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Abstract: We investigate the ability of local continuum crystal plasticity theory to simulate intense slip localization observed experimentally in metals exhibiting softening mechanisms. A generic strain softening model is implemented within a massively parallel FFT solver framework to study intragranular strain localization throughout high resolution polycrystalline simulations. It is coupled to a systematic analysis strain localization modes: Equivalent plastic strain and lattice rotation fields are processed to create binary maps of slip and kink bands populations, estimate their volume fraction and mean strain level. High resolution simulations show the formation of an intragranular localization band network. The associated localization maps are used to identify accurately slip and kink bands populations and highlight the distinct evolution of kink bands, influenced by lattice rotation. It is evidenced that selection between slip or kink localization modes is only due to grain to grain incompatibilities with classical crystal plasticity models, as they do not account for their actual physical differences. As a result they predict the formation of a large amount of kink bands, whereas experimental observations of strongly softening metals (such as irradiated metals) seldom report them.

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R. Lebensohn has worked extensively on full-field FFT based method simulations for polycrystal behavior modelling, and worked on kink banding in ice polycrystals.

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Our paper is in direct relation with Pr. McDowell's work on plastic flow localization in irradiated polycrystal modeling.

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Dear editors,

Please find attached our manuscript entitled « Intragranular localization induced by softening crystal plasticity: Analysis of slip and kink bands localization modes from high resolution FFT-simulations results », to be considered for publication in *Acta Materialia*.

This paper investigates the ability of continuum crystal plasticity to simulate intragranular plastic slip localization in polycrystals exhibiting softening mechanisms. The originality of the paper is to analyze simulated localization bands nature (slip or kink bands). To this end, we developed a post-processing method to produce a systematic analysis of slip and kink band networks from full-field simulations. We show that both modes are activated whereas kink bands are not observed experimentally, for instance in irradiated polycrystals. A general discussion on the fundamental reasons of localization modes formation with classical crystal plasticity models concludes this work.

Thank you for your consideration of this manuscript.

Best regards,

A.Marano, L.Gélébart, S. Forest

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Intragranular localization induced by softening crystal plasticity: Analysis of slip and kink bands localization modes from high resolution FFT-simulations results

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Abstract

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We investigate the ability of local continuum crystal plasticity theory to simulate intense slip localization observed experimentally in metals exhibiting softening mechanisms. A generic strain softening model is implemented within a massively parallel FFT solver framework to study intragranular strain localization throughout high resolution polycrystalline simulations. It is coupled to a systematic analysis strain localization modes: Equivalent plastic strain and lattice rotation fields are processed to create binary maps of slip and kink bands populations, estimate their volume fraction and mean strain level. High resolution simulations show the formation of an intragranular localization band network. The associated localization maps are used to identify accurately slip and kink bands populations and highlight the distinct evolution of kink bands, influenced by lattice rotation. It is evidenced that selection between slip or kink localization modes is only due to grain to grain incompatibilities with classical crystal plasticity models, as they do not account for their actual physical differences. As a result they predict the formation of a large amount of kink bands, whereas experimental observations of strongly softening metals (such as irradiated metals) seldom report them.

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Keywords: Crystal plasticity, Intragranular localization, Slip bands, Kink bands, FFT simulations

1. Introduction

A critical issue to address in bridging the gap between microscopic mechanisms and macroscopic mechanical behavior of crystalline materials is the intrinsically heterogeneous nature of plastic slip. Several authors have provided a precise description of these discrete phenomena [1, 2] : deformation occurs by formation of discrete surface steps caused by the emergence of dislocations. When intense dislocation glide occurs on a few crystallographic planes, a sharp slip localization band parallel to dislocations glide planes forms called *slip band*, widely observed in metallic single crystals and polycrystals. Another type of slip localization band observed in deformed crystals, associated with high lattice rotation and orthogonal to the glide direction, is the so-called *kink band*. Kink bands are reported as a late deformation mode of metallic single crystals [1, 3], in strongly anisotropic hexagonal crystals such as ice or Zinc [4, 5, 6, 7, 8], as a crack-tip localization mode [9, 10, 11] or for titanium alloys under high strain rate deformation [12]. Asaro and Rice bifurcation analysis [13] showed that in presence of strain softening the constitutive equations of crystal plasticity can predict both localization modes, and a few authors have studied the formation of kink bands in crystal plasticity simulations [14, 15, 16, 5].

Theoretical and numerical studies have evidenced the role of local softening mechanisms in the apparition of heterogeneous deformation [17, 18]. These mechanisms result of interactions between dislocations and crystal defects and are particularly intense in several metals such as irradiated or hydrogen charged polycrystals. In that case dislocation sources are locked by a hydrogen atom atmosphere making their activation much harder. Therefore required stress to generate further slip from an already active source is thought to be lower than stress needed to activate a new locked source thus promoting intense slip on a limited number of atomic planes [19, 20]. Another example is the extensively studied dislocation channeling mechanism observed in a large variety of irradiated metals such as Copper [21, 22], Zirconium [23, 24], steel [25, 26, 27, 28] or Vanadium [29], but also quench-hardened

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3 aluminum [30] and gold [31] single crystals. Those materials are hardened by a high density
4 of nanometer size defects like dislocation loops or stacking fault tetrahedra. Their inter-
5 action with gliding dislocations leads to their progressive sweeping/annihilation [32] and
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7 thus to a strong local softening promoting further slip in the region where it has already
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9 occurred. Defect-free channels parallel to dislocation glide planes are indeed observed after
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11 deforming those materials, and are strongly correlated to surface slip steps indicating that
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13 defect-annihilation based softening is responsible for the formation of intense slip bands.
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15 A similar mechanism is observed in ω -enriched Ti-Nb-based gum metals where ω -particles
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17 depleted channel are correlated to surface localization bands [33]. Conversely correlation of
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19 clear channels with kink bands has never been observed and more generally kink bands are
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21 not reported as intragranular localization modes in strongly softening crystals.
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25 Numerous efforts have been made aiming at modeling these phenomenon at the poly-
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27 crystal scale as they have a first order influence on the macroscopic mechanical behavior or
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29 on cracking initiation due to localization induced stress concentrations. Relying on molec-
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31 ular dynamics or dislocations dynamics analyses of the dislocation channeling mechanism
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33 [34, 35, 36], many dislocation-based classical crystal plasticity models have been developed
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35 to simulate irradiated metals behavior [37, 38, 39, 40, 41, 42, 43], accounting for the soften-
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37 ing through local defect-density dependent critical shear stress and defect-density evolution
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39 equation modeling their annihilation with increasing glide. This framework successfully
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41 reproduces the main features of macroscopic behavior of irradiated metals.
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43 These strain softening based models have also been used to conduct full-field simulations
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45 of strain localization. Sauzay et al. [25] have explicitly modeled one or two predefined soft
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47 clear channels embedded in a hard matrix in order to study induced stress concentrations.
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49 Zhang et al. [44] have followed a different approach at the polycrystal scale by prescribing
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51 softening only on a predefined network of potential slip bands in 2D polycrystalline FE
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53 simulations. This modeling strategy allows localization bands to form but requires prior
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55 knowledge of geometric characteristics of the bands network. On the contrary, Erinosh
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57 and Dunne [45] have modeled a full 3D polycrystal with a strain softening behavior with
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no assumptions on localization paths. Their simulations predict formation of transgranular localization bands due to slip softening, however they used cubic grains microstructure and associated mesh resolution (average of 1000 elements per grain) is too coarse to reproduce accurately intragranular slip localization. Patra and McDowell [46, 47] have recently published simulations with higher resolution using a dislocation channeling based softening model, and their results predict indeed formation of intragranular localization bands. However they simulated a 2D aggregate under the generalized plane strain hypothesis which is not representative of complex localization patterns that can arise in 3D microstructures. Most importantly, they did not analyze the slip or kink nature of the simulated bands in order to compare results with experimentally observed cleared channels in irradiated steels.

