fusion Energy

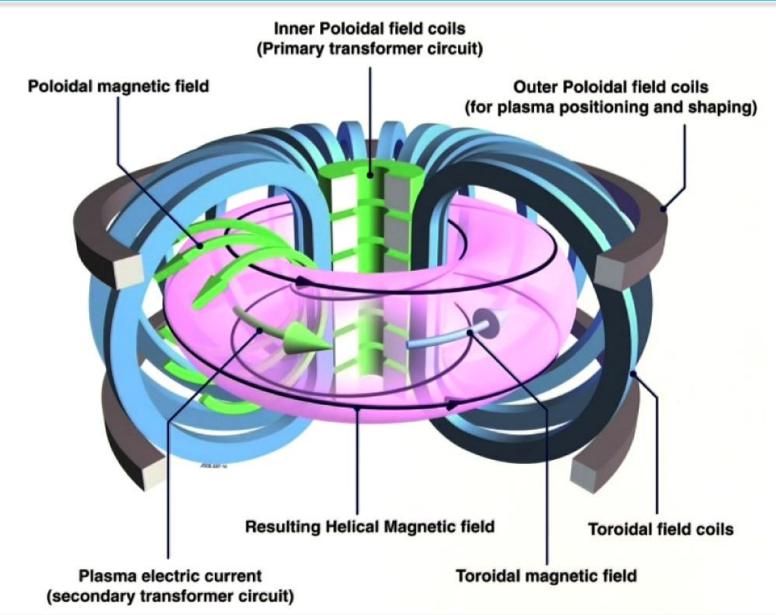
- The fusion of light atoms release energy ${}^{2}D+{}^{3}T = {}^{4}He + n + 17.6 \text{ MeV}$
 - energy source of the stars
 - potential CO₂ free, safe energy source



- The reaction requires very high temperatures (150 M°)
 das is ionised and becomes plasma (free ions and electronic)
 - gas is ionised and becomes plasma (free ions and electrons)
- The hot plasma can be contained by a magnetic field
 - tokamak is the most advanced approach
 - fusion power record in JET : 16 MW (in 1997)
 - next step: ITER



Tokamak





The ITER Project

• Goals:

- Fusion power amplification factor Q=10 for 300-500s

Fusion power ~500 MW

- Steady state operation at Q=5 (3000s)

7 ITER Partners

EU, China, India, Japan, Korea, Russia, USA

ITER Tokamak

Major radius : 6.2m Minor radius : 2.0m Toroidal field : 5.3T Plasma current : 15 MA First plasma : end 2025 Fusion power operation: end 2035



Guido Huijsmans, PASC 2019, Zurich, 12-14/6/2019

ITER Building Site (march 2019)

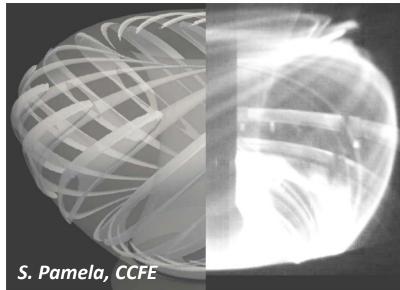




MHD Instabilities

- Large scale magnetic instabilities of the plasma
 - -Driven unstable by pressure gradients and plasma current
 - Limit global pressure, current and local pressure, current gradients
 - -Typical time scales : 1 millisecond
 - -Leading to fast losses of plasma energy and density
 - Large transitory energy fluxes to the plasma facing components
- Disruptions:
 - Global MHD instability leads to fast plasma termination
- Edge Localised Modes (ELMs):
 - Local MHD instability in outer 20% of the plasma leading to repetitive energy and density losses of 1-10% (at 1-100Hz)

