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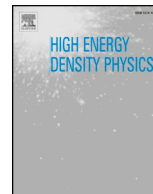
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## Extreme-UV absorption processes in a laser-produced mid-Z plasma: Measurements and theoretical interpretation

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## ABSTRACT

A good knowledge of absorption properties of plasmas at temperature of few tens of eV is essential in several domains such as astrophysics and inertial fusion science. For instance the description of stellar envelopes or the analysis of beta-Cephei pulsation requires an accurate determination of the Rosseland absorption coefficient, which strongly depends on the radiative properties of plasmas in the extreme-UV (XUV) range. Contrary to measurements in X-ray range, the literature on the absorption properties of plasmas of mid-Z elements in XUV domain is less abundant. Furthermore the theoretical interpretation of such spectra represents a theoretical challenge since this energy range involves transition arrays from  $n$  equal 3 to 3 with an approximately half-open 3d subshell and possibly other open spectator subshells which contain a huge number of lines. The aim of this paper is to describe an experiment recently performed on the LULI 2000 laser facility mostly devoted to measurements of the absorption in the 60 – 180 eV spectral region in a copper plasma at a temperature of 10 to 30 eV and a density of few mg/cm<sup>3</sup>. The experimental scheme is based on an indirect heating of multilayer thin foils by two gold cavities irradiated by two nanosecond doubled-frequency beams with an energy of several hundreds of J. This scheme allows one to obtain moderate temperature- and density-gradients and ensures conditions close to local thermodynamic equilibrium. The self-emission of cavities in XUV range is tentatively eliminated by the use of a time-dependent detection. A preliminary interpretation of these measurements is proposed. This analysis relies on three different codes: the hybrid code SCO-RCG, the Flexible Atomic Code in detailed or configuration-average mode, and the HULLAC code in level or configuration mode. A partial agreement is obtained between theory and experiment, though the account for temperature gradients is probably necessary to accurately describe the present measurements.

## 1. Introduction

The accurate determination of absorption properties of plasmas in the extreme UV (XUV) range bears a particular importance in several domains of physics such as astrophysics [1] or inertial confinement physics [2,3]. In laboratory experiments using the indirect scheme, the heating of the target is determined by radiation transfer in XUV range. The plasma emissive properties in XUV region make them good candidates as radiation sources for nanolithography devices [4]. From a theoretical point of view, the modeling of XUV absorption represents a serious challenge since it usually involves the account for transition arrays with a very large number of lines. This modeling may also be very sensitive to phenomena such as configuration interaction which

implies a strong effort.

While a wide literature is available concerning X-ray absorption measurement, the amount of published results in XUV domain is limited. Without claiming to exhaustivity, one may quote the works by Da Silva et al in Fe and NaF [5], Springer et al in Fe [6,7], Winhart et al in Al, Fe, Ho [8], Kontogiannopoulos et al in Al and ZnS [9], Zhang et al in Al [10], Fe [11], or Qing et al in Mo [12]. Such experiments present a particular difficulty because the hohlraums used in the heating scheme and the sample itself are strong emitters in XUV region and one must discriminate between this self-emission and the absorption signal. The opacity properties in XUV region also have effects on emission spectra as analyzed, e.g., by Fujioka et al in Sn [13]. From the above list, it appears that copper radiative properties in XUV region have not been

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widely investigated. Nevertheless, this element is involved as a dopant in beryllium ablaters for inertial confinement fusion [14–16]. Because of its low abundance, copper is not expected to be of major astrophysical interest, however the experimental and theoretical techniques used to analyze its radiative properties also apply to iron and nickel that play a significant role in stellar atmospheres. With such motivations, we report in this paper XUV absorption measurements in copper, performed on the LULI2000 laser facility. In order to get an indirect measurement of plasma temperature (and to a lesser extent density), a simultaneous measurement of X-ray absorption has been performed, using a four-spectrometer arrangement. This campaign is an extension of our previous attempts [17] where XUV measurements were hampered because of the lack of temporal resolution.

The complexity of XUV spectra in medium-Z elements such as copper for a temperature close to 20 eV – a condition frequently met in laser-plasma experiments – may be easily understood from their electronic structure. In such thermodynamic conditions the average ionization of copper is about 6. Since the  $\text{Cu}^{6+}$  ion ground-state configuration is  $1s^2 2s^2 2p^6 3s^2 3p^6 3d^5$  one notes that the 3d subshell is half opened, which results in a maximum complexity for the 3-3 or 3-4 transitions (inner or outer transitions from M shell). This provides an additional motivation for the XUV-absorption study in a copper plasma.

The present paper is organized as follows. In Section 2 we describe the experimental setup used during this campaign. Measurements are then presented in Section 3. Section 4 is devoted to hydrodynamic calculations performed to characterize the plasma in the experiment. Various theoretical aspects of copper XUV absorption are then described in Section 5. A comparison of computations with the present measurements is lastly proposed in Section 6. Secondary aspects are dealt with in appendices. A brief description of recorded data in X-ray range is given in Appendix A. The influence of carbon tampers on the total XUV opacity is analyzed in Appendix B.

## 2. Experimental setup

The experimental setup is based on a scheme already presented in previous papers [17,18]. Two main 1.5-ns long laser beams at  $2\omega$  from LULI 2000 facility are heating spherical gold cavities (hohlraum), delivering an energy in the 400–600 J range. The cavity diameter is 2 mm and its thickness is 20  $\mu\text{m}$ . Two holes are drilled in each cavity, one for the incoming laser, the other for the outgoing radiation, facing the sample to be analyzed. The incident laser beam is converted into a roughly Planckian radiation at a temperature in the 50–100 eV range. The analyzed sample is a planar foil tilted at  $45^\circ$  with respect to the

heating axis and to the radiography axis. This sample is made of a metal – mostly copper in the current campaign – tamped with carbon foils, designed for moderating the sample expansion. The plasma generated from this sample is radiographed by a backlighter (BL) emission, produced by the interaction of a third LULI laser beam with a gold massive foil. This beam, of 0.9-ns duration and about 10-J energy, is delayed by 1.5 ns with respect to the heating pulse for shots up to #83, and by 1 ns for shots after #83.

