

# Millimeter-sized particle sensor using a wide field of view monolithic lens assembly for light scattering analysis in Fourier domain

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## ABSTRACT

We present our latest advances in the field of miniature optical particulate matter sensors. By illuminating a single particle in an air channel, one can record the light scattering signature with a CMOS image sensor and then classify particles. This signature is optically pre-processed with an advanced, millimeter-sized, monolithic, refracto-reflective optical system. It performs notably a Fourier transform with very wide field of view of scattering angles, and includes as well integrated fluidics and alignment. Functional prototypes were fabricated using laser micro machining on glass, selective polishing, and were replicated with epoxy resin using a molding process.

**Keywords:** Particulate matter; Light-scattering; CMOS image sensor; Miniature sensor; Miniature optics; Air quality.

## 1. INTRODUCTION

Particulate Matter (PM) is a class of pollutant known to have serious medical impacts [1][2]. It is composed of suspended airborne particles of size ranging from a few nanometers to a few micrometers. In particular, the regulated subclass  $PM_{2.5}$  refers to particles smaller than  $2.5\mu m$ . The IARC (International Agency for Research on Cancer) have classified  $PM_{2.5}$  as a group 1 agent (known carcinogenic agent) [3]. In addition, a meta-analysis conducted by the US-EPA have concluded on the causality of premature death by  $PM_{2.5}$  exposure [4]. Beyond  $PM_{2.5}$ , the unregulated subclass  $PM_1$  (particles smaller than one micron) is highly suspected of being far more harmful than  $PM_{2.5}$  as it can penetrate the respiratory system more deeply [5]. Therefore, sensing and monitoring of small particles is of crucial importance. However, we still rely on conventional air quality monitoring ground stations that cannot deliver the required spatio-temporal resolution of air quality (indoor and outdoor [6]). This raises the urgent need for personal air quality monitors that are low cost and portable [7][8]. In this document, we report our latest developments concerning miniature optical PM sensors.

### 1.1. Light-scattering & Miniature PM monitors

There is a wide range of techniques capable of sensing particulate matter [9]. Among them, we believe that the family of light scattering sensors is the most suited for miniaturization. The light scattering set-up (already used in the majority of existing low-cost  $PM_{2.5}$  sensors) shows great simplicity and good sensitivity. The technique consists of a visible light source (or near infrared) used for the illumination of an air chamber and an off-axis photo-detector with respect to the optical axis (see Figure 1). The latter would only detect light that was deviated (i.e. scattered) by a particle in the chamber.

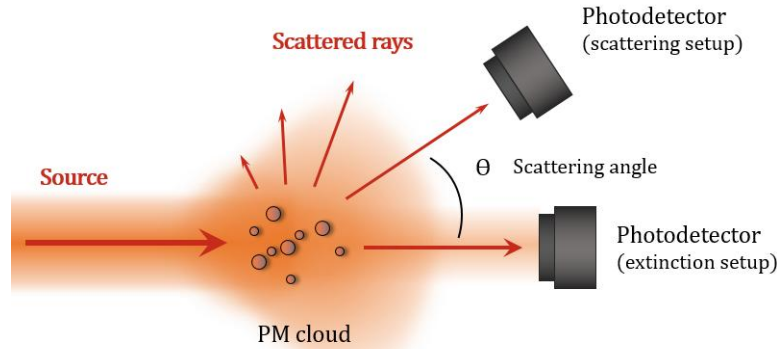


Figure 1: Illustration of the light-scattering technique

Scaling down optical  $PM_{2.5}$  &  $PM_{10}$  sensors usually involves co-integration of light sources, photodetectors as well as fluidics using techniques developed for silicon microfabrication, optronics and lab-on-chips [10][11]. In particular, our early designs includes planar photonic integrated circuits with active components such as a light source and photodiodes that are both coupled to passive optics such as silicon-based waveguides. The air channel is vertically drilled out of the substrate [12].

Particle concentration can be estimated from the total scattered intensity collected by the off-axis photodetector. However, useful information such as their nature and sizes remain unknown. Estimating these optical parameters (refractive index and diameter) is achievable by measuring the ‘light scattering signature’ of a particle.

## 1.2. Lorenz-Mie theory & scattering signatures

A particle’s ‘scattering signature’ refers to its scattering efficiency as a function of the angle. It depends on the geometry of the particle (shape and size), its refractive index and the wavelength of the excitation light in the surrounding medium. Being able to calculate such signature allows for the classification of particles [13].

The Lorenz-Mie theory [14][15] is the most common description of light-scattering. It solves the electromagnetic problem of a uniform sphere illuminated by a monochromatic plane wave. Despite its simple hypothesis, this theory has proved to be quite robust. It shows for example that the smaller the particle is (compared to the excitation wavelength), the more spherical the scattering signature is. For a large particle (larger than a few wavelengths), most of the scattered intensity is deviated with smaller angles and sides lobes appear as the diameter increases. The signatures varies also with the complex refractive index of the sphere.