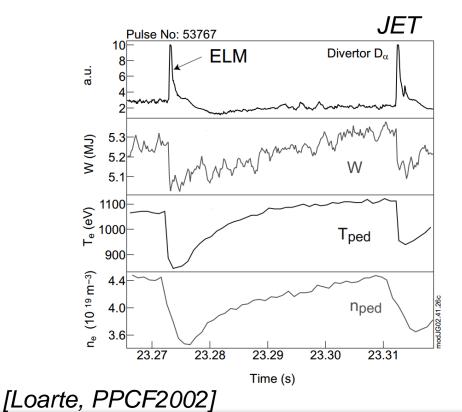
JOREK simulation MAST



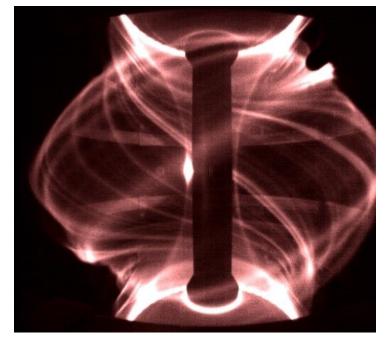


Edge Localised Modes (ELMs)

- H-mode regime: spontaneous stabilisation of turbulence at the plasma edge leads to large pressure gradients in the outer ~5% of the plasma
 - standard operating regime in ITER
- Edge pressure gradient is not limited by transport but by an MHD instability
- Edge Localised Mode (ELM) removes up to 10% of the plasma energy in several hundred microseconds



MAST



[Kirk, MAST]

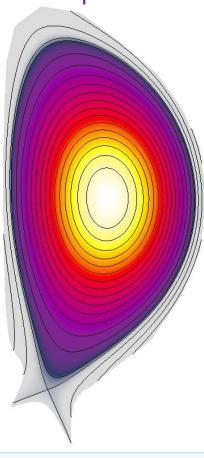


Magneto-Hydro-Dynamics (MHD)

• Theoretical model (H. Alfven, 1942)

- description of the plasma as a electrically conducting fluid embedded in a time varying magnetic field
 - Combining Navier-Stokes fluid equations with (pre-) Maxwell's equations
 - Conservation of mass, momentum, energy and magnetic flux
- applications: plasmas, solar physics, astrophysics, dynamos

$$\begin{aligned} \frac{\partial \rho}{\partial t} &= -\nabla \cdot \left(\rho \vec{v}\right) + \nabla \cdot D\nabla \rho + S_{\rho} & \frac{\partial \vec{B}}{\partial t} = \nabla \times \left(\vec{v} \times \vec{B} - \eta \vec{J}\right) \\ \rho \frac{\partial \vec{v}}{\partial t} &= -\rho \vec{v} \cdot \nabla \vec{v} - \nabla \left(\rho T\right) + \vec{J} \times \vec{B} & \mu_0 \vec{J} = \nabla \times \vec{B}, \quad \nabla \cdot \vec{B} = 0 \\ \frac{\partial \rho T}{\partial t} &= -\vec{v} \cdot \nabla \rho T - \gamma \rho T \nabla \cdot \vec{v} + \nabla \cdot \kappa \nabla T + S_{\rho} \end{aligned}$$





Challenges MHD Simulations

- Time scales:
 - Depending on the application the time scale of interest varies from 1 microsecond to 100's milliseconds
 - Fast waves : 10⁻⁸ s, Alfven waves : 10⁻⁶ s, sound waves : 10⁻⁴ s
- Length scales:
 - MHD instabilities develop thin current sheets
 - Magnetic Reynolds number $S \sim 10^8 10^{10}$ (i.e. normalised resistivity⁻¹)
 - Layer width scales as S^{-1/2}
- Anisotropy
 - heat conduction is very much larger along a magnetic field line compared to the perpendicular direction
 - Conduction : $K_{/\!/}\,/\,K_{\perp}\,{\sim}\,10^{10}$



Non-linear MHD code JOREK

- JOREK code solves the (extended) MHD equations in 3D general tokamak geometry
 - -Closed and open field lines, plasma wall interaction, conducting structures
 - -Main applications: ELMs and disruptions
- now developed with the EU fusion program
 - -14 Fusion Labs + Universities, ~25 persons
 - -GIT repository, wiki, decentralised development