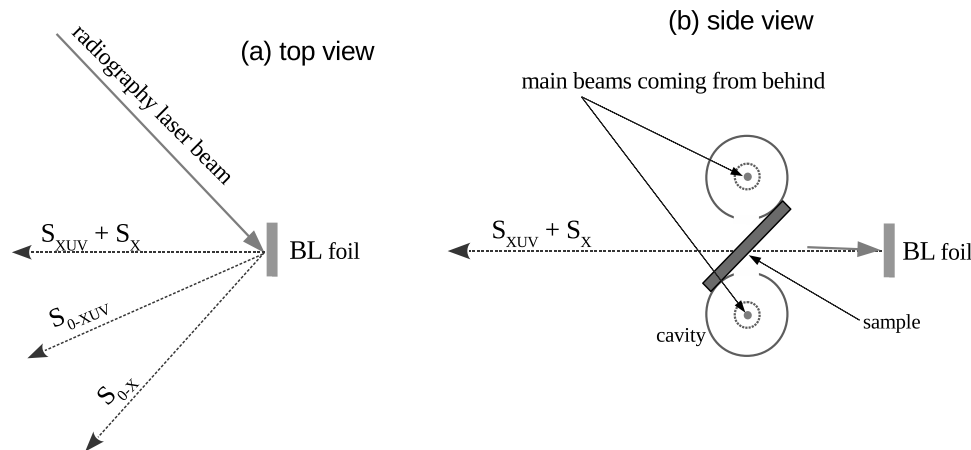
The backlighter emission is analyzed with four spectrometers. The layout of these devices and of the beams is shown on Fig. 1. The spectrometers  $S_{\text{XUV}}$  and  $S_{\text{X}}$  are aligned on the radiography axis and detect the absorbed beam in the XUV range (80–180 eV) and in the X-ray range (700–1700 eV) respectively. The spectrometers  $S_{0\text{-XUV}}$  and  $S_{0\text{-X}}$  provide an off axis detection of the BL emission unabsorbed by the sample. A description of the XUV spectrometers is provided in Ref. [19]. The  $S_{\text{X}}$ ,  $S_{0\text{-XUV}}$  and  $S_{0\text{-X}}$  spectrometers record radiation using image plate detectors, while the  $S_{\text{XUV}}$  spectrometer is equipped with a streak camera.

The main diagnostic used during this campaign is a pinhole camera which allows us to check the laser focusing in the hohlraums. With respect to the previous LULI campaign [17] three main differences in the setup must be emphasized. First, the heating-laser energy is much higher, about 500 J versus 100 J previously. Second, the backlighter delay is shorter 1 ns or 1.5 ns versus 2.5 ns in 2016. Last, the transmitted signal in XUV range is time-resolved. The first two differences result in a higher electronic temperature of the sampled plasma. Therefore conditions analyzed in this paper are quite different from those in previous campaigns.

## 3. Extreme-UV absorption measurements

As mentioned above, the current experimental setup allows us to detect X-ray and XUV absorption. X-ray absorption by plasmas has been a widely investigated topic during the last decades [18,20–28]. The comparison of experimental and theoretical spectra most often provides useful information about sample temperature and density. A brief description of the recorded X-ray data during the present campaign is given in Appendix A.

A series of shots with cavities and absorption foils intended to measure the XUV opacity have been performed. These are named “absorption shots”. Their list is given in Table 1. After shot 101, the camera position was shifted in order to observe a different XUV range, so that the spectral range detected is 70–175 eV (71–177 Å) for shots up to #101, and 55–120 eV (103–225 Å) above.



**Fig. 1.** (a) Top view of the layout of the four spectrometers. The gold cavities, if present, are located above and below the drawing plane. The  $S_{\text{XUV}}$  and  $S_{\text{X}}$  spectrometers detect the absorbed signal, while the  $S_{0\text{-XUV}}$  and  $S_{0\text{-X}}$  spectrometers measure the unabsorbed light. Their angle of detection is respectively  $23^\circ$  and  $50^\circ$  from the radiography axis. (b) Side view of the experimental layout during an absorption shot. The BL beam comes from behind at a  $45^\circ$  incidence. Only the radiography axis is shown. The detectors  $S_{0\text{-XUV}}$  and  $S_{0\text{-X}}$  are off plane and not shown here.

**Table 1**

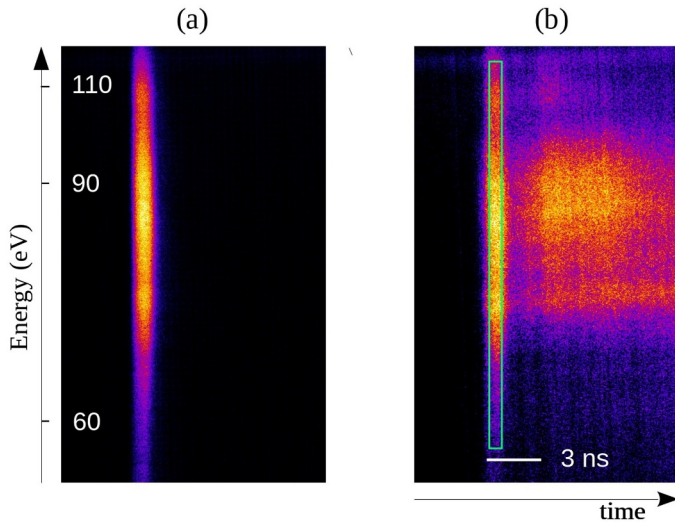
List of XUV shots. All samples are tamped by two 70-nm carbon slabs, with a total areal mass of  $42.4 \mu\text{g}/\text{cm}^2$ . Sample widths refer to the cold material. The tabulated areal masses include a factor  $\sqrt{2}$  accounting for the  $45^\circ$  incidence of the probe beam. “North” and “South” columns refer to the energy of each of the heating beams.