## 2. DESIGNING THE OPTICAL SYSTEM

We have developed a first generation of optical PM sensor that is the base frame for our new generation PM sensor (see hereafter). The former is able to count and record a particle’s scattering signature projected onto a holed CMOS image sensor (that is both a detector and a fluidic channel). More details are presented in reference [16] (same conference). Similar designs are also found in conference papers [17][18] and in patent [19].

The recorded signature is optically transformed through a planar, lens-free projection with a short working distance. The geometry is optimized to maximize both the sensitivity of low intensity scattered light as well as the Field of View (FoV) of scattered angles. We abusively define the FoV as the range of evaluated scattering angles. In the first PM sensor generation, the FoV is limited by the geometry as we can evaluate scattering signatures within a FoV of only a few tens of degrees. There is little margin of improvement that can be made using the lens-free planar projection. Moreover, the uncertain position of the particle within the illumination beam can result in an affine transformation of the image as well as a blurring effect, with a shifted range of evaluated scattering angles. This last part is taken into account by our image analysis procedure but one may want to simplify the computing part as much as possible for future portable applications.

Some of these identified problems (the narrow field of view and the influence of the position of the scattering particle) concerning the direct projection method can be addressed. The suggested solutions resulted in the design and fabrication

of our miniature optical system, shown in Figure 2. This piece was made from a single fused silica glass substrate and contains several optical surfaces, alignments and fluidics. It is included inside a small volume of about 3 mm x 6 mm x 1 mm. More information can be found in the patent [20].

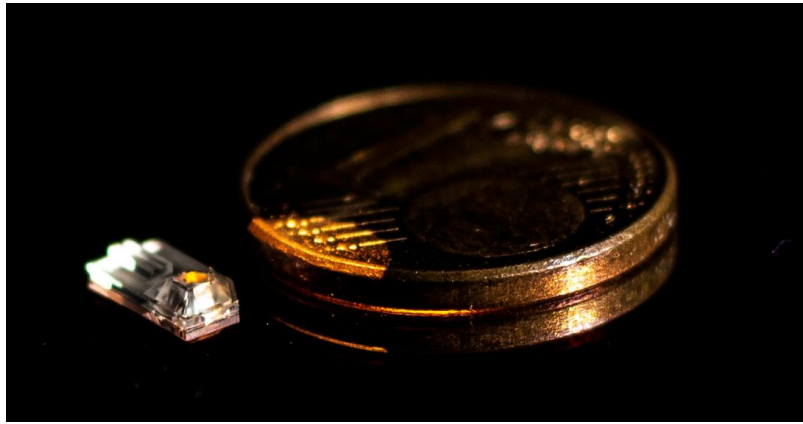


Figure 2: Photography of the miniature lens system next to a one-cent coin (EU)

### 2.1. Position insensitivity

In most non-miniaturized light-scattering photometers, the position of the particle has no impact on the measures. Indeed, the range of positions allowed for the particle is very small as compared to the optical path of scattered rays. Noteworthy, errors induced by the particle position have also been reported by others teams working on scaling down their sensors [21]. In our case, the impacts of the particle position include translation, magnification and rotation of the recorded image; a superposition of shifted signatures can be generated by clouds of particles, resulting in a position blur; as a corollary, the detection of a moving particle (with respect to the image integration time) results in a motion blur.

In short, position insensitivity can be achieved with a far-field set-up. An equivalent set-up is the common d-f lens system: The detector array is placed at the image focal plane of a thin lens (simplified model) so that the object is seen at infinity. Consequently, the detector can record an angular image by refocusing parallel rays. Let us consider the object (a particle or a cloud of particles) as a punctual source (or several punctual sources), at unspecified positions and casting rays which intensity vary according to the scattering angle. The detector array will then directly record the scattering signature. The recorded image is not modified by displacing the particle as the same scattered rays are always seen under the same angles (see Figure 3).

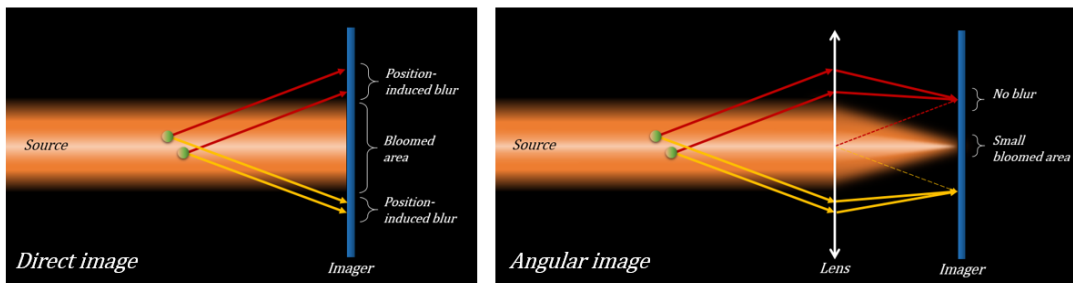


Figure 3: Illustration of the d-f setup to perform angular imaging by refocusing parallel scattered rays

Using Fourier's harmonic description of the d-f set-up [22], one can show that the information on the position of the particle is only carried by the phase of the wave at the image focal plane of the lens. The angular image (i.e. the scattering signature) is carried by the amplitude of the wave at this focal plane. A simple photo-detector array like ours is only sensitive to the amplitude: the recorded image is purely an image of the scattering signature, in the Fourier domain. This optical pre-treatment of the scattering signature dramatically simplifies the analysis of the image taken by the retina, removing the need for energy-costly image processing.