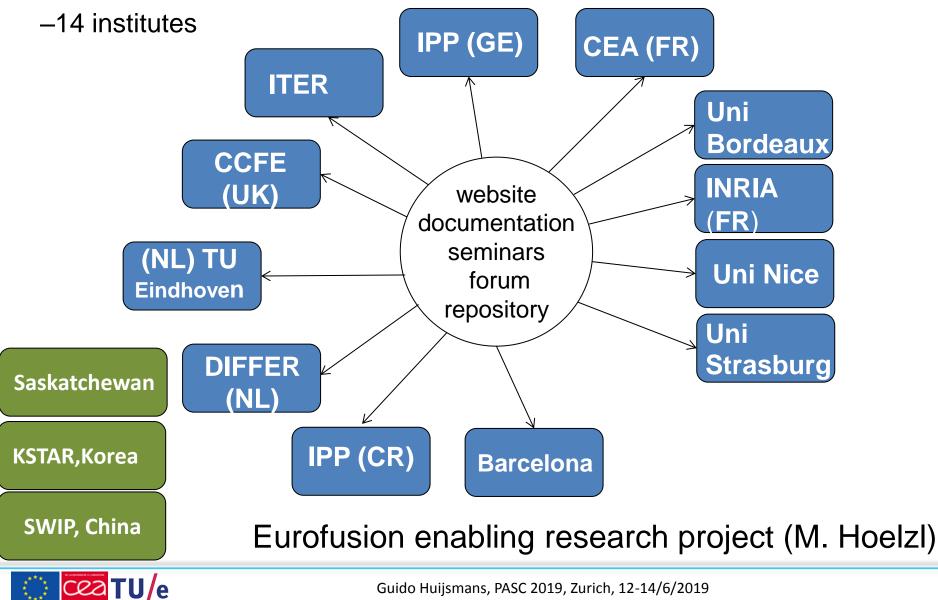
Characteristics

- -Cubic (Bezier) Finite element representation in the poloidal plane
 - Extension of cubic Hermite elements
- -Fourier series in the toroidal direction
- -Fully implicit time evolution
- -MPI/OpenMP parallelisation



JOREK Network (2019)

Decentralised development



Bezier Finite Elements

- Bezier patches are widely used in CAD, computer graphics
 - to describe 2D surface in 3D physical space
 - parametrised in local coordinates (s,t)
 - X(s,t), Y(s,t), Z(s,t)
 - Cubic bezier patch defined by 16 control points
 - here the height represents a physics variable
 - (R,Z) space and variables described by Bezier patches : Isoparametric representation: R(s,t), Z(s,t), ψ (s,t)
 - values and derivatives continuous in space (C¹)
 - but not continuous in local (s,t) coordinates
 - generalisation of cubic Hermite finite elements
 - Allows local refinement



 P_{33}

t

 P_{03}

 P_{30}



Guido Huijsmans, PASC 2019, Zurich, 12-14/6/2019

 P_{00}

R = R(s,t)

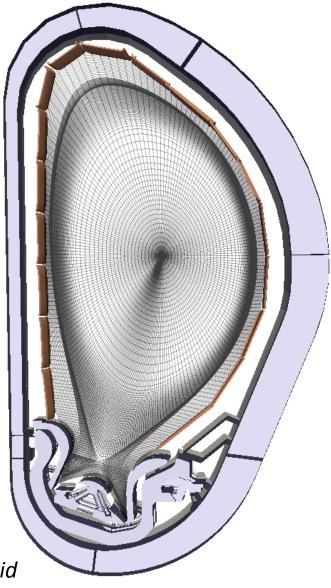
Z = Z(s,t)

 $\psi = \psi(s,t)$

JOREK Grids

- Elements aligned to magnetic geometry
 - the curved boundaries of the Bezier patches can be accurately aligned with the magnetic geometry
 - alignment and higher order (cubic) elements allow an accurate description of the anisotropy of the heat conduction ($K_{//}/K_{\perp}=10^{10}$)