This work aims at gaining deeper insight into the ability of softening classical crystal plasticity to simulate accurately intense intragranular localization observed in the various metals exhibiting softening mechanisms. To this end, we implemented a generic softening crystal plasticity model within a massively parallel FFT solver allowing to model three dimensional polycrystalline unit cells with higher grid resolutions and number of grains. A systematic analysis of simulated localization bands is carried out on simulations results. For that purpose, we developed a methodology using full-field outputs of the FFT simulations to build localization mode maps that allow to identify and quantify simulated slip and kink bands populations.

2. Crystal plasticity constitutive model

The constitutive model used in this study reduces to the two main ingredients allowing to simulate strain localization along crystallographic planes: the classical finite deformation crystal plasticity framework combined with a softening flow rule. This simple and generic formulation allows to avoid any material complexity to focus the study on the link between strain softening crystal plasticity and slip localization. Crystal plasticity kinematics is described by the classical multiplicative decomposition of the deformation gradient tensor \mathbf{F} into its elastic part \mathbf{F}_e and its plastic part \mathbf{F}_p [48] : $\mathbf{F} = \mathbf{F}_e \cdot \mathbf{F}_p$. where \mathbf{F}_p maps the

reference configuration to the isoclinic stress-free local configuration where crystal lattice orientation is unchanged with respect to the reference configuration and \mathbf{F}_e maps the intermediate local configuration into the deformed configuration, describing crystal lattice distortion and rotation. It is assumed that plastic deformation takes place through the slip of dislocations on prescribed slip planes with normal \mathbf{n}^α along slip direction \mathbf{m}^α . The plastic velocity gradient $\mathbf{L}_p = \dot{\mathbf{F}}_p \cdot \mathbf{F}_p^{-1}$ is then determined by the shearing rate of the N_s material slip systems through the relation :

$$\mathbf{L}_p = \sum_s^{N_s} \dot{\gamma}^\alpha \boldsymbol{\mu}^\alpha \quad (1)$$

where γ^α is the plastic slip on slip system α and $\boldsymbol{\mu}^\alpha = \mathbf{m}^\alpha \otimes \mathbf{n}^\alpha$ the Schmid tensor for slip system α . Crystal elasticity is defined by a linear relation between the Green-Lagrange elastic strain tensor $\mathbf{E}_e = \frac{1}{2}(\mathbf{F}_e^T \cdot \mathbf{F}_e - \mathbf{1})$ and Piola elastic stress tensor $\boldsymbol{\Pi}_e = \det(\mathbf{F}_e) \mathbf{F}_e^{-1} \cdot \boldsymbol{\sigma} \cdot \mathbf{F}_e^{-T}$ (defined in the isoclinic configuration) : $\boldsymbol{\Pi}_e = \underline{\underline{\mathbf{A}}} : \mathbf{E}_e$. $\underline{\underline{\mathbf{A}}}$ is the fourth-order elastic tensor, $\boldsymbol{\sigma}$ the Cauchy stress tensor w.r.t. current configuration. Plastic flow is described by a Norton-type visco-plastic flow rule (Eq. 2) and an exponential softening of critical resolved shear stress τ_c^α with increasing cumulated slip on each slip system γ_{cum}^α (Eq. 4).

$$\dot{\gamma}^\alpha = \left\langle \frac{|\tau^\alpha| - \tau_c^\alpha}{K} \right\rangle^n \text{sgn}(\tau^\alpha) \quad (2)$$

$$\tau^\alpha = \mathbf{M} : \boldsymbol{\mu}^\alpha \quad (3)$$

$$\tau_c^\alpha = \tau_{c_i}^\alpha - \Delta\tau^\alpha \left(1 - \exp\left(-\frac{\gamma_{cum}^\alpha}{\gamma_0^\alpha}\right) \right) \quad (4)$$

Resolved shear stress τ^α , is calculated by the projection of the Mandel stress tensor $\mathbf{M} = \det(\mathbf{F}_e) \mathbf{F}_e^T \cdot \boldsymbol{\sigma} \cdot \mathbf{F}_e^{-T}$ on slip system α (Eq. 3). n and K are Norton-law parameters. The model involves three important material coefficients : τ_{c_i} , $\Delta\tau^\alpha$ are respectively the initial critical shear stress and the maximum softening that can be reached on slip system α , and γ_0^α is a parameter adjusting the softening rate.

Despite its simplicity, we believe it to be representative of most softening models for irradiated metals [37, 38, 39, 40, 41, 42, 43, 49]. They are indeed formulated within the same kinematic framework and rely on softening rules that, when written in the case of

single slip, reduce to the form :

$$\tau_c = \tau_0 + A\sqrt{\rho_D} \quad (5)$$

$$\dot{\rho}_D = -B\rho_D|\dot{\gamma}| \quad (6)$$

A and B being material coefficients and ρ_D a defect density. Eq. 5 describes hardening due to local defect density and Eq. 6 defect sweeping by gliding dislocations, inducing softening. When integrated for a constant shear rate these equations yield an exponential decay of the critical resolved shear stress similar to Eq. 4.

3. Slip/kink localization modes analysis

In this section, we present a post processing methodology designed to identify the nature of localization bands in FFT simulations results. In order to identify localization bands, we use the equivalent plastic strain field defined by Eq. 8 as a measure of local slip intensity. Contrary to slip bands, kink bands involve high lattice rotation that can be used to distinguish kinks from slip bands. Lattice rotation angle is computed using the polar decomposition of the elastic part of the deformation gradient : $\mathbf{F}_e = \mathbf{R}_e \cdot \mathbf{U}_e$. Neglecting the small elastic distortion described by the right stretch tensor \mathbf{U}_e , the elastic rotation tensor \mathbf{R}_e is interpreted as the lattice rotation and the corresponding angle θ can be computed with Eq. 7. p is the cumulative plastic strain.

$$\theta = \arccos \left(\frac{1}{2}(\text{tr}(\mathbf{R}^e) - 1) \right) \quad (7)$$

$$p = \int_0^t \sqrt{\mathbf{L}_p : \mathbf{L}_p} dt \quad (8)$$

These fields are then used to define L and R , indicator functions respectively of slip localization and high lattice rotation areas, by the relations:

$$L(\mathbf{X}) = \mathcal{H}(P(\mathbf{X}) - \bar{p}\Phi_D) \quad (9)$$

$$R(\mathbf{X}) = \mathcal{H}(\theta(\mathbf{X}) - \bar{\theta}\Phi_R) \quad (10)$$

where \mathcal{H} is the Heaviside step function and \mathbf{X} is the material point coordinate vector. They indicate regions where fields p and θ are above a level defined by their mean value \bar{p} and

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3 $\bar{\theta}$ over the whole unit cell multiplied by suitably chosen relative thresholds, Φ_D and Φ_R
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5 respectively. Therefore L maps plastic strain localization areas that are mainly localization
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7 bands. As mentioned above, kink bands can be distinguished from slip bands because they
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9 involve large lattice rotation which suggests a natural definition of kink bands as areas
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11 exhibiting both intense plastic slip and high lattice rotation, that is to say $L(\mathbf{X}) = 1$ and
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13 $R(\mathbf{X}) = 1$. We then assume that localization area without intense lattice rotation are slip
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15 bands. Hence, kink and slip bands indicator functions, S and K , are given by :

$$16 \quad K(\mathbf{X}) = L(\mathbf{X}) \cdot R(\mathbf{X}) \quad (11)$$

$$17 \quad S(\mathbf{X}) = L(\mathbf{X}) - K(\mathbf{X}) \quad (12)$$

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20 and can be plotted simultaneously to evidence localization modes. Finally, these functions
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22 are used to determine for the slip and kink bands population, volume fractions, f_S and f_K ,
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24 and mean value of equivalent plastic strain, $\langle P_S \rangle$ and $\langle P_K \rangle$, as follows :

$$25 \quad \langle P_K \rangle = \frac{1}{f_K V} \int_{\Omega} K(\mathbf{X}) P(\mathbf{X}) d\mathbf{X} \quad (13)$$

$$26 \quad \langle P_S \rangle = \frac{1}{f_S V} \int_{\Omega} S(\mathbf{X}) P(\mathbf{X}) d\mathbf{X} \quad (14)$$

27 28 29 30 31 32 33 34 35 36 85 **4. FFT Simulations**

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39 Simulations are performed using the FFT solver [AMITEX_FFTP](http://www.maisondelasimulation.fr/projects/amitex/html/)¹ which offers two main
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41 advantages. First, its massively parallel implementation enables to simulate strain localiza-
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43 tion in three dimensional and high resolution polycrystalline unit cells in order to overcome
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45 limitations observed in the literature. Previous simulations aiming at modeling softening
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47 induced strain localization where indeed conducted either on 3D microstructures but with
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49 low resolutions [45] or with high resolution but 2D microstructures [47]. Second, FFT based
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51 methods provide mechanical fields in the form of 3D images very well suited for the com-
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53 putation of localization modes indicator functions and associated quantities defined in the
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55 former section.