Shot number	Element	Sample width (nm)	Areal mass ( $\mu\text{g}/\text{cm}^2$ )	Energies at $2\omega$ (J)	
				North	South
91	Al/Ni/Al	38/12/38	14.5/15.1/14.5	595	515
93	Cu	11	13.9	598	474
94	Cu	22	27.9	491	448
96	Cu	11	13.9	488	498
98	Al/Cu/Al	38/11/38	14.5/13.9/14.5	540	491
102	CuO	15	10.7 + 2.7	592	651
106	Cu	22	27.9	543	539
107	Cu	11	13.9	555	528
109	Cu	11	13.9	543	558

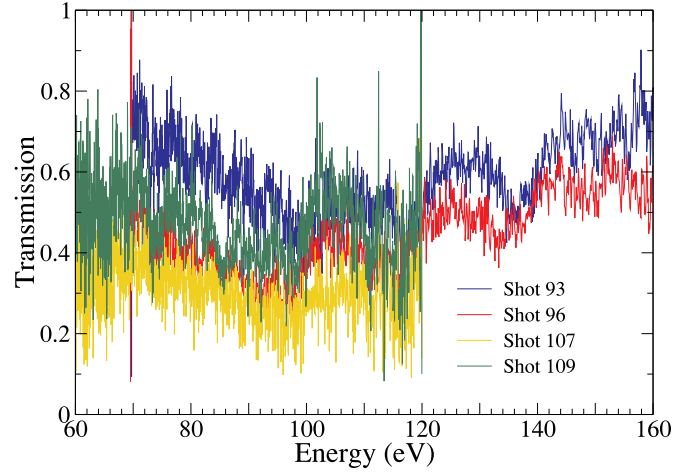
These shots involving cavities and absorption foils must be complemented with shots providing a reliable determination of the backlighter spectral intensity. We have proceeded as follows. We performed another series of shots involving no absorbing sample and no cavities, named “backlighter shots”. For these shots one records on the streak camera located after the  $S_{\text{XUV}}$  spectrometer the time-dependent spectrum  $I(\text{BL}; S_{\text{XUV}}; E, t)$ . On this same shot one records on the image plate located after the off-axis  $S_{0\text{-XUV}}$  spectrometer the time-integrated signal  $I(\text{BL}; S_{0\text{-XUV}}; E)$ . Accordingly, when an “absorption shot” is performed with targets, the on-axis time-dependent signal is  $I(\text{abs}; S_{\text{XUV}}; E, t)$  and the off-axis time-integrated signal is  $I(\text{abs}; S_{0\text{-XUV}}; E)$ . If the signals  $I(\text{BL}; S_{0\text{-XUV}}; E)$  and  $I(\text{abs}; S_{0\text{-XUV}}; E)$  without time resolution are similar, one estimates that both shots were performed in similar backlighter conditions. Then one obtains the spectral transmission from the expression

$$\mathcal{T}(E) = \frac{\int_{\Delta t} I(\text{abs}; S_{\text{XUV}}; E, t) dt}{\int_{\Delta t} I(\text{BL}; S_{\text{XUV}}; E, t) dt} \quad \text{if } I(\text{BL}; S_{0\text{-XUV}}; E) \simeq I(\text{abs}; S_{0\text{-XUV}}; E) \quad (1)$$

where the choice for the integration interval  $\Delta t$  is explained below.



**Fig. 2.** Backlighter and absorption time-dependent spectra recorded on the streak camera. Subfigures (a) and (b) refer to shots 105 and 107 respectively. The green rectangular frame represents the zone used for computing the transmission signal. The same temporal and spectral zone is selected on both shots.



**Fig. 3.** Transmission in XUV range measured on 4 different shots on LULI 2000 facility.

An example of time-dependent backlighter- and absorption-shot recordings is given in Fig. 2. On the Fig. 2a, one observes the incident backlighter pulse. The above-mentioned interval  $\Delta t$  may be taken as the horizontal width of the bright band or a fraction of it, as shown by the horizontal side of the green frame shown on Fig. 2b. Fig. 2b displays the signal recorded with cavities and absorbing sample. The leftmost bright band is the backlighter signal with partial absorption by the sample. A careful inspection shows some wavelength-dependent structures. The important — because of its significant time-integrated value — broad shape on the right side originates from the self-emission of cavities and of the sample. One notes that this emission is strongly wavelength-dependent and delayed with respect to the backlighter signal. The time-resolved detection allows us to eliminate this contribution in the transmission (1).

In this campaign, we have chosen the reference shots (backlighter shots) 97 (resp. 105) for determining the transmission for shots 91–98 (resp. 102–109). The various parameters recorded on shots 97 and 105 allow us to consider that they are acceptable as reference shots.

Among all the shots listed in Table 1 we have selected four shots on a series of monitoring criteria: target manufacturing quality, energy of the laser beams, informations from the pinhole image, streak synchronization, direct inspection of spectra, signal-to-noise ratio acceptability. The raw data for these shots are presented in Fig. 3. The data appear to be quite noisy but exhibit some reproducible features.

In order to get a clearer picture, we performed a basic smoothing on the raw transmission data. We tried several different averaging methods. The simplest one consists in computing the arithmetic mean of the transmission values of, e.g.,  $\pm 15$  points around the current one (uniform ponderation). Averaged transmission data obtained with this method are presented in Fig. 4a. The number  $N = 15$  is chosen so that the spanned energy interval  $E_{j+15} - E_{j-15} \simeq 1.34 \text{ eV}$  at 100 eV, 0.94 eV at 80 eV, is a good approximation of the experimental resolution estimated to be  $E/\delta E \simeq 70$ . As seen on this figure, these averaged values are rather sensitive to strong fluctuations in primary data and we may use smoother averaging procedures. Another formula tested here is the “squared cosine average”  $\bar{T}_n = \sum_{-N \leq j \leq N} \cos^2(\pi j/2N) T_{n+j}/N$ , properly normalized since  $N$  is the sum of the squared cosines. If we want to keep the same FWHM as for the above uniform ponderation, we must chose  $N$  twice as big. In Fig. 4b we present such an average with  $N = 31$ . One must notice that there is some arbitrariness in this procedure but the smoothed data is compatible with our estimate of the experimental error on transmissions. On the smoothed data in Fig. 4 one observes that, while plasma temperature and density may change from shot to shot, several structures in 70–120 eV range are reproducible.