- Aligned grids can be extended (nonaligned) up to the plasma facing components
 - essential for an accurate description of the plasma-wall interaction



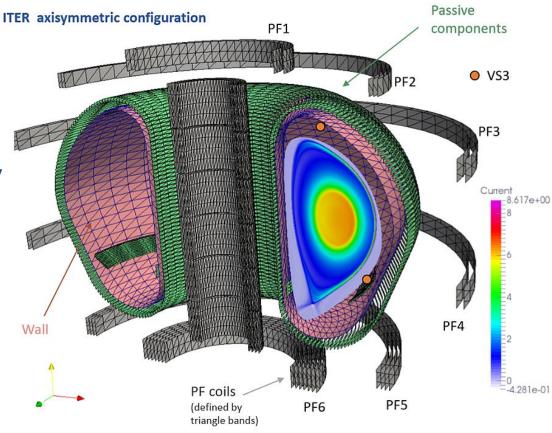
example ITER grid



Boundary Conditions

- The evolution of magnetic fields and currents in coils and conducting structures can be solved independently from the main plasma
 - -Solved (once) using the code STARWALL (boundary element method)
- Provides boundary conditions for the magnetic fields at the JOREK domain boundary

$$-B_{normal}/B_{tan} = M$$





Implicit time evolution

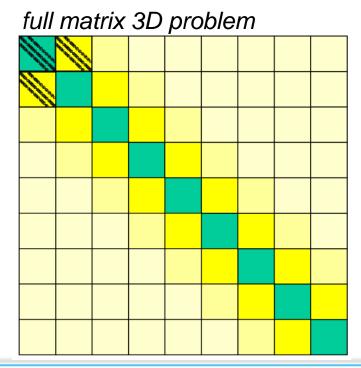
- The time scales of interest can vary from the Alfven time (microsecond) to slow growing resistive instabilities (10s of seconds in ITER)
- Explicit schemes would be limited by the fast wave frequency (full MHD) or by Alfven waves (reduced MHD)
 - Not practical for most MHD tokamak applications
- Implicit scheme allows large time steps resolving the phenomena of interest
 - Linearised Crank-Nicholson or BDF (Gear's) schemes

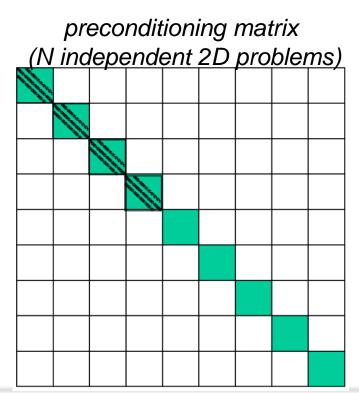
$$\frac{\partial A(\vec{y})}{\partial t} = B(\vec{y}) \quad \Rightarrow \quad \left(\frac{\partial A(\vec{y}_n)}{\partial y} - \frac{1}{2}\delta t \frac{\partial B(\vec{y}_n)}{\partial y}\right)\delta \vec{y} = B(\vec{y}_n)\delta t$$

- Implicit schemes yields large matrix problem at each time step
 - 5x10⁴ nodes, 8 variables, 4 dof per node, 15 Fourier modes: N=5x10⁷
 - Challenging for large scale parallelisation

Preconditioned GMRES

- Matrix problem (~10⁷unknowns) solved using preconditioned GMRES
- standard preconditioners not satisfactory for MHD
 - condition number MHD matrices very large
- use physics-based preconditioner
 - ignore non-linear coupling of N toroidal Fourier modes in preconditioning matrix
 - N independent, sparse, blocks solved using PaStiX library