## 2.2. Asymmetric crown shape

Let us consider a lens system coupled to a detector array. A factor that limits the FoV is, for instance, the pupil of the system. Our idea behind improving the FoV for light scattering analysis is to merge several of these subsystems around a perpendicular air channel in a crown shape, as illustrated in Figure 4. The edges of each subsystem may contain aberrations or unwanted artefacts that we call ‘blind fields’, especially at the limit of two merged ones where we may observe cross-talk effects between the subsystems.

By taking advantage of the symmetry of the scattering signature around the optical axis, one can sacrifice a bit of redundancy by facing half of the lenses toward the blind fields of the other halves. The resulting design is an asymmetric crown shape with an uneven number of optical subsystems arranged around a perpendicular air channel. An example is shown in Figure 4 with five subsystems (modeled as thin lenses).

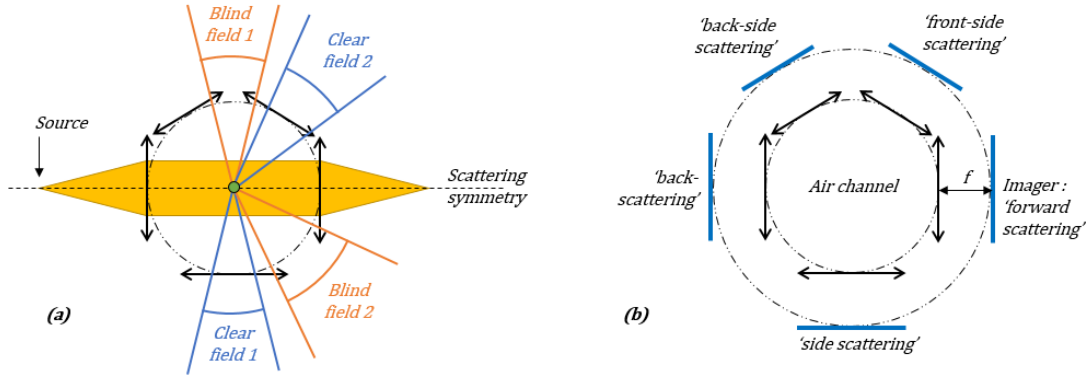


Figure 4: Principle of blind fields asymmetrically coupled to clear fields (a). Lenses coupled with imagers in Fourier planes (b)

In this design, the FoV can be - in theory - as wide as  $180^\circ$ . The limiting factor is the surface bloomed by the illumination beam (which is orders of magnitude more intense than the scattered intensity). For a collimated beam (as in Figure 4), the bloomed area is at best, the size of the diffraction spot of our optics plus the point spread function of our retina. For a diverging (or converging) beam, the bloomed area is convoluted with associated angles within the beam divergence.

## 2.3. Compact optical subsystems with coincidental Fourier planes

Each optical subsystem must meet a certain set of specifications: it must be as compact as possible; it must also fold its Fourier plane (i.e. image focal plane) onto a plane perpendicular to the fluidic channel so that all subsystems Fourier planes are coincidental. This set-up enables the use of a single holed retina (in a fashion similar to our first-generation PM sensor) to image all Fourier planes on separate regions of interest.

We design in Figure 5 an optical subsystem composed of two spherical diopters and a  $45^\circ$  spherical internal reflector that folds the image focal plane. The surface can be covered with a metallic reflective layer such as aluminum or gold. Alternatively, no reflective layer is used as the internal reflections within the material can be efficient enough.

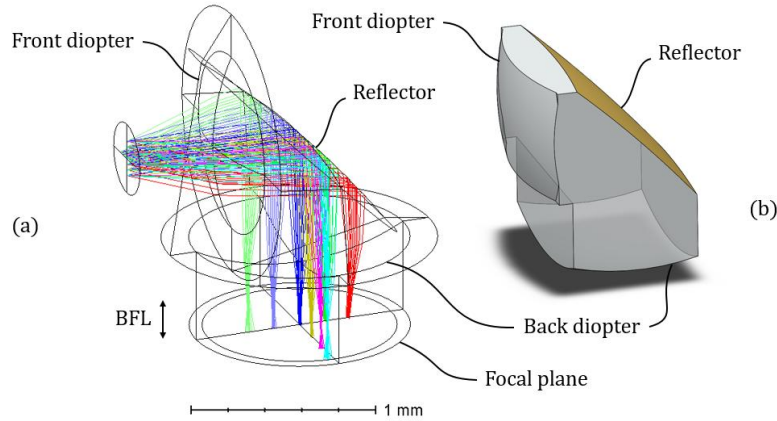


Figure 5: Design of the refracto-reflective optical subsystem. (a) Ray tracing view from Zemax Optic Studio. (b) 3D view of the truncated subsystem.