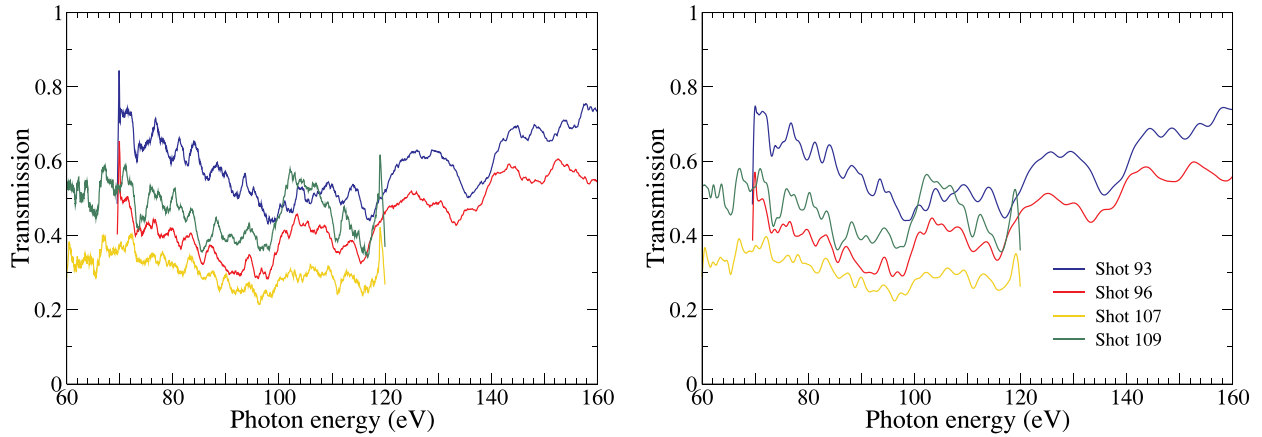


Fig. 4. Transmission in XUV range processed : comparison of two smoothing procedures.

#### 4. Hydrodynamic analysis

Hydrodynamic simulations were performed using the 2D Lagrangian radiation hydrodynamics code FCI2 in cylindrical geometry. The general features of the hydro-code and their implementation may be found in our previous publications [17,18]. The radiative energy within the cavity is simulated by a multi-group Monte-Carlo transport algorithm. The laser heating of both cavities is treated by a ray-tracing algorithm accounting for the propagation, refraction and collisional absorption of the laser flux. We take into account an estimate of the laser energy inside each cavity and a 1.5 ns square laser pulse. The focal spot is described by a 528- $\mu\text{m}$  diameter super-Gaussian shape. The window from which the radiation flows out of the cavity to heat the sample (“heating window”) is not included in the simulation.

In a second step, we resort to a post-processor to evaluate the incident flux on the sample. The distance between the cavity hole and the sample is taken as 1.75 mm, which corresponds to its nominal value (lower distances had been considered in previous calculations in order to account for our specific geometry). Finally, the 45°-angle between the sample and the axis defined by the centers of the two cavities is included in the computation. To estimate the flux, a fictitious window is created in the cavity in order to simulate the above-mentioned heating window. The radius of such a window (constant in time) is 450  $\mu\text{m}$  and a closing of the order of 50  $\mu\text{m}$  at the instant of the probe (1 ns) is considered.

The sample is assumed to be in local thermodynamical equilibrium, irradiated by the calculated Planckian radiation. The simulations of the hydrodynamics of the sample are performed with the calculated radiative flux profile, taking into account the uncertainties on laser energy deposition in the cavity (backscattering, attenuation in phase plates, 3D aspects of the geometry, etc.) by a 25% lowering of the laser energy, determined by the feedback of laser spectroscopy experimental campaigns at LULI facility over the past fifteen years. These calculations allow one to predict the thermodynamic conditions of the sample when it is irradiated by a backlight 1 ns after the heating pulse.

The results for shot 96 are plotted on Fig. 5a and b for temperature and mass density respectively. Data points in the time interval 1–2 ns where the backlighter is switched on are emphasized. The obtained radiative temperature inside the cavities is about 75 eV. It appears that important spatial and temporal variations in temperature and density are expected during this probing interval, especially inside the carbon slabs.

#### 5. Analysis of XUV absorption using various atomic codes

In this section we will review a series of properties of XUV opacity derived from the use of various atomic codes. We will then compare some experimental spectra to theoretical predictions. As mentioned in the introduction the presence of a nearly half opened 3d-subshell in copper for  $T \sim 20$  eV results in particularly complex spectra. This is

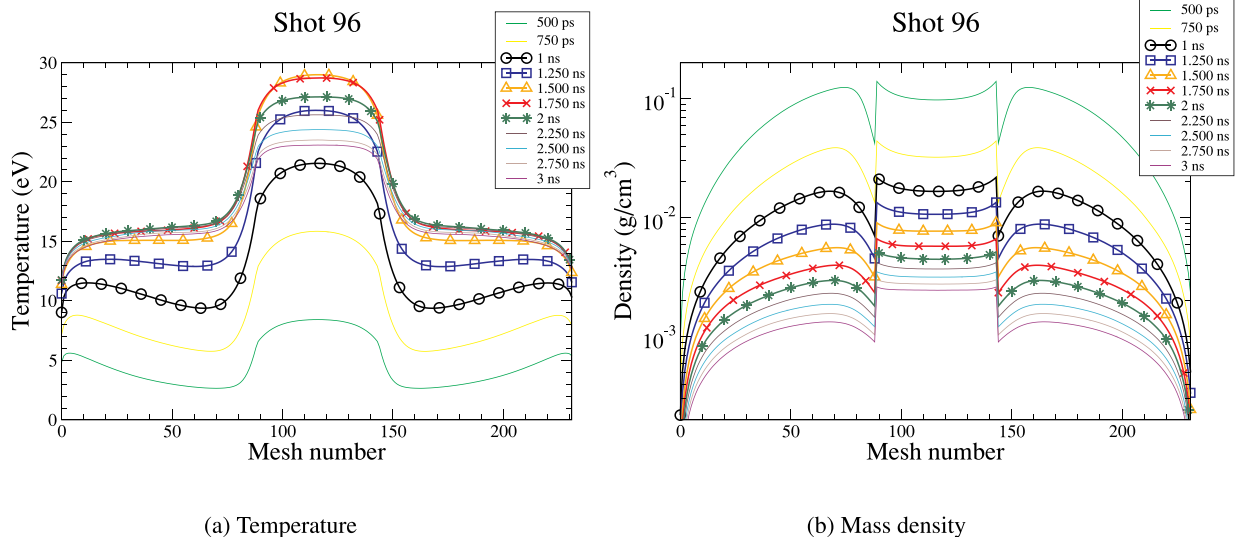


Fig. 5. Hydrodynamic analysis for shot 96 using FCI2 code. A 25% lowering on the laser incident energy has been applied.