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57 ¹<http://www.maisondelasimulation.fr/projects/amitex/html/>

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4 95 *4.1. Numerical implementation*

5 The FFT solver AMITEX is based on the original fixed-point numerical scheme proposed
6 by Moulinec and Suquet [50] but implements a modified discrete Green operator based on
7 a finite difference method to evaluate derivatives in Fourier space, equivalent to the one
8 proposed by Willot [51]. This numerical scheme is shown to be equivalent to the use of hex-
9 ahedral finite elements with reduced integration [52]. In addition, Anderson’s convergence
10 acceleration technique is applied to the fixed point algorithm [53, 54, 55].

11 Material constitutive law is integrated using a fully implicit θ -method implementation
12 of constitutive equations generated by the MFronT code generator [56]. Internal variables
13 increments $\{\Delta \mathbf{E}_e, \Delta \gamma^\alpha\}$ between time t and $t + \Delta t$ are computed from their value at time t
14 $\{\Delta \mathbf{E}_e^t, \gamma^{\alpha,t}\}$ by solving with Newton-Raphson algorithm the following system of non linear
15 equations :

$$\Delta \mathbf{E}_e + \mathbf{E}_e^t - \frac{1}{2}(\mathbf{F}_e^{T,t} \cdot \mathbf{F}_e^t - \mathbf{1}) = 0 \quad (15)$$

$$\Delta \gamma^\alpha - \left\langle \frac{|\tau^\alpha| - \tau_c^\alpha}{K} \right\rangle^n \text{sgn}(\tau^\alpha) \Delta t = 0 \quad (16)$$

16 Note that here Green-Lagrange elastic strain \mathbf{E}_e tensor is considered as an additional variable
17 to avoid inaccuracies in numerical evaluation of \mathbf{F}_e , following the approach presented in Ling
18 et al. [57].

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40 FFT simulations apply periodic boundary conditions to 3D regular grids of voxels (i.e. 3D
41 images). Two types of polycrystalline microstructures have been generated using voxelized
42 periodic Voronoi tessellations :

- 43 • 2D periodic unit cells (1 voxel thick in the X direction) containing 225 grains (15^2).

44 Because of X direction periodicity, this is equivalent to 3D infinite columnar grains
45 in the X direction, also equivalent to a 2D modeling under generalized plane strain
46 hypothesis. Three in plane slip systems with a 60 degree misorientation relative angle
47 are modeled (Fig. 1), and each grain is assign a random "2D orientation" is assigned
48 to each grain, leaving all slip plane normals and glide directions in the (Y, Z) plane.
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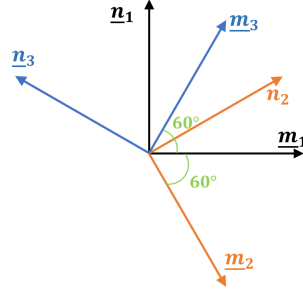


Figure 1: Three inplane coplanar slip systems used for 2D simulations

- 3D periodic unit cells consisting of 64 grains (4^3) with random grain orientations. In order to assess results variability, 9 realizations of these random microstructures have been employed, as well as a 512 grains (8^3) random aggregate. Simulations have been carried out using the 12 FCC slip systems $\{111\} \langle 110 \rangle$, the 12 BCC slip systems $\{110\} \langle 111 \rangle$ or the 3 basal HCP slip systems $\{0001\} \langle \bar{1}210 \rangle$.

Unless otherwise stated grid resolution has been chosen so that mean grain size is resolved by 50 elements. Thus, 2D and 3D simulations contain in average respectively 2500 and 125000 voxels per grain.

In addition to periodic boundary conditions, tensile loading is applied in the Z direction by prescribing the mean value of the corresponding component of the displacement gradient $\mathbf{H} = \mathbf{F} - \mathbf{1}$ at a constant strain rate of $10^{-5} s^{-1}$. Mean values of all other components of engineering stress (first Piola-Kirchhoff stress) are prescribed to zero.

Constitutive model parameters used in all simulations unless otherwise stated are listed in Tab. 1. All simulations feature isotropic linear elasticity. Norton law coefficients n and K values are chosen in order to limit rate dependence without damaging numerical convergence. As simulated crystal systems have only one family of equivalent slip systems, superscript α on flow rule parameter is omitted in the rest of this paper. The single slip system softening behavior and simulated macroscopic mechanical behavior for 2D, 3D FCC and 3D BCC polycrystals are plotted on Fig. 2 for this set of material parameters which involves 20% maximum softening of the critical resolved shear stress on each slip system.

K	n	E	ν	τ_{C_i}	τ_{C_f}	γ_0
$10 \text{ MPa} \cdot \text{s}^{\frac{1}{n}}$	15	100000 MPa	0.3	100 MPa	80 MPa	0.1

Table 1: Material parameters used for all simulations

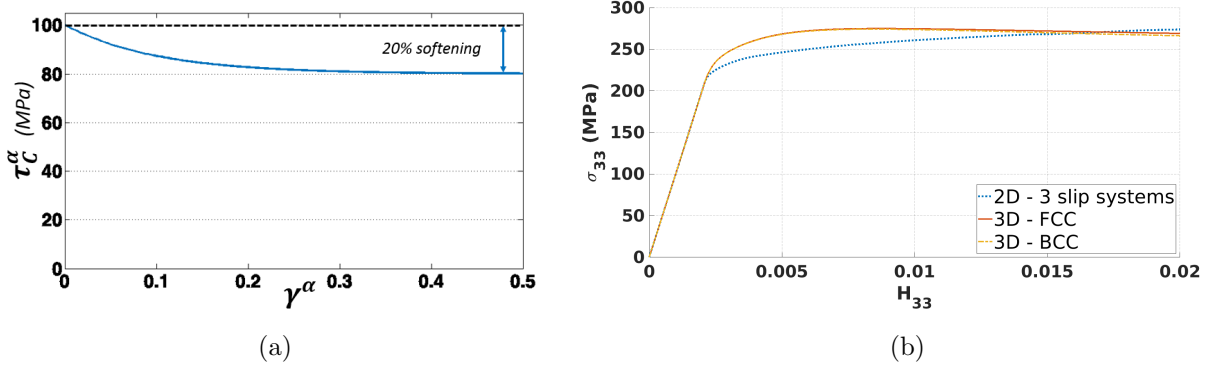


Figure 2: Critical resolved shear stress evolution curve used for all simulations (a), and associated macroscopic stress-strain responses for different polycrystalline simulations (b) (FCC and BCC curves are almost superimposed)