Every surface participates to the focusing of rays so that we can obtain a good optical system with few aberrations for our application and a short back focal length ( $BFL = 0.37 \text{ mm}$ ). The subsystem takes advantage of three surfaces out of a same volume, thus can be manufactured out of a unitary piece. For this prototype, the material used for the design is fused silica glass, but it can also work with most optical polymers. This refracto-reflective subsystem was designed using the optimization tools of Zemax Optic Studio software in sequential mode (Figure 5.a). Compactness is then improved by truncating such optical surfaces (Figure 5.b).

#### 2.4. Subsystem merging and fiber alignment

Five identical optical subsystems are merged into a unitary piece. The resulting model is rendered in Figure 6. It contains the merged subsystems around a vertical fluidic channel. Note that the front surfaces (first dioptrers) are part of the inside walls of the channel.

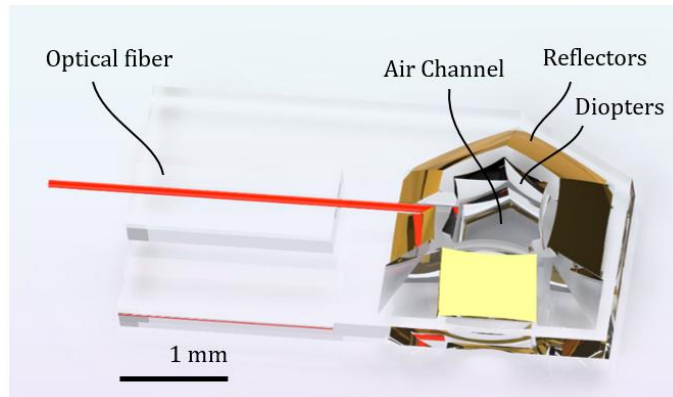


Figure 6: Rendering of the miniature optical system

We also design a V-groove that continues through the back subsystem and stops at the edge of the channel. This V-groove allows an easy alignment of a standard pigtailed optical fiber ( $125 \mu\text{m}$  of diameter). The fiber can illuminate the channel forming a beam with a divergence defined by the numerical aperture (NA) of the fiber. This piece is designed to be manufactured from a single, 1 mm thick, fused silica substrate.

#### 2.5. Angular response at the coincidental Fourier plan

We present a simulation (ray tracing) of the silica glass piece in Figure 7. For a better comprehension, we have simplified the scattering particle down to a simple conical source point. The left figure shows the propagation of rays

casted by five randomly positioned particles. We verify that the resulting image on the Fourier plane is not impacted by the particles positions.

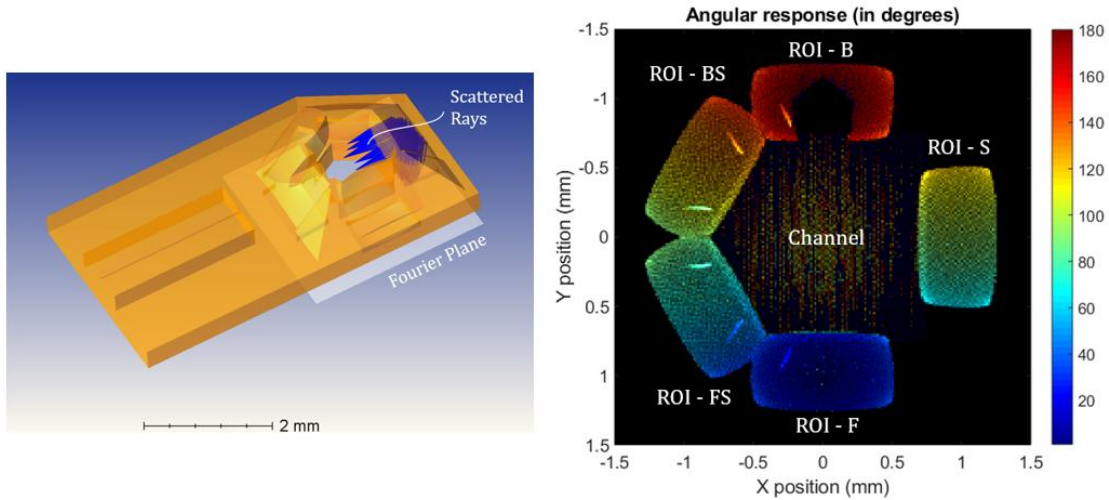


Figure 7: Ray Tracing simulation of the optical system (left). Angular (color) map in the focal plane (right)

The right figure presents the angular response of the optical system. We verify that a point in the focal plane is associated to a scattering angle. We also recognize the five regions of interest (ROI) associated with the five optical subsystems. These ROIs allow us to evaluate the scattering signature thanks to the associated overlapping FoVs.