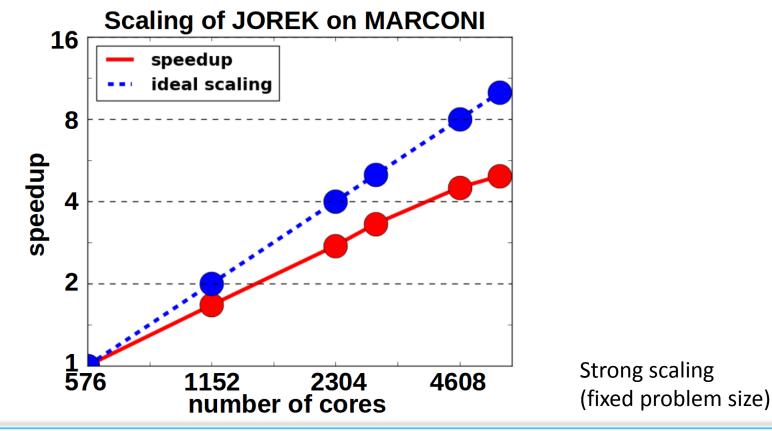






JOREK Parallelisation

- Parallelisation : MPI+openMP,
 - # CPU : mostly due to memory requirements
- 3 main parts:
 - Matrix construction, factorisation preconditioner and GMRES solve

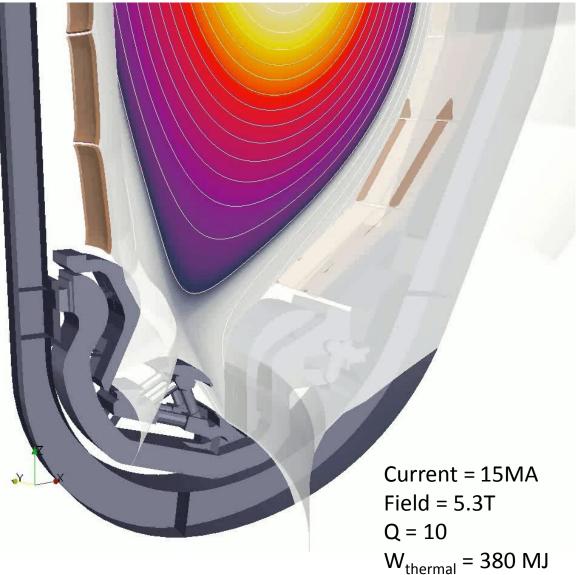




ITER ELM Simulation

- Ballooning instability –n=10
- Losses:
 - -Energy loss : 1%
 - –Density loss : 2%
 - -ELM depth : ~12cm
 - –Duration 250 micro sec

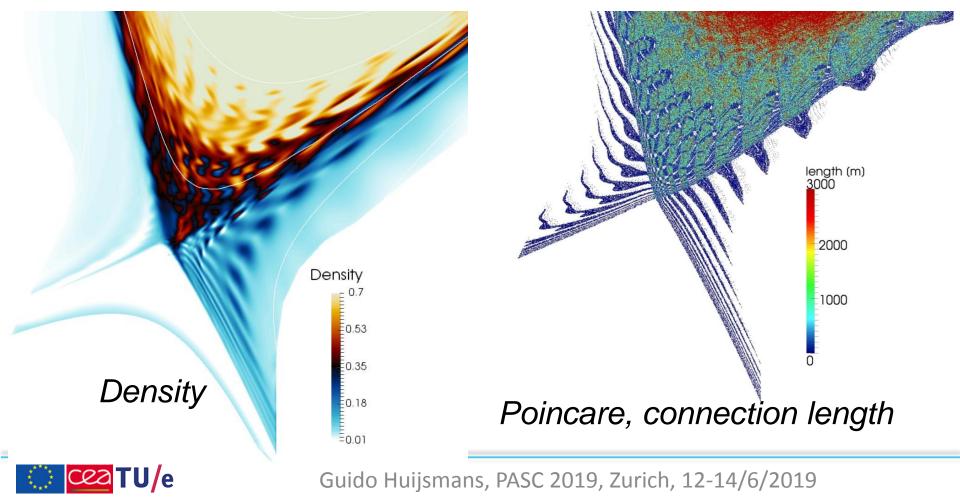
Plasma temperature (0-20keV) Heat flux to divertor (0-3 GW/m²)