**Table 2**

Number of lines in the array  $3d^n\sigma - 3d^{n-1}4f\sigma$  as a function of  $n$  and as a function of various spectator subshells  $\sigma$ . The second column corresponds to the case where all subshells except 3d and 4f are closed. The third column contains the number of  $3d^n4s - 3d^{n-1}4s4f$  lines, etc. In the case labeled 4f transitions  $3d^n4f - 3d^{n-1}4f^2$  are numbered, so that the 4f subshell is active. In this table the principal quantum number of the spectator electron must verify  $m > 3$  for  $ms$ ,  $mp$ , and  $md$  subshells, and  $m > 4$  for  $mf$  subshell.

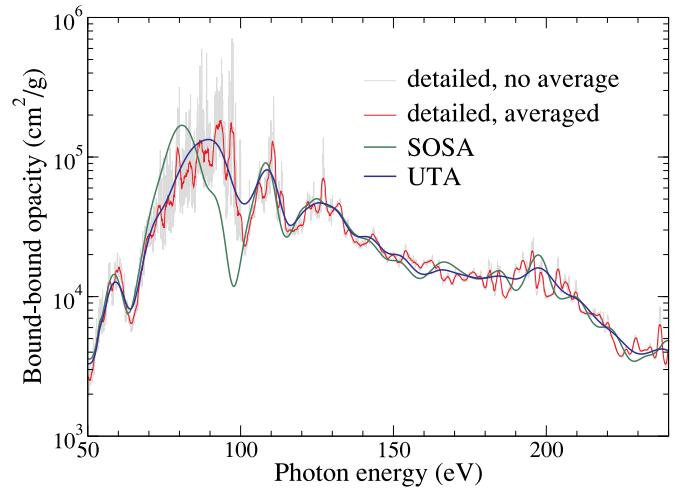
n	Spectator subshell						
	none	ms	mp	md	4f	mf	3p <sup>4</sup>
1	3	11	83	171	108	219	458
2	81	308	2435	5280	3590	7365	13738
3	721	2763	22,261	50,014	35,433	73,134	127,434
4	2825	10,870	88,492	202,749	146,856	304,121	510,687
5	5470	21,085	172,440	398,540	291,521	604,605	998,734

illustrated by Table 2 where the number of lines in the array  $3d^n - 3d^{n-1}4f$  is given in the second column as a function of  $n$ . This number of lines becomes huge when one considers the presence of a spectator electron, as shown by the following columns in the same table. Because of a symmetry property [29], all  $3d^n$  cases with  $n \leq 10$  are considered: if  $\sigma$  is any spectator subshell, the number of lines in the array  $3d^n\sigma - 3d^{n-1}4f\sigma$  is equal to the number of lines in the array  $3d^{11-n}\sigma - 3d^{10-n}4f\sigma$ . For instance the array  $3d^74d - 3d^64d4f$  contains 202,749 lines. In the case of a  $3p^5$  spectator subshell, the number of lines is the same as for a  $4p$  spectator subshell given by column 4. This shows that elaborate atomic models are required for the description of such XUV spectra.

The atomic codes used for the interpretation of our results are the hybrid code SCO-RCG [30,31], the detailed codes HULLAC [32] and FAC [33]. Since these codes have been described several times in the literature, one will refer to the quoted bibliography for details.

### 5.1. Configuration-average shift

The large number of transitions involved in the 3-3 array of copper at temperatures around 20 eV would incite us to use averaging procedures such as nonrelativistic configuration average or Unresolved Transition Array (UTA) scheme [34], relativistic configuration average or Spin-Orbit Split Array (SOSA) scheme [35], or even super-configuration average (STA) [36]. These various averaging modes have been implemented in the SCO-RCG code. An important feature of such approaches is that the average array positions are obtained using approximations which may be drastic because the interaction between levels belonging to different configurations cannot be taken into account. This property is illustrated on Fig. 6 which represents the copper bound-bound opacity computed with the SCO-RCG code. Only bound-bound transitions are included. It appears that the UTA mode results in a maximum opacity close to 90 eV, which is close to the maximum of the detailed computation at 93 eV. Conversely, the SOSA mode results in a maximum opacity at 80 eV, i.e., in a red shift of the peak much more significant than in UTA mode. The dip in opacity observed at 103 eV in detailed or UTA computations is also shifted towards 98 eV in SOSA mode and its depth is then greater. In the other regions of the spectrum, the various computation models do not exhibit such significant differences. Indeed the barycenters of one given UTA and of the group of SOSAs corresponding to the same nonrelativistic configuration may differ in energy position: this is due to the fact that the interaction between relativistic configurations is accounted for in the computation of UTA position and not in the computation of SOSA position. Furthermore, if one needs to compute the Rosseland opacity important for a proper radiative-transfer modeling in astrophysics, the value is sensitive to line profile and therefore detailed and UTA (or even more SOSA) calculations will differ significantly.

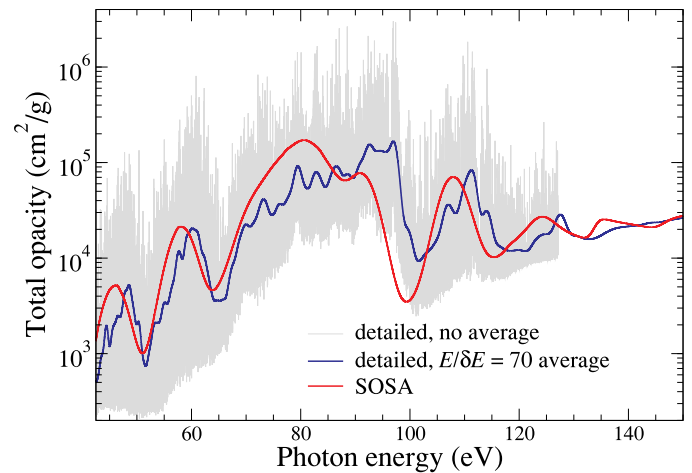


**Fig. 6.** Effect of configuration average on the XUV copper opacity computed with SCO-RCG code. The plasma temperature and density are 20 eV and 10 mg/cm<sup>3</sup> respectively. The red curve is a numerical average on 200 consecutive values of the detailed computation — which spans 1.3 eV and simulates an experimental broadening similar to the actual resolution. Green and blue curves are configuration-average results, arising from theoretical formulas.