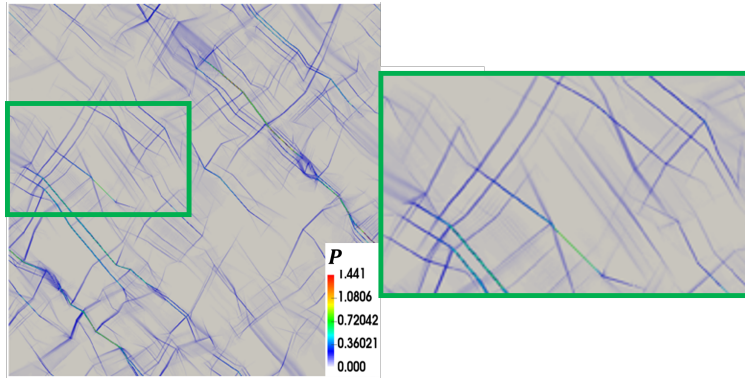
5. Results

5.1. Identification of slip and kink bands

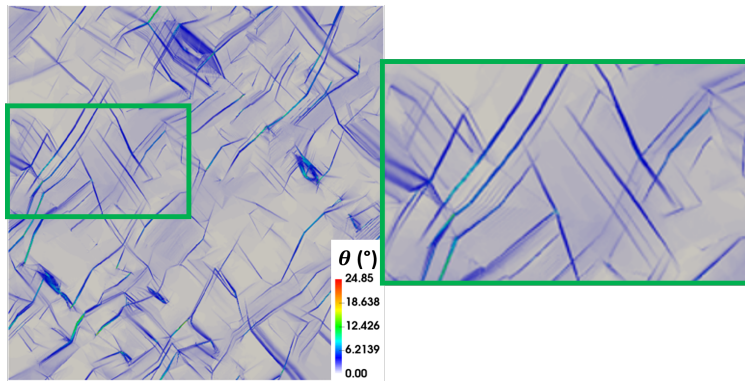
Fig. 3 (a-b) shows equivalent plastic strain and lattice rotation fields simulated for the 2D microstructure after 1% overall elongation. Clear networks of intragranular slip localization bands have formed as well as intense lattice rotation bands. Indicator functions S and K of slip/kink bands are computed from these fields as defined in sec. 3. They are plotted respectively in red/blue and superposed to the microstructure in order to construct the associated localization mode map (c). In addition, slip planes traces are superposed to compare the detected slip and kink band orientations to crystallographic directions. The zoomed view (d) clearly demonstrates that all red/blue bands are respectively parallel/perpendicular to a slip plane. Fig. 4 shows similar results for a 3D simulation of a FCC polycrystal, as well as the video provided as supplementary material.

A systematic study of simulated bands confirms that this correspondence holds for most detected bands. The proposed methodology provides then an efficient tool to identify plastic

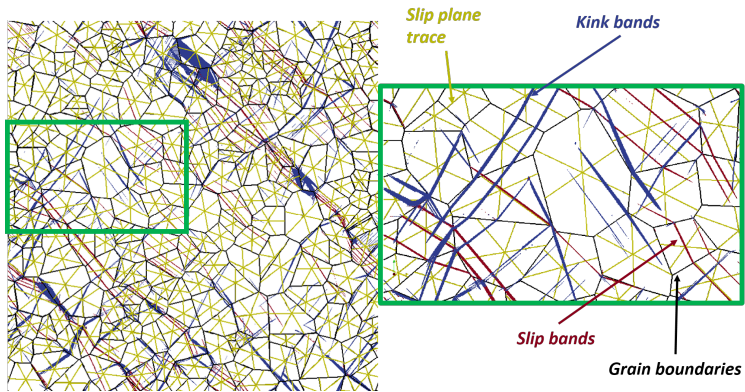
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(a)



(b)



(c)

(d)

Figure 3: Equivalent plastic strain (a) and lattice rotation angle (b) fields for the 2D polycrystal (3 in-plane slip systems) after 1% overall strain. Associated localization map (c). Slip (red) and kink (blue) bands are always respectively parallel/orthogonal to a slip plane (yellow) as illustrated by the zoom at the green-surrounded region (d). Grain boundaries are represented by black lines. Grid resolution: 750x750 voxels

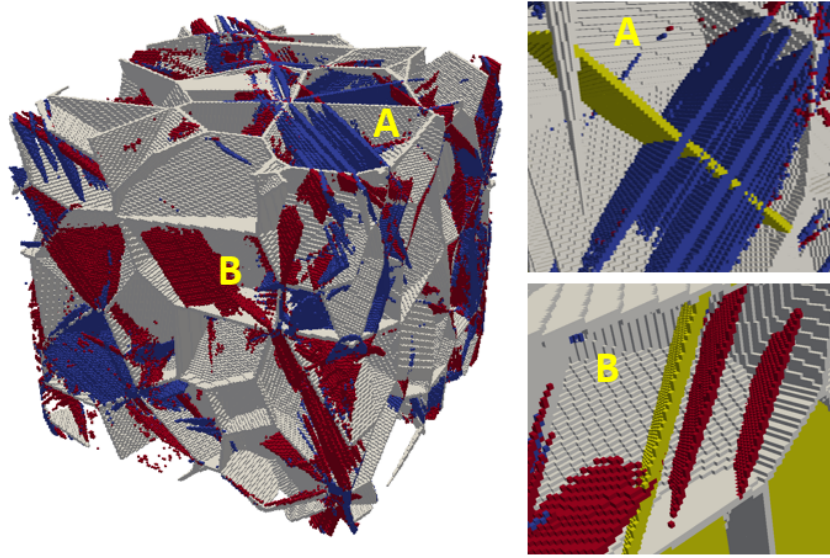


Figure 4: Localization map built for a FCC 3D polycrystal after 2% overall strain showing slip/kink bands (red/blue) and grain boundaries (grey). Activated slip plane (yellow) is plotted on the zooms on A and B marked grains. The A grain contains a series of kink bands orthogonal to the activated slip plane. The B grain contains 2 slip bands parallel to the activated slip plane. Grid resolution: 200x200x200 voxels

localization modes that could be applied to any finite strain crystal plasticity based simulation. It is especially helpful to analyze 3D simulations (see. Fig. 4) which lead to complex 3D images of dense planar bands network, making direct observation of bands orientation cumbersome.

Thresholds detection values have been tuned by hand to obtain optimal maps. Too low values of Φ_D leads to detection of more homogeneously deformed area whereas too high values leads to the detection of only a few localization bands. Best compromise has been achieved for $\Phi_D = 3$. Φ_R is then chosen to obtain best optimal band separation. Too high values lead to identification of kinks exhibiting too low lattice rotation as slips. Besides, regions with a slight inhomogeneous deformation can also have a moderate local lattice rotation and a slip band crossing them would be identified as a kink for too low values of Φ_R . Optimal results have been obtained for $\Phi_R = 2$. Thresholds values do not have a strong impact on qualitative analysis of localization maps. However they have a stronger influence on bands volume fraction and mean plastic strain estimation. Yet using the same

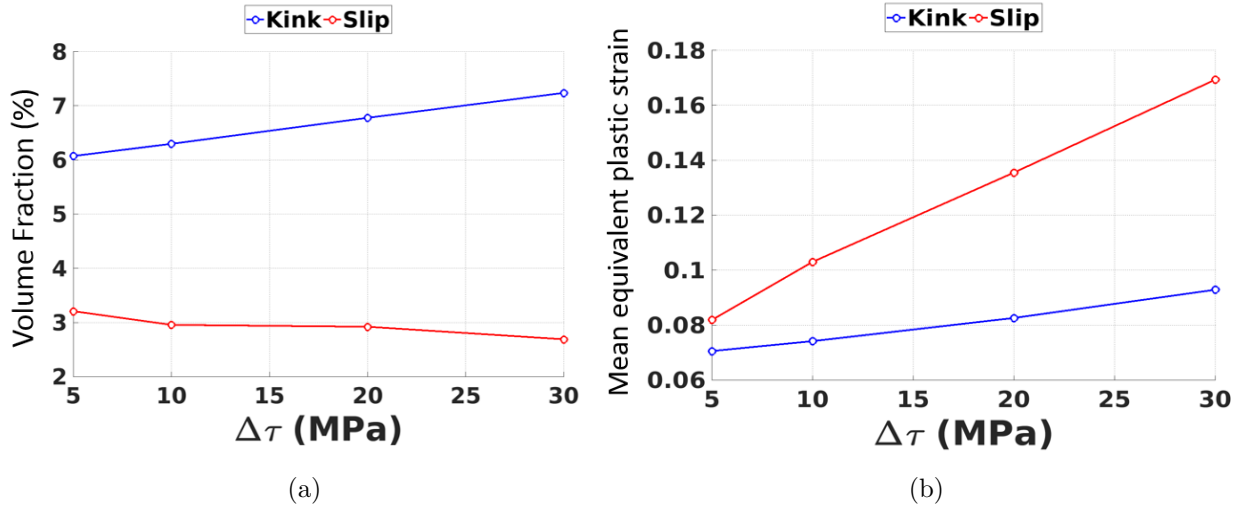


Figure 5: Evolution of slip/kink bands volume fraction (a) and mean equivalent plastic strain (b) with softening intensity for the 2D polycrystal (3 in-plane slip systems) after 1% overall strain (slip/kink bands represented in red/blue respectively). Grid resolution: 750x750 voxels.

set of threshold values to analyze different simulations allows for relative comparison of these quantities that provides qualitative insights on strain localization properties, as presented in the following sections.