Note that we observe luminous “claw marks” at blind fields at the edge of two adjacent subsystems. These defects are cross talk effects between the systems meaning that rays can enter through a first dioptric and exit through a last dioptric of the adjacent system.

### 3. FABRICATION PROCESS

#### 3.1. Micromachining on glass

The optical system is manufactured by the company FEMTOprint with an innovative 3D fabrication method for glass [23][24]. The fabrication protocol is composed of three main steps: laser exposure, wet etching and polishing.

The laser exposure is performed on a f200a Head machine starting from a 1 mm thick fused silica glass wafer. The substrate is illuminated with a focused femtosecond laser beam at 1030 nm, properly shaped and focused with a 20x objective (Thorlabs, NA=0.4). The exposure conditions trigger a non-linear absorption process that causes a densification within the laser voxel. As consequence, the etching rate of the material for a KOH solution decrease down to 1000 times compared to the un-exposed material [25]. We generate the object within the substrate by moving the sample and the beam in the fashion of a 3D printer.

Later, we immerse the wafer in a water solution of KOH (45%) at 80°C for 10h. During the etching step, the unexposed volume is released from the wafer. At the end, the device is cleaned with water and dried before the quality control. Since the etching process has a finite selectivity and is quite long, the original design is pre-compensated in order to achieve the desired dimensions after 10h.

The machined surfaces showed a roughness around 80 nm (Ra) on the vertical sidewalls (channel-facing front dioptrics) and 150-300 nm (Ra) on the planar or 3D surfaces (reflecting surfaces and back dioptrics). For this reason, we introduce a proprietary polishing process in order to reduce the roughness of the optical elements below 30 nm by reflowing the surface with limited deformation. An optical image showing a top view of the fabricated glass piece is shown in Figure 8.

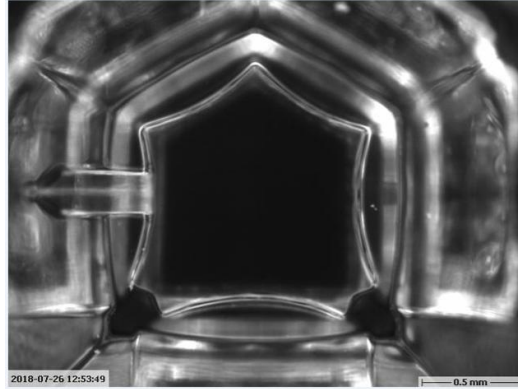


Figure 8: Optical image of the fabricated optical system

### 3.2. Molding and replication

In this section, we explore the process of replicating our printed optical systems to achieve cost effectiveness. We show preliminary tests with a discarded glass prototype (polishing-induced deformation test sample) that we will call ‘mother’ in this section.

We use PDMS (silicone) as the molding material. For complex 3D pieces like this one, the mold is made of two parts: the bottom part is molded and dried first so that the upper part can be molded in turn. A picture of the glass prototype inside its mold is shown in Figure 9 (left).

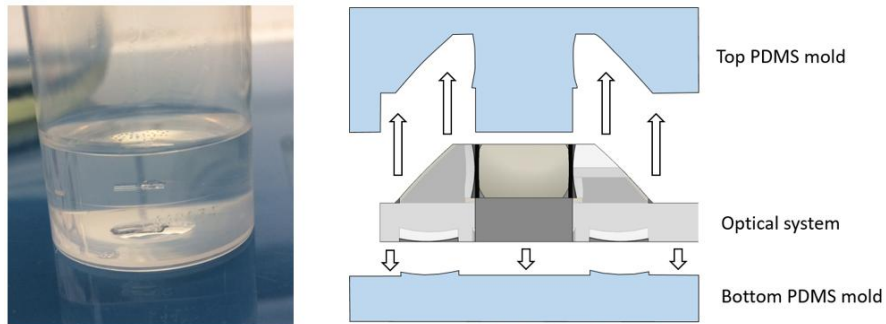


Figure 9: Photography of the mother molded in PDMS (left). Cross sectional view of the unmolding step (right)

Despite the delicate surfaces of the channel inner walls, the unmolding step went smoothly. We observe no degradation of the mother after being molded and unmolded. The low roughness of the original glass piece appears to be well transferred into the mold. Previous in-house studies have shown that this method is well suited for the molding of optical grade surfaces. This PDMS mold is then used to shape a replica (call ‘daughter’ hereafter) with an optical polymer. Here, we use a commercial transparent clear epoxy resin.