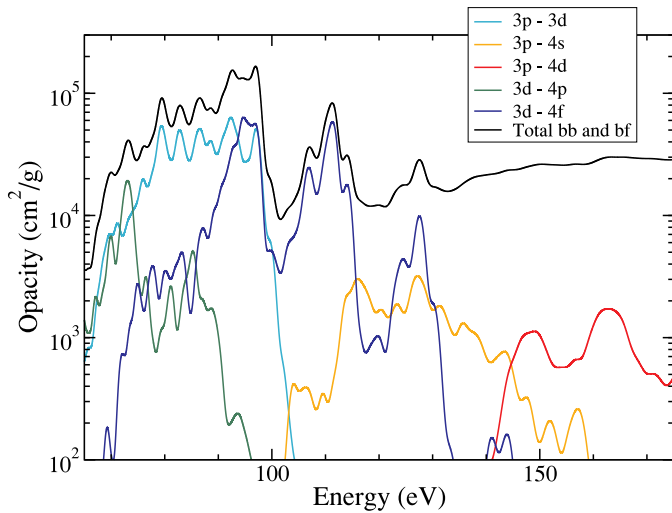
Since the only averaging mode currently available in FAC is the relativistic configuration average or SOSA, one expects that such averaging will manifest itself as a red-shifted opacity profile. This is indeed what we observe in Fig. 7 where an even greater shift of about 30 eV is visible. This computation is restricted to bound-free and bound-bound transitions 3-3 and 3-4, and doubly excited states are not included in order to keep the detailed approach tractable. For instance in Cu<sup>6+</sup>, we account for configurations  $3s^2 3p^6 3d^5$ ,  $3s^2 3p^5 3d^6$ ,  $3s^2 3p^6 3d^4 4^*1$ ,  $3s^2 3p^5 3d^5 4^*1$ . The above considerations prevent us to use configuration-average calculations in FAC when accurate XUV opacities are required.

### 5.2. Spectral analysis of the various arrays

In order to define which transitions are related to the above-mentioned opacity shift, it is useful to compute the contribution to opacity



**Fig. 7.** Effect of configuration average on the XUV copper opacity computed with FAC. The plasma temperature and density are 20 eV and 10 mg/cm<sup>3</sup> respectively. The gray curve is the detailed computation with only natural and Doppler broadening accounted for. The blue curve is an average of detailed computation, obtained by convoluting data with a Gaussian response file such as  $E/\delta E = 70$  which is close to the experimental resolution. The red curve comes from FAC configuration-average calculation.



**Fig. 8.** Various contributions to copper opacity at  $T = 20$  eV and  $\rho = 10$  mg/cm<sup>3</sup> computed with FAC in detailed mode. All computations are performed in detailed mode and convoluted by a response curve such as  $E/\delta E = 70$ . The average charge is  $\langle Z \rangle = 6.26$ .

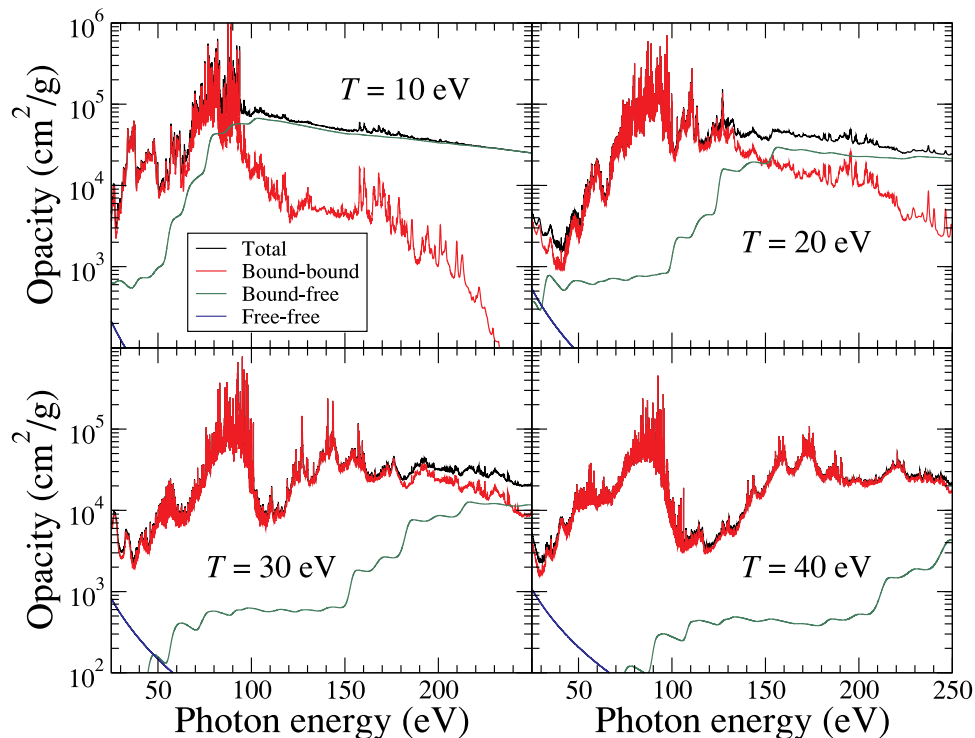
of the various arrays such as 3p-3d, 3d-4p, 3d-4f,... The breakdown of the various contributions to XUV copper opacity at 20 eV is presented in Fig. 8. Ions Cu<sup>3+</sup> to Cu<sup>9+</sup> are considered. Knowing the limitations associated to the SOSA mode, the computation was performed in detailed mode, where 3-3 and 3-4 lines were accounted for. The contribution of 3-5 lines is not fully negligible but smaller than what is presented here. As above, configurations 3p<sup>6</sup> 3d<sup>N-18</sup>, 3p<sup>5</sup> 3d<sup>N-17</sup>, 3p<sup>6</sup> 3d<sup>N-19</sup> 4\*1, 3p<sup>5</sup> 3d<sup>N-18</sup> 4\*1 are accounted for,  $N$  being the number of bound electrons — the closed-shell core 1s<sup>2</sup> 2s<sup>2</sup> 2p<sup>6</sup> 3s<sup>2</sup> is omitted. Since levels with an opened 3p<sup>5</sup> subshell are weakly populated at  $T = 20$  eV, transitions 3s-3p have not been included. One notes that in the analyzed conditions the main contribution to opacity in the 90–100 eV region comes from the 3p-3d and 3d-4f lines. The 3d-4p contribution is only significant in