5.2. Grid resolution influence on slip and kink bands

Fig. 6 shows the evolution of slip and kink band volume fractions and mean plastic strain after 1% total elongation for 2D simulations conducted with increasing grid resolution. When increasing grid resolution, slip bands volume fraction decreases and their mean strain level increases. Softening material behavior is known to induce numerical instabilities leading to such mesh dependence. On the contrary, results show that kink bands properties are much less sensitive to grid resolution and seem to converge. Associated localization maps illustrate this trend: When increasing grid resolution the slip bands thickness decreases while their number increases. In contrast kink bands patterns are very similar in the three maps.

Due to lattice rotation, the Schmid factor in kink bands can be locally decreased (or the reverse) and hinder further slip. Hence, lattice rotation hardening restrain slip localization. This rotation induced hardening mechanism opposes to material softening and can explain

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3 why kink bands population exhibit a low mesh size dependence despite the strongly softening
4 material behavior.
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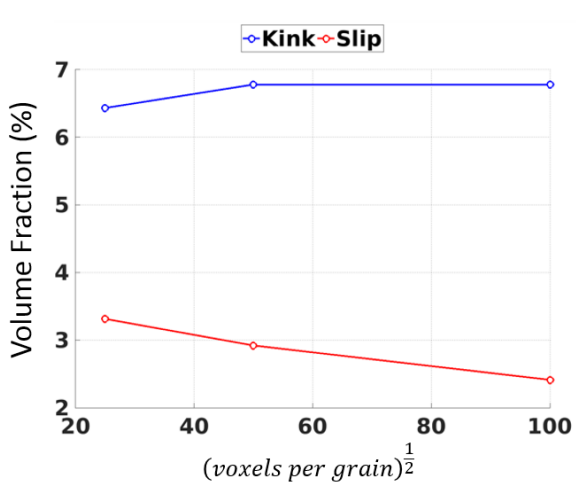
7 8 180 *5.3. Softening influence on slip and kink bands* 9

10 [Fig. 5](#) presents evolution of slip/kink volume fractions and mean plastic strain after 1%
11 total elongation when varying the maximum softening level $\Delta\tau$ for 2D simulations. Again,
12 slip and kink band population evolutions present significant differences. Increasing $\Delta\tau$ causes
13 slip bands volume fraction to slightly decreases whereas kink bands volume fraction increases.
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18 185 The mean plastic strain level increases with softening intensity for both populations but
19 increase is steeper for slip bands.
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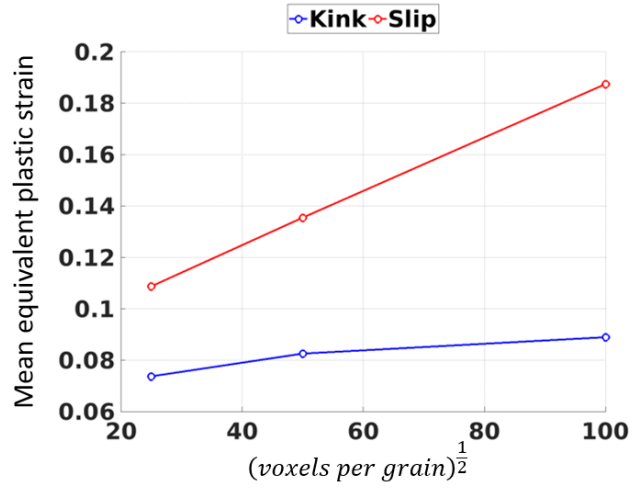
22 Softening will also promote increased plastic slip in kink bands but because of rotation
23 induced hardening, slip localization will be hindered and additional plastic slip will occur
24 by widening of existing kink bands or formation of new ones. This mechanism explains the
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28 190 smaller increase in kink bands mean plastic strain level as well as their increased volume
29 fraction for a higher $\Delta\tau$.
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32 33 *5.4. Comparison between 2D and 3D simulations* 34

35 [Fig. 7](#) and [Fig. 8](#) show the evolution of slip/kink band volume fractions and mean plastic
36 strain level with increasing loading for a 2D simulation and a 3D simulation of a FCC
37 polycrystal. Results highlight a clearly distinct evolution of slip and kink band populations
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39 195 for the 2D simulations. Both modes are present in comparable amounts in the first stages
40 of deformation but then volume fraction grows more quickly for kinks than slip bands.
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49 200 and existing band widening whereas only the first phenomenon is observed for slip bands.
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(a)



(b)