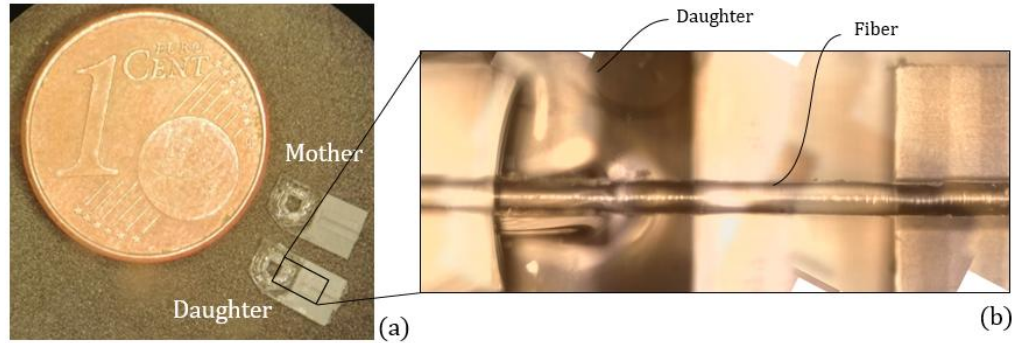


Figure 10: Glass prototype ('mother') next to its epoxy resin replica ('daughter') (a). Optical image of the daughter with a fiber installed (b)

A photography of the resulted replica is shown in Figure 10.a next to the original glass prototype. Apart from the different refractive indices of the materials, the surface quality of the lenses appears identical. The shapes are also reproduced with a great fidelity even inside the channel and with the V-groove that can hold an optical fiber with great precision (as shown in Figure 10.b).

#### 4. CHARACTERIZATION

Preliminary tests were performed with the optical system only (without a holed retina). To do so, we packaged our optical system with an upper and a lower shell (see Figure 11) that were fabricated with a black resin using a high resolution (25  $\mu\text{m}$  voxel) 3D printer (Form 2 printer by Formlabs).

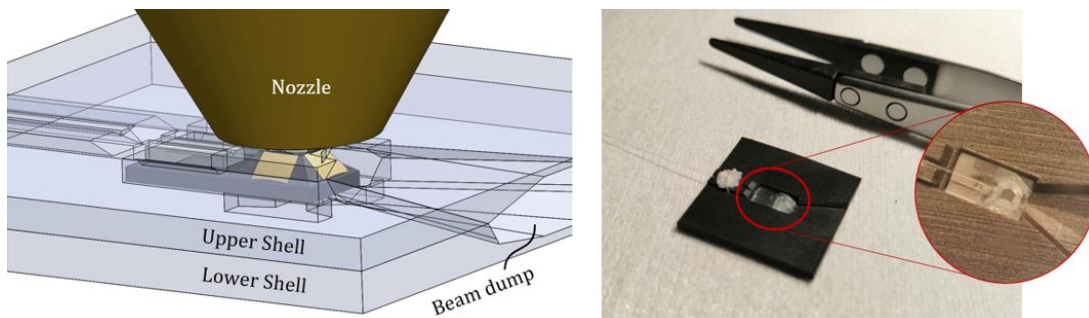


Figure 11: (left) Assembled 3D models of the shells. (right) Photography of the lower shell holding the lenses aligned with a fiber.

The shells contain a housing with precise dimensions for the optical system, an upper 1 mm circular air channel aligned with a metallic nozzle, an opening in front of the back diopeters, an additional V-groove and beam-dump for stray light evacuation. The air stream is injected into the upper part through the nozzle so that the optical path is not obstructed by fluidic parts. In a future set-up, the air-stream will be injected trough a lower holed retina as it prevents particle soiling.

We use a multimode pigtailed fiber (MMF 105/125) with low divergence ( $\text{NA} = 0.1$ ) illuminated by an AlGaInP laser diode operating at a wavelength of 637 nm and with an optical power of 5 mW (HL63102MG by Oclaro). The focal plane is not accessible in this set-up but we can project it using a microscope objective (NPL 10x/0.2 NA objective by Leitz Wetzlar) in reverse orientation and focus it on a bared Global Shutter CMOS monochromatic image sensor (Thorlabs USB2.0 CMOS Global Shutter camera).



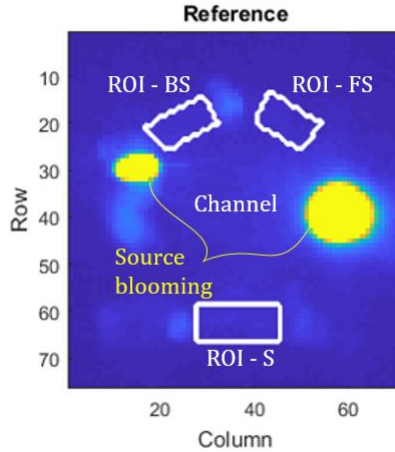


Figure 12: Reference image taken with light on, and no air stream

We take a reference image with light on, and no air stream shown in Figure 12. The sensing area was previously cleaned up with dry air. Every image of scattering signatures will have this reference subtracted.