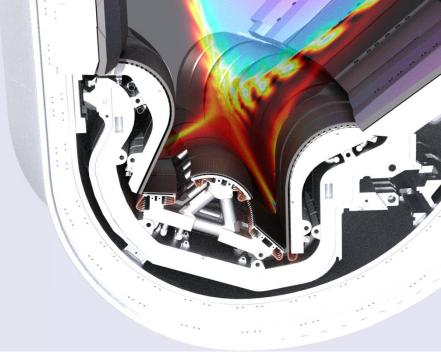
ELM Energy Losses

- Energy loss during ELMs is due to two mechanisms:
 - Ejection of filaments : convective energy loss
 - Formation of magnetic tangles: conduction parallel to perturbed field lines
 - conductive convective ELMs



Plasma-Wall Interaction

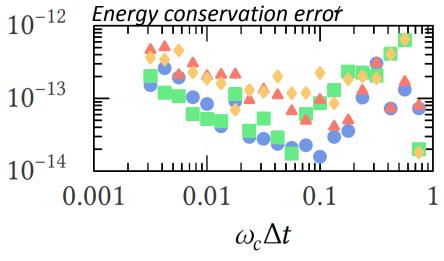
- To describe the consequences of the MHD instabilities (ELMs, disruptions), the plasma-wall interaction needs to be accurately modeled:
 - MHD model extended with "divertor" boundary conditions:
 - Plasma flows into the wall at Mach one (or larger)
 - Relation between conductive and convective energy fluxes: K\(\nabla_{//}\)T=c n v_{//}\(T = \label{V} = \label{V
 - Discrete particles to model
 - recycling of plasma into neutrals,
 - ionisation, recombination, charge exchange
 - Impurities : sputtering and spreading due to MHD instabilities



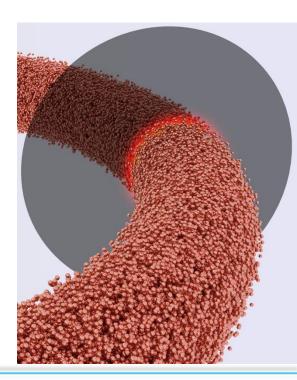


Particles

- Particles are followed in the time evolving magnetic and electric field of the MHD fluid
 - full orbit using well-known Boris method (with correction toroidal geometry)
 - particles are followed in real space (R,Z, ϕ) and finite element space (s,t, ϕ)
 - charge states are evolving in time (Ionisation, recombination, CX)
 - Particle-background collisions with binary collision model
 - sputtering model for impurity and neutral sources



Energy conservation independent of time step Δt , momentum conservation ${}^{\sim}\!\Delta t^2$





Kinetic Neutrals

Coupling of JOREK MHD fluid and particle

-Particle contributions become sources in MHD equations

• Conservative form:

$$\begin{aligned} \frac{\partial \rho}{\partial t} + \nabla \cdot \left(\rho \vec{v}\right) &= \mathbf{S}_{\rho} \\ \frac{\partial \left(\rho \vec{v}\right)}{\partial t} + \nabla \cdot \left(\rho \vec{v} \vec{v}\right) + \nabla \cdot \overline{P} - \vec{J} \times \vec{B} = \vec{S}_{\nu} \\ \frac{\partial}{\partial t} \left(\frac{1}{2} \rho v^{2} + \frac{3}{2} \rho T\right) + \nabla \cdot \left(\frac{1}{2} \rho v^{2} \vec{v} + \frac{3}{2} \rho T \vec{v} + \vec{v} \cdot \overline{P}\right) &= \mathbf{S}_{E} \end{aligned}$$

JOREK form

$$\begin{split} &\frac{\partial\rho}{\partial t} + \nabla \cdot \left(\rho \vec{v}\right) = S_{\rho} \\ &\rho \frac{\partial \vec{v}}{\partial t} + \rho \left(\nabla \cdot \vec{v}\right) \vec{v} + \nabla \cdot \overline{P} = \vec{S}_{v} - \vec{v}S_{\rho} \\ &\frac{\partial \left(\frac{3}{2}\rho T\right)}{\partial t} + \vec{v} \cdot \nabla \left(\frac{3}{2}\rho T\right) + \frac{5}{2}\rho T \left(\nabla \cdot \vec{v}\right) = S_{E} - vS_{v} + \frac{1}{2}v^{2}S_{\rho} \end{split}$$