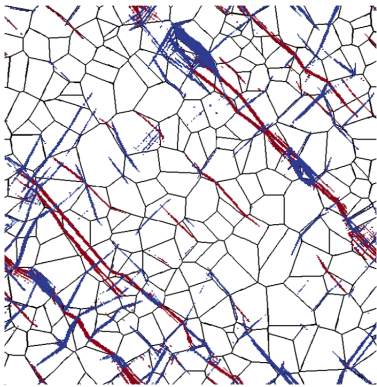
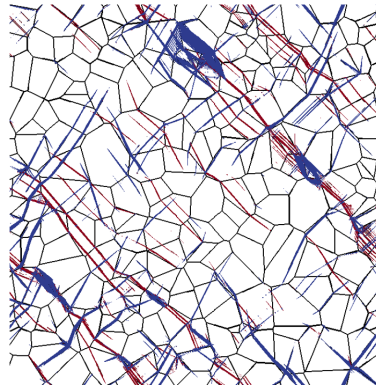
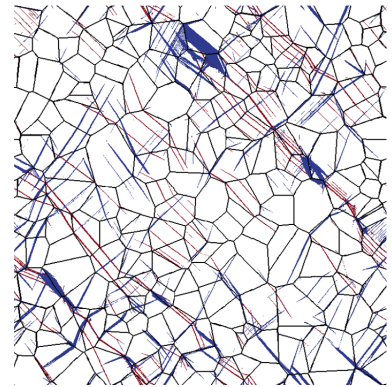
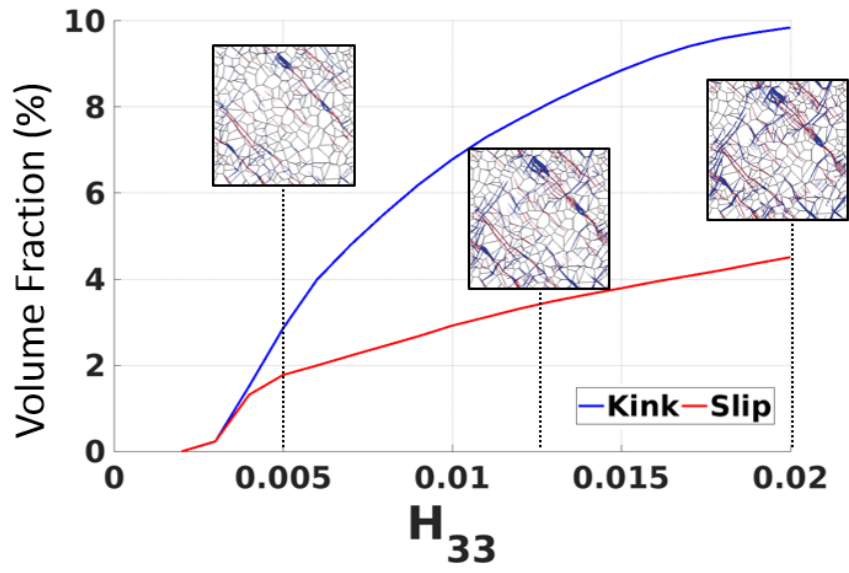
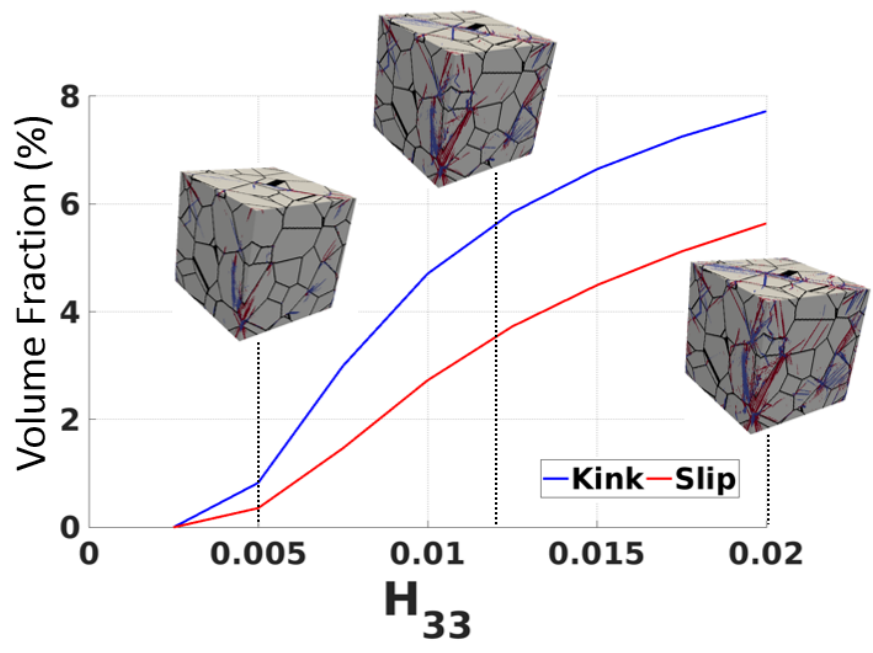
(c) 25^2 voxels per grain(d) 50^2 voxels per grain(e) 100^2 voxels per grain

Figure 6: Influence of grid resolution on slip (red) and kink (blue) bands volume fraction (a) and mean equivalent plastic strain (b) for the 3 in-plane slip systems 2D polycrystal after 1% overall strain. (c - e): associated localization maps.



(a)



(b)

Figure 7: Evolution of slip/kink band volume fraction for the 2D simulation with 3 in-plane slip system (a) and a FCC 3D polycrystal (b), with snapshots of associated localization maps.

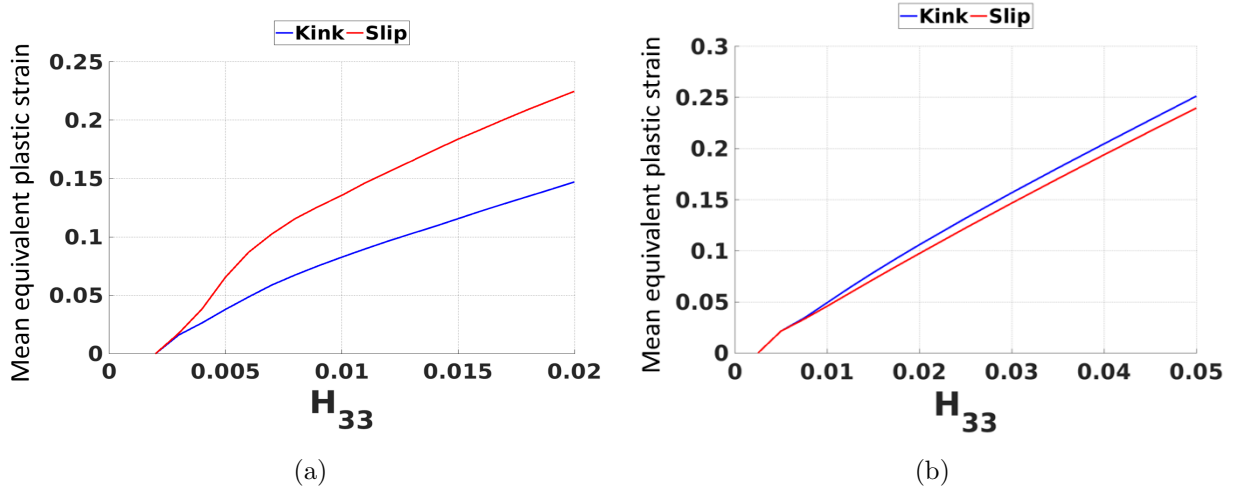


Figure 8: Evolution of slip/kink band mean equivalent plastic strain for the 2D (3 in-plane slip systems) (a) and a FCC 3D 64 grain polycrystal (b)

For geometrical reasons, the same amount of lattice rotation induces lower variation of Schmid factor in three dimensional simulations compared to the 2D simulations where all directions involved in Schmid factor calculations (glide direction, slip plane normal and loading directions) are coplanar. Hence, lattice rotation induced hardening should have a minor impact in 3D simulations than in 2D simulations, which is consistent with actual results.

5.5. Sensitivity to simulated Volume Element

To our knowledge, kink bands have never been reported for strongly softening metals. However, the results presented in previous sections reveal large proportions of kinks in simulated localization band networks. In order to find out if these proportions are due to the specific microstructure of the used unit cell, 9 random realizations of a 64 grain and one 512 grain 3D polycrystals have been generated to characterize the variability of simulated localization bands populations with volume element instances, and volume element size. Fig. 9 presents the evolution of slip/kink bands volume fraction with increasing loading. It is found that for the 64 grains volume element the standard deviation of simulated band volume fractions is generally smaller than the difference between slip and kink bands volume

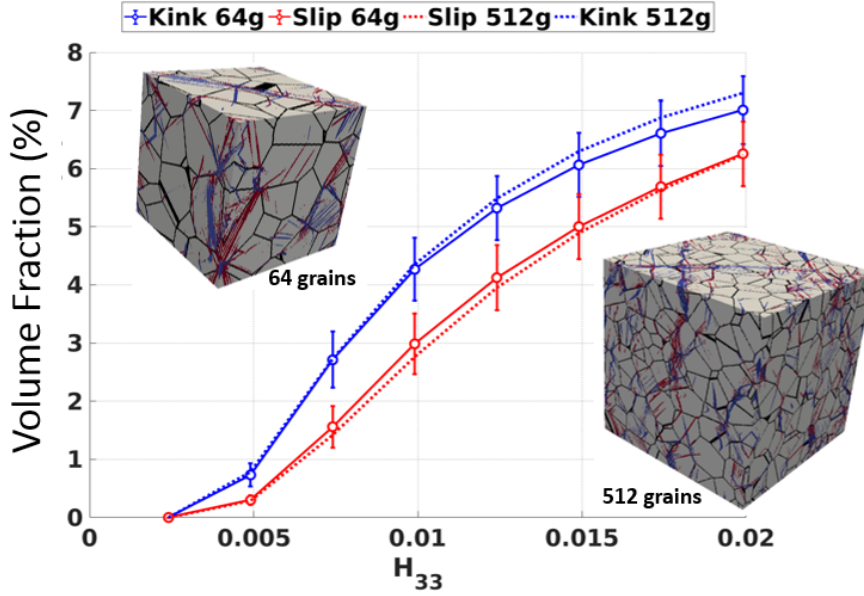


Figure 9: Slip/kink bands volume fraction evolution with loading in FCC polycrystal. Plotted value is the mean of 9 realizations of a 64 grains random Voronoi aggregate, error bars indicating standard deviation of the 9 simulations. Results for the 512 grains random Voronoi aggregate are plotted in dashed-lines. Associated localization maps show localization at 2% overall strain in one 64 grains polycrystal and in the 512 grains one.

fractions. Results of the 512 grain aggregate simulation are contained within the error bars, very close to the mean value of the 9x64 grains simulations. Besides, similar localization networks are observed on 64 and 512 grains simulations localization maps. It follows that a single 64 grains volume element may be sufficient to draw a qualitative analysis of slip/kink bands populations for these cubic crystals.