We observe that the forward region of interest (F-ROI) is completely bloomed by the illumination beam, the backward ROI (B-ROI) is partially bloomed by the scattering at the end of the fiber. These yellow surfaces are blind areas beyond the dynamics of the pixels. However, the BS, S and FS ROIs receive very few stray light. Therefore, we will evaluate only these three ROIs to reconstruct scattering signatures with total FoV as wide as  $90^\circ$ .

An example of a measured scattering signature is shown in Figure 13. It was obtained by spraying particles from an aerosol canister (Smoke Check HIS Canned Smoke by InspectUSA) in the nozzle.

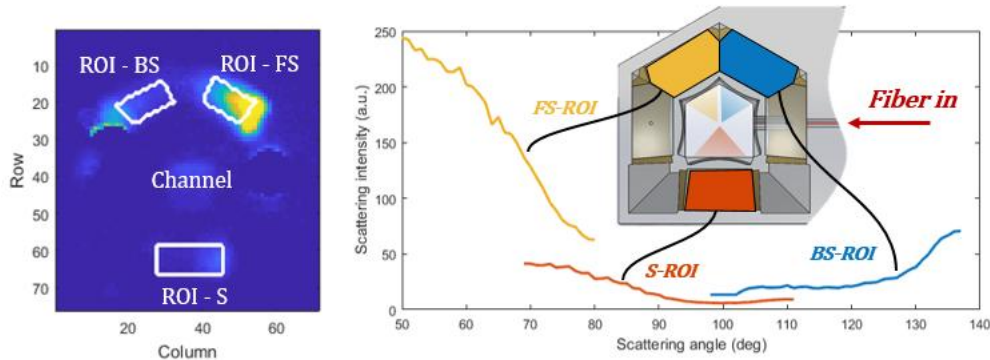


Figure 13: Example of experimental image (left) and reconstructed signature (right)

The left figure is the image obtained (reference subtracted) in the presence of the aerosol. We evaluate pixels within the FS, S and BS ROIs (white contours) and we associate every pixels to an angle following our angle map calculated by ray-tracing (see Figure 7, right). This allows us to draw three curves and reconstruct a scattering signature (right figure). Through numerous tests, the signature was obtained with a very good repeatability. Particles from the aerosol canister were not calibrated in size, for this reason we could not compare this signature to models. In the future, we plan to measure signatures with a calibrated aerosol test bench.

The reconstruction of the signature was extremely simple compared to the planar projection set-up. The procedure should be compatible with low energy portable applications. Note that the curves are not perfectly overlapping: the edges of the individual curves correspond to blind field and should not be overtrusted. This overlapping mismatch will not bother us much as it appears to be very constant and is very certainly linked to the different optical subsystems truncations (i.e. their pupils).

## 5. CONCLUSION & PERSPECTIVES

In conclusion, we have designed a miniature, monolithic refracto-reflective system suited for the optical pre-treatment of scattering signatures. This design is applied to our family of particulate matter sensors with holed retina. It addresses the various areas of improvements identified for particulate matter detection such as particle's position insensitivity, ultra wide field of view, alignment and simplified image processing. We propose a fabrication process for a glass prototype that was developed by the FEMTOprint company as well as a replication process. Preliminary tests have shown good results reconstructing scattering signatures within a FoV of 90 degrees.

Planned tests include a full set-up with the optical system mounted on an existing holed retina. Other tests consist in measuring scattering signatures and limits of detection (LoD) of single calibrated laboratory particles in our aerosol test bench. Finally, we are developing even more advanced designs. Our main aim is to improve on the point spread function (PSF) of a folded optical subsystem. It also features new integrated functions within the glass substrate conceived in the objective of reducing stray light and cross talk effects, i.e. improving on the sensitivity.