the region below 80 eV, while 3p-4s (resp. 3p-4d) show up above 110 eV (resp. 140 eV). Above 120 eV, the main contribution to opacity comes from photoionization (bound-free processes). The 4-4 transitions contribute to the opacity in the region below 65 eV, for a moderate fraction. Close to 70 eV one also expects a small contribution from 4 to 5 transitions, not detailed here. We did not try to match each of the 3d-4f peaks to a particular charge state, though the visible structures correspond certainly to Cu<sup>3+</sup>, Cu<sup>6+</sup>, Cu<sup>7+</sup>, and marginally Cu<sup>4+</sup>, Cu<sup>8+</sup>. Conversely the contribution of the various charge states to the 3p-3d opacity are overlapping. In view of this analysis it appears that the SOSA shift mentioned above is mostly related to the 3p-3d array, with a possible influence of the 3d-4f array.

### 5.3. Temperature dependence

The influence of the temperature on the absorption spectrum analyzed with SCO-RCG code is presented on Fig. 9, where the bound-bound, bound-free, free-free contributions are shown separately. In this computation transitions such as 3-5 and above are accounted for, as well as multiply excited states. The bound-bound contribution, dominant close to  $E = 100$  eV whatever the temperature, is roughly temperature-independent in the 100 eV region. Below 70 eV — where 4-4 and 4-5 transitions are dominant — the opacity decreases for plasma temperatures  $T$  above 10 eV. Conversely, for energies above 120 eV where 3-5 transitions occur, the bound-bound opacity increases significantly with  $T$ . The bound-free opacity significantly decreases with  $T$ , as the 3d subshell depopulates.

Accordingly, the transmission of a 14- $\mu$ g/cm<sup>2</sup> plasma slab of copper significantly evolves when  $T$  changes from 10 to 40 eV. This is shown in Fig. 10 drawn in the same conditions as Fig. 9. One observes that at 10 eV such a sample is strongly absorbing in the 70–150 eV range, while some transmission windows appear at 30 eV and above. In general the XUV absorption depth and shape exhibit a strong temperature dependence. This behavior substantially differs from what is observed in the X-ray range where as a rule one may follow the gradual evolution of peaks with temperature (see, e.g., Ref. [37]), and it indicates that



**Fig. 9.** Copper opacity computed at four different temperatures with the SCO-RCG code. The plasma density is 10 mg/cm<sup>3</sup> in each case.

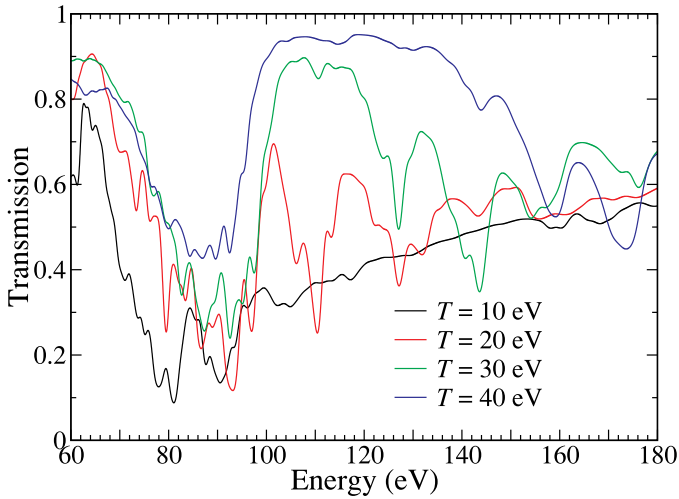
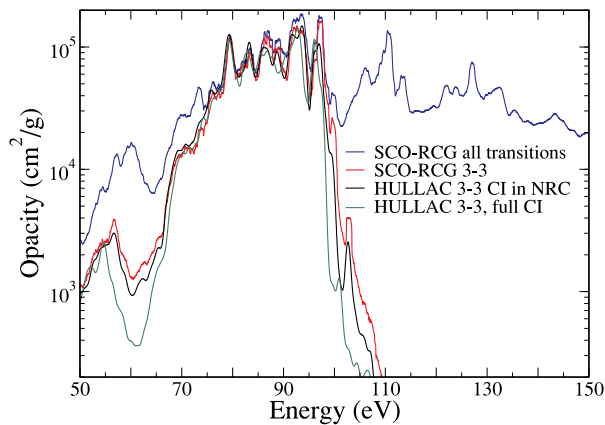


Fig. 10. Copper transmission computed at four different temperatures with the SCO-RCG code. The plasma mass density is  $10 \text{ mg/cm}^3$  and its areal mass is  $14 \mu\text{g/cm}^2$ . The computed transmission has been convolved with a Gaussian response file such as  $E/\delta E = 70$ .

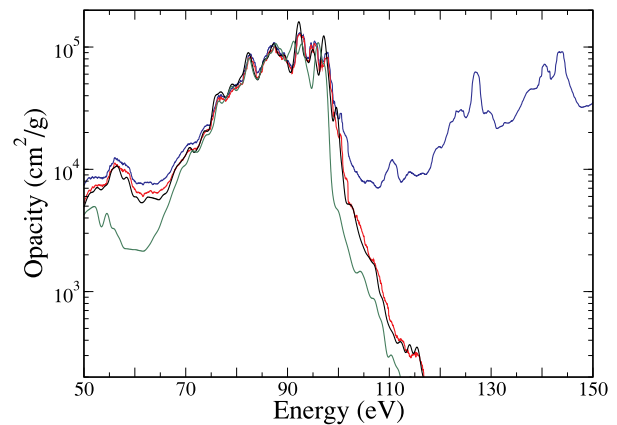
temperature gradients should then play an important role. However, on this figure one observes that the position of the main absorption structures, e.g., 92, 110, 128 eV...do not change with  $T$ , therefore they should remain visible even in the presence of temperature gradients.