6. Discussion : localization bands formation in crystal plasticity simulations

Asaro and Rice [13] have shown that both slip and kink bands arise as the two possible bifurcation modes for elasto-plastic single crystals undergoing single slip at large strains. They defined this two modes as slip localization planes respectively orthogonal to glide plane normal direction \mathbf{n} (slip bands) and glide direction \mathbf{m} (kink bands). In the case of strain-softening crystals, their analysis shows that both modes become simultaneously

possible at incipient plasticity. Incipient plasticity always occurs at small strain in metallic materials and in these conditions small strain formulation of crystal plasticity equations are valid to describe material behavior. In the small strain framework, resolved shear stress τ^α on slip system α and plastic strain are computed as follow :

$$\tau^\alpha = \mathbf{m} \cdot \boldsymbol{\sigma} \cdot \mathbf{n} \quad (17)$$

$$\dot{\epsilon}_p = \sum \alpha \dot{\gamma}^\alpha \mathbf{m} \otimes_{sym} \mathbf{n} \quad (18)$$

The Cauchy stress $\boldsymbol{\sigma}$ being a symmetric tensor and \otimes_{sym} the symmetric tensor product, \mathbf{m} and \mathbf{n} play a perfectly symmetric role in Eq. 17: Inverting them leaves the equation unchanged. This consideration implies that kink and slip bifurcation modes are strictly equivalent at incipient plasticity with respect to the constitutive equations. It follows that structural effects, i.e. grain to grain plastic strain incompatibilities will govern the selection of slip or kink localization modes.

In order to provide an illustration of this property, two simulations have been carried out using the same grain geometry, grain orientations and material coefficients, but using two distinct crystal slip systems : the 12 FCC $\{111\} \langle 110 \rangle$ slip systems and the 12 BCC $\{110\} \langle 111 \rangle$ slip systems. The latter are indeed obtained by switching slip planes normals and glide directions of the FCC slip systems, thus according to Asaro and Rice analysis the potential localizations planes are the same in both polycrystals. The two identical microstructures induce identical structural effects and thus should activate the same localization planes at incipient plasticity. Simulations results clearly illustrate this point: In corresponding localization maps, shown on Fig. 10, most of FCC slip (resp. kink) bands have a kink (resp. slip) counterpart for the BCC crystal structure. Then, finite strain kinematics leads to distinct evolutions of slip and kink bands because of rotation induced hardening, discussed in previous sections. It explains why the two localization maps are not strictly equivalent after applying 1% overall tensile strain.

With a the view to investigating the influence of structural effects on slip/kink band formation a simulation has been carried out for a HCP crystal considering only the 3 basal slip systems $\{0001\} \langle \bar{1}210 \rangle$. In that case the distribution of available localization planes

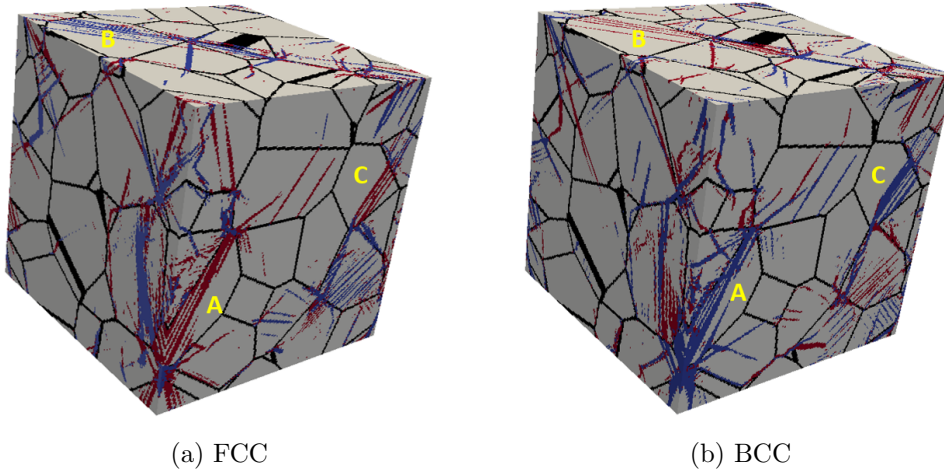


Figure 10: Localization maps of 3D polycrystals after loading to 1% strain with (a) : 12 FCC slip systems $\{111\}[110]$ and (b) 12 BCC slip systems $\{110\}[111]$, with identical geometry and grains orientations. Grains marked A,B and C illustrate the almost identical band structure, with FCC slip banding (resp. kink) corresponding to BCC kink banding (resp. slip).

is then strongly anisotropic and should be more influenced by structural effects than in more isotropic cases such as cubic crystals. Indeed, the only potential plane for slip band formation in each grain is the basal plane, whereas kink banding, in prismatic planes offer 3 times more planes to accommodate grain to grain plastic incompatibilities. Fig. 11-a shows that kink bands volume fraction is approximately two times higher than slip band volume fraction, whereas the two quantities are much closer for the FCC crystals (Fig. 9). Associated localization map (Fig. 11-b) shows that localization occurs mainly at grain boundary triple lines from which kink bands seem to emerge more often than slip bands.

Triple lines grain boundary induce strong stress concentrations due to grain to grain incompatibilities. They are highly likely to trigger strain localization in some or all of the neighboring grains. Thus this structural effect will promote localization paths that extend over at least 2 grains and cross grain boundaries close to triple lines. Considering that geometrically there are three distinct kink planes against only one slip plane, the probability to form such transgranular localization paths across kink bands is higher. This could explain why the gap between slip and kink bands volume fractions is higher in the

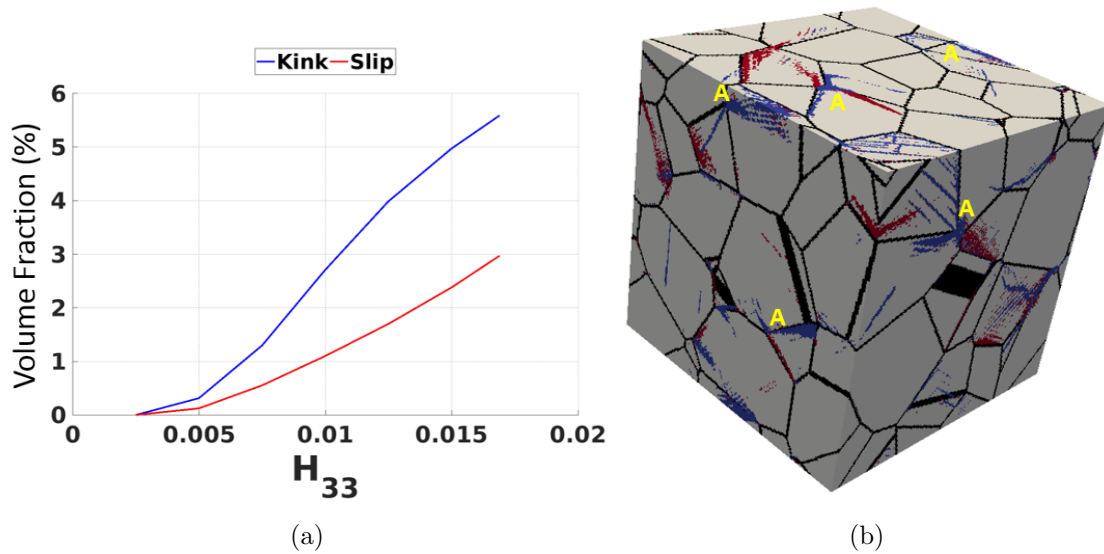


Figure 11: Slip/kink bands volume fraction evolution for a 64 grains random HCP polycrystal (a). Zones marked A in the associated localization map after 1% overall strain (b) show that localization occurs generally at triple grain boundary junctions mostly through kink banding.

case of the simulated HCP crystal.