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## REFERENCES

- [1] G. B. Hamra *et al.*, "Outdoor Particulate Matter Exposure and Lung Cancer: A Systematic Review and Meta-Analysis," *Environ. Health Perspect.*, Jun. 2014, doi: 10.1289/ehp.1408092.
- [2] J. O. Anderson, J. G. Thundiyil, and A. Stolbach, "Clearing the Air: A Review of the Effects of Particulate Matter Air Pollution on Human Health," *J. Med. Toxicol.*, vol. 8, no. 2, pp. 166–175, Jun. 2012, doi: 10.1007/s13181-011-0203-1.
- [3] A. J. Cohen, J. M. Samet, K. Straif, and International Agency for Research on Cancer, *Air pollution and cancer*. Lyon: International Agency for Research on Cancer, 2013.
- [4] "Integrated Science Assessment for Particulate Matter (External Review Draft, 2018)," U.S. Environmental Protection Agency, Washington, DC, 2018.
- [5] S. A. Cormier, S. Lomnicki, W. Backes, and B. Dellinger, "Origin and Health Impacts of Emissions of Toxic By-Products and Fine Particles from Combustion and Thermal Treatment of Hazardous Wastes and Materials," *Environ. Health Perspect.*, vol. 114, no. 6, pp. 810–817, Jun. 2006, doi: 10.1289/ehp.8629.
- [6] B. C. Singer and W. W. Delp, "Response of consumer and research grade indoor air quality monitors to residential sources of fine particles," *Indoor Air*, vol. 28, no. 4, pp. 624–639, Jul. 2018, doi: 10.1111/ina.12463.
- [7] E. G. Snyder *et al.*, "The Changing Paradigm of Air Pollution Monitoring," *Environ. Sci. Technol.*, vol. 47, no. 20, pp. 11369–11377, Oct. 2013, doi: 10.1021/es4022602.
- [8] Francesca Borghi *et al.*, "Miniaturized Monitors for Assessment of Exposure to Air Pollutants: A Review," *Int. J. Environ. Res. Public Health*, vol. 14, no. 8, p. 909, Aug. 2017, doi: 10.3390/ijerph14080909.
- [9] S. Amaral, J. de Carvalho, M. Costa, and C. Pinheiro, "An Overview of Particulate Matter Measurement Instruments," *Atmosphere*, vol. 6, no. 9, pp. 1327–1345, Sep. 2015, doi: 10.3390/atmos6091327.
- [10] X. Li *et al.*, "Miniaturized particulate matter sensor for portable air quality monitoring devices," in *IEEE SENSORS 2014 Proceedings*, Valencia, Spain, 2014, pp. 2151–2154, doi: 10.1109/ICSENS.2014.6985464.
- [11] M. Dong, E. Iervolino, F. Santagata, G. Zhang, and G. Zhang, "Silicon microfabrication based particulate matter sensor," *Sens. Actuators Phys.*, vol. 247, pp. 115–124, Aug. 2016, doi: 10.1016/j.sna.2016.05.036.
- [12] S. Nicoletti, "Particle detector and method for producing such a detector," US 2013/0120749 A1, 16-May-2013.
- [13] D. Weinert, T. Cleary, G. Mulholland, and P. Beever, "Light Scattering Characteristics And Size Distribution Of Smoke And Nuisance Aerosols," *Fire Saf. Sci.*, vol. 7, pp. 209–220, 2003, doi: 10.3801/IAFSS.FSS.7-209.
- [14] C. F. Bohren and D. R. Huffman, *Absorption and scattering of light by small particles*. Wiley, 1983.
- [15] H. C. van de Hulst, *Light Scattering by Small Particles*. Dover Publications, 1981.

- [16] M. Fournier *et al.*, “A miniaturized optical sensor for particulate matter detection,” presented at the Photonics West, San Francisco, 2020.
- [17] G. Jobert *et al.*, “A Miniaturized Optical Sensor for Fire Smoke Detection,” in *2019 20th International Conference on Solid-State Sensors, Actuators and Microsystems & Eurosensors XXXIII (TRANSDUCERS & EUROSENSORS XXXIII)*, Berlin, Germany, 2019, pp. 1144–1149, doi: 10.1109/TRANSDUCERS.2019.8808611.
- [18] S. Boutami *et al.*, “Visible to mid-infrared integrated sensors for air quality measurement,” in *Optical Sensing, Imaging, and Photon Counting: From X-Rays to THz 2019*, San Diego, United States, 2019, p. 25, doi: 10.1117/12.2529262.
- [19] S. Boutami and S. Nicoletti, “Optical detector of particles,” 2018W0-EP51890, 25-Jan-2017.
- [20] G. Jobert, “Décteur optique de particules,” B03897 FR-DD18825 HB, 16-Jul-2018.
- [21] J. Pribošek and G. Röhrer, “Estimation of the Particle Sizing Error Due to Particle Position in an Integrated PM2.5 Optical Particle Counter,” *Proceedings*, vol. 2, no. 13, p. 850, Dec. 2018, doi: 10.3390/proceedings2130850.
- [22] B. E. A. Saleh and M. C. Teich, *Fundamentals of Photonics*. New York, USA: John Wiley & Sons, Inc., 1991.
- [23] Y. Bellouard, “The Femtoprint Project,” *J. Laser MicroNanoengineering*, vol. 7, no. 1, pp. 1–10, Feb. 2012, doi: 10.2961/jlmn.2012.01.0001.
- [24] D. M. Krol, “Femtosecond laser modification of glass,” *J. Non-Cryst. Solids*, vol. 354, no. 2–9, pp. 416–424, Jan. 2008, doi: 10.1016/j.jnoncrysol.2007.01.098.
- [25] C. A. Ross, D. G. MacLachlan, D. Choudhury, and R. R. Thomson, “Optimisation of ultrafast laser assisted etching in fused silica,” *Opt. Express*, vol. 26, no. 19, p. 24343, Sep. 2018, doi: 10.1364/OE.26.024343.