[D. van Vugt , S. Franssen]



Sources, Moments

- The sources are given by: $S_{\rho}(\vec{x}) = \int mf(\vec{x}, \vec{v}) d\vec{v}$ $S_{\nu}(\vec{x}) = \int m\vec{v}f(\vec{x}, \vec{v}) d\vec{v}$ $S_{E}(\vec{x}) = \int \frac{1}{2}mv^{2}f(\vec{x}, \vec{v}) d\vec{v}$
- Express sources in JOREK finite element representation to obtain a continuous function from a list of discrete particles

$$\tilde{S}_{\rho}\left(\vec{x}\right) = \sum_{ijk} p_{\rho,ijk} H_{ij}\left(s,t\right) H_{\varphi,k}\left(\varphi\right)$$

• Projection using weak form (system of equations to be solved)

$$\int v^*(\vec{x}) \tilde{S}_{\rho}(\vec{x}) d\vec{x} = \int v^* S_{\rho}(\vec{x}) d\vec{x}$$
$$\int v^*(s,t,\varphi) \sum_{ijk} p_{\rho,ijk} H_{ij}(s,t) H_{\varphi,k}(\varphi) d\vec{x} = \int v^* mf(\vec{x},\vec{v}) d\vec{v} d\vec{x}$$
$$\int v^*(s,t,\varphi) \sum_{ijk} p_{\rho,ijk} H_{ij}(s,t) H_{\varphi,k}(\varphi) d\vec{x} = \sum_n v^* mw_n \delta(\vec{x} - \vec{x}_n)$$



Moments: smoothing

- Some smoothing is required –depending on number of particles
- Modified projection equation:

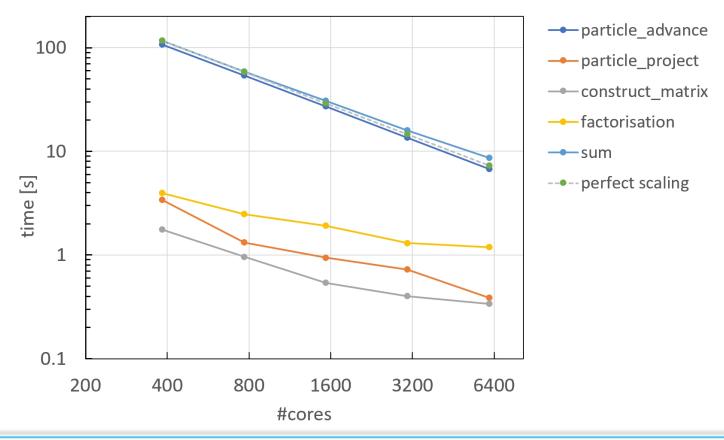
$$\int v^* (\vec{x}) (1 - \lambda \nabla^2 - \varsigma \nabla^4) \tilde{S}_{\rho} (\vec{x}) d\vec{x} = \int v^* S_{\rho} (\vec{x}) d\vec{x}$$
$$\int (v^* \tilde{S}_{\rho} + \lambda \nabla v \cdot \nabla \tilde{S}_{\rho} + \varsigma \nabla^2 v^* \nabla^2 \tilde{S}_{\rho}) d\vec{x} = \int v^* S_{\rho} (\vec{x}) d\vec{x}$$

- LHS matrix is calculated and factorised once (using MUMPS)
- RHS is collected at every particle step
 - Important for conservation properties
- Projection (i.e. MUMPS solve) at every JOREK fluid time step



Parallelisation Scaling

- Good parallel scaling as long as particles dominate total time
 - 4x10⁷ particles, 1600 elements, 8 toroidal harmonics
 - Marconi, Skylake (1 mpi, 48 threads per node)
 - efficiency 84% at 6000 cores