Lebensohn et al. [15] carried out crystal plasticity simulations of ice HCP polycrystals deforming mainly through basal slip. As in our HCP simulation, they note significant occurrence of kink bands in their results which is in agreement with reported observations of kink bands in ice [4, 5]. Flouriot et al. [58] have also noted kink bands formation in crack-tip field simulations in a FCC crystal that are similar to those observed with crack-tip field measurements in ductile crystals [10]. As in this two situations, kink bands observations are mostly reported where strong strain incompatibilities arise such as crack-tip fields, compression of HCP single crystals [7] or deformation of strongly anisotropic HCP polycrystals [8, 4, 5] mainly deforming through basal slip. In those cases, crystal plasticity models appears to be well-suited to simulate their formation.

However, the case of irradiated Zirconium polycrystals provides a good example to also highlight their limitations. They are HCP crystals deforming mainly through basal slip and could exhibit formation of kink bands, like ice polycrystals, because of this slip anisotropy. On the contrary, deformed Zr polycrystal observations reveal only very intense slip bands,

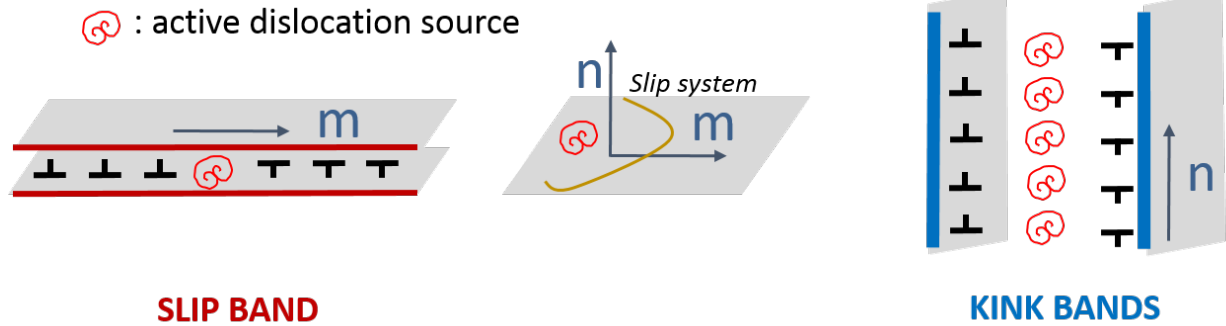


Figure 12: Schematics of active dislocation source distributions required to form a slip or a kink band.

associated to dislocation channeling, a strongly softening mechanism, while kink bands have never been reported yet [23, 24]. Thus, kink band formation in polycrystals could be the result of a competition between structural effects and microscopic mechanisms that cannot be accounted for within the classical crystal plasticity framework.

Indeed, slip and kink localization modes are strictly equivalent in these models from the constitutive perspective. Yet considering associated dislocation mechanisms, both modes are very different. Indeed, slip bands formation involves only a few very active dislocation sources located in close slip planes whereas kink band formation involves the activation of a considerably larger number of sources aligned along the direction normal to the slip plane as represented on Fig. 12. Hence, the two modes are not equivalent regarding dislocation mechanisms. Hence for materials exhibiting strong softening mechanisms intensification of dislocation emission from already active sources is promoted over activation of new sources and thus kink bands formation should be highly unlikely. Kink bands are indeed never reported in observations of deformed irradiated or quench-hardened metals, that undergo such softening mechanisms (dislocation channeling), where slip localization seems to occur only through intense slip bands. Consequently classical crystal plasticity models appear to be fundamentally unable to reproduce accurately localization bands formation in these materials.

7. Conclusions

We have used a massively parallel FFT solver to study intragranular strain localization induced by a strain softening classical crystal plasticity model. This numerical tool allows to compute realistic three dimensional polycrystalline simulations including full description of complex crystal systems and achieve grid resolutions that allow for a fine description of intragranular localization bands. Our simulations show the formation of an intragranular localization network of narrow bands exhibiting high plastic slip.

We proposed a new method to study the nature of simulated localization bands based on the analysis of equivalent plastic strain and lattice rotation fields. We produced localization maps that were used to accurately identify the slip and kink band populations in the localization network, for both simple bidimensional simulations and realistic three dimensional polycrystals with complex crystal systems. Quantification of band volume fraction and mean plastic strain highlight the distinct evolution of slip and kink bands. Because of rotation induced hardening, kink bands tend to widen with increasing loading, and their volume fraction and mean strain level are less sensitive to mesh dependence and softening magnitude. We conclude that it is essential to identify the nature of localization modes when simulating intragranular strain localization.

In agreement with Asaro's and Rice's bifurcation analysis, we showed that slip or kink bands localization modes are strictly equivalent for softening classical crystal plasticity models. They only account for strain incompatibility effects on plastic localization mode formation, which translate into a large amount of kink bands in all simulations of softening polycrystals. This feature is in contradiction with experimental observation of localization bands in strongly softening metals which reveals the fundamental physical differences in slip or kink band formation from the dislocation mechanism perspective. Therefore, in order to accurately simulate intragranular strain localization at the continuum scale in softening metals, physical mechanisms that can promote individually kink or slip band formation need to be accounted for with more complex theories such as strain gradient plasticity. For instance, this framework allows to account in the constitutive equations for an energy density

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4 325 associated to the geometrically necessary dislocation (GND) density tensor, which is known
5 to be high in kink bands because of the large lattice curvature that they induce. Such models
6 could be able to reduce kink band formation and will be explored in future works.
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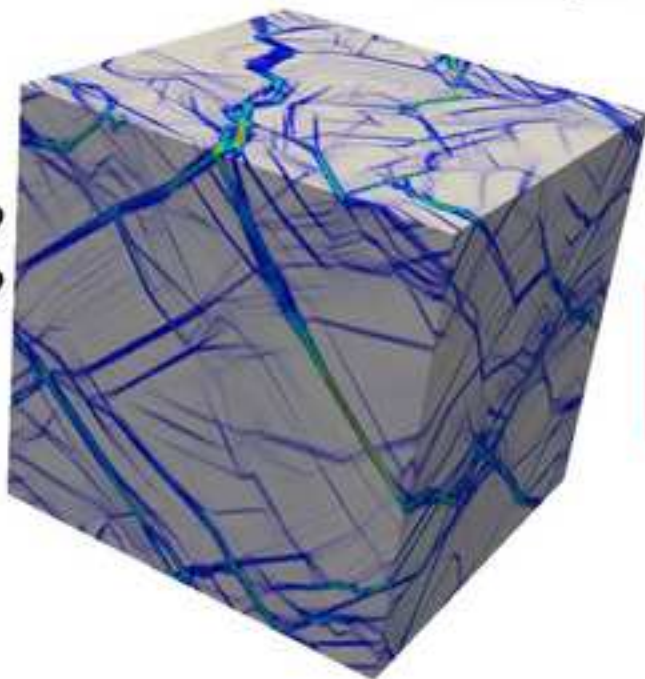
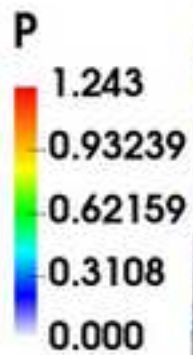
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PLASTIC STRAIN LOCALIZATION :

Slip or Kink
banding ??



**LOCALIZATION
MODES
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