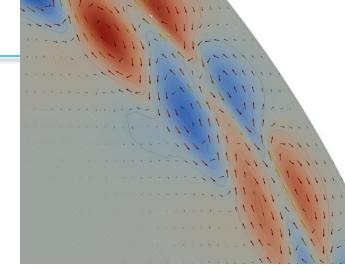


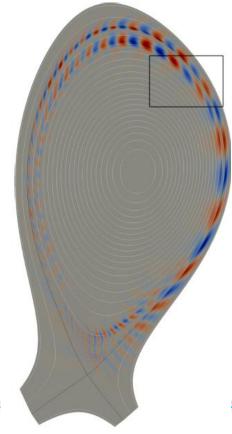
Tungsten (W) transport and ELMs

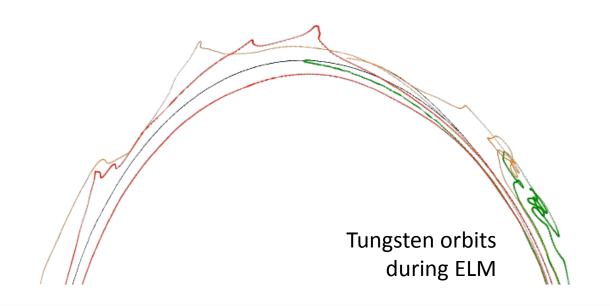
- Modern tokamaks (and ITER) have Tungsten divertors
 - high melting temperature
 - low retention of Tritium
- Even low concentrations of W lead to large radiation losses
 - leading to disruptions
- Main source of W is due to sputtering of the divertor due to large energy deposition due to ELMs
 - i.e. produces W in the divertor, outside main plasma
- However, ELMs also expel Tungsten from the main plasma
 - at least in current experiments
- JOREK MHD + W-particles simulations (D. van Vugt, TUe)
 - Study the ELM induced W transport
 - W production due to sputtering

ELM induced W Transport

- 3D vortices of the ELM instability at the edge of the plasma
 - associated electric field perturbs W
 orbits and causes radial transport
 - -magnetic field perturbation unimportant
- Transport is due 3D to interchange motion







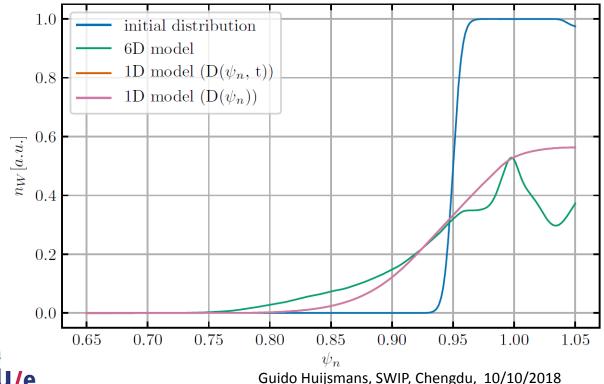
TU/e

ELM induced W transport

• Effective ELM induced W radial transport (in 1D) is diffusive

-In the case of W accumulation inside the plasma ELMs expel Tungsten

- As in current experiments
- -In ITER, ELMs are predicted to move Tungsten into the plasma
 - Due to inter-ELM profiles of Tungsten mainly outside the main plasma
 - Opposite to current experiments





Summary

- MHD instabilities are one of the main concerns for ITER operation
 - ELMS, disruptions
 - MHD instabilities must be controlled in ITER
- Nonlinear MHD code JOREK
 - simulation of MHD and its control in current and future fusion experiments
 - MHD+particle model for plasma wall interaction, fast particles
- HPC requirements
 - fully implicit scheme due to large range of time scales
 - Large sparse matrices ⇒ memory requirements, parallisation inefficiency beyond several 1000 cores (fluid model)
 - MHD+particle model scales much better
- Next: extending particle model
 - verification and validation: towards a predictive capability
 - fast α -particles, massive material injection