#### 5.4. Influence of configuration interaction

Configuration-interaction (CI) has been known for long to strongly affect  $\Delta n = 0$  arrays [38–40]. For instance the effect of CI on xenon or tin spectral properties relevant to XUV sources for nanolithography has been investigated into detail [41]. In order to analyze CI effect in copper opacity, we have performed a computation with the detailed code HULLAC. This code permits to specify whether CI is fully accounted for, accounted for inside nonrelativistic configurations (NRC), or switched off. The HULLAC results for XUV opacity of copper are shown in Fig. 11a and b, at a temperature of 20 and 30 eV respectively. In HULLAC, options full CI and CI in NRC are compared and only 3-3 transitions are considered. On the same graph, the SCO-RCG results — accounting only for CI inside NRC — are shown, with only 3-3 transitions included or all transitions included. It turns out that, considering 3-3 transitions only, SCO-RCG and HULLAC with CI in NRC closely



(a) Configuration interaction in copper at 20 eV.



(b) Configuration interaction in copper at 30 eV.

Fig. 11. Opacity in copper: configuration interaction effect analyzed with HULLAC. Copper mass density is  $10 \text{ mg/cm}^3$ . Comparison is made with SCO-RCG code which only includes configuration interaction inside nonrelativistic configurations. All curves are 1-eV averaged to make the figure more readable.

agree on the whole considered energy range. When full CI is accounted for in HULLAC, the opacity locally drops by a factor of about 3 in the wings of the main 3-3 structure, close to 60 eV and above 100 eV. Therefore, CI will not be very important at  $T = 20 \text{ eV}$ , because the effect is mostly hidden by the contribution of other transitions. A similar property has been reported in iron [42].

#### 5.5. HULLAC-FAC comparison

An example of copper plasma transmission computed with the detailed codes HULLAC and FAC is given on Fig. 12. Both codes assume an areal mass of  $14 \mu\text{g/cm}^2$  and use the same configuration basis. Four charge states are included in HULLAC, and 7 in FAC. The overall aspect is similar, though some differences are due to different averaging methods. The discrepancy at  $E \approx 50 \text{ eV}$  is attributed to configuration interaction, fully included in FAC only.

#### 6. Analysis of experimental data

We intend here to focus the discussion on shots 96 and 109. The above-mentioned squared-cosine smoothing procedure involving 31 data points results in the plots displayed in Fig. 13a. These shots

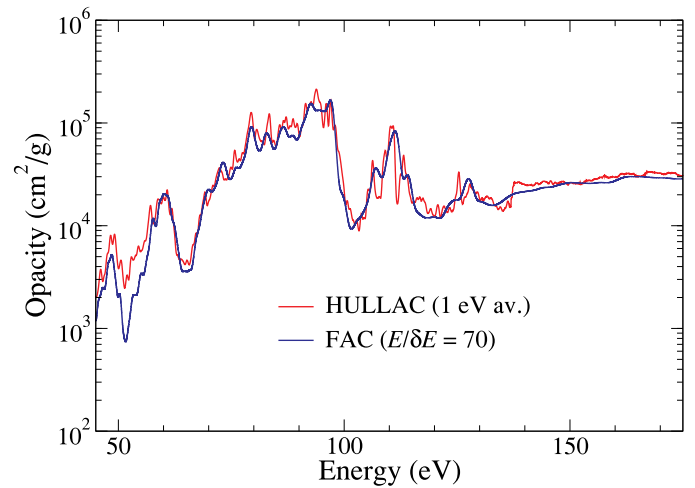
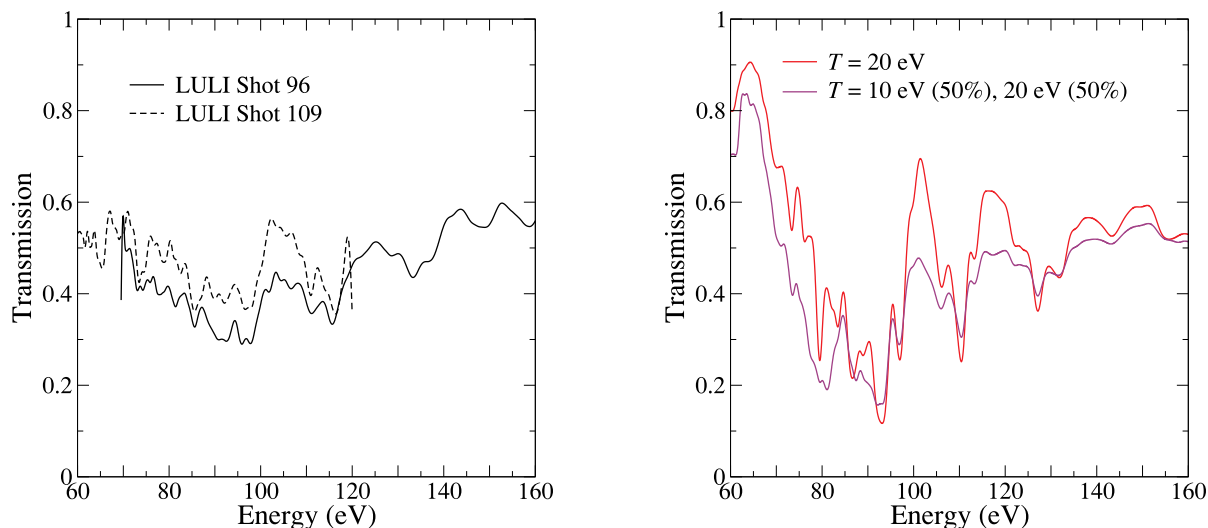


Fig. 12. Copper transmission at 20 eV and  $10 \text{ mg/cc}$  computed with detailed codes HULLAC and FAC. HULLAC computation is averaged by convolution with a response file of 1-eV FWHM, while FAC is averaged by convolution with a Gaussian function such as  $E/\delta E = 70$ .





(a) Measured XUV transmission for shots 96 and 109. A squared cosine smoothing procedure was applied to raw data.

(b) XUV transmission in copper computed with SCO-RCG. A simulation of the effect of gradients has been done by averaging the transmissions at temperatures of 10 eV and 20 eV.

**Fig. 13.** XUV transmission in copper : measurements and SCO-RCG computations.

recorded on different but overlapping energy ranges shows very similar features. Copper areal mass is  $14 \mu\text{g}/\text{cm}^2$  in both cases, and carbon tampers total areal mass is  $42.4 \mu\text{g}/\text{cm}^2$ .

The SCO-RCG computation involving copper (carbon is not included) is presented in Fig. 13b. The red curve is a computation assuming  $T = 20$  eV and the purple curve is the geometrical average of 10 eV and 20 eV computations, in order to account for gradients.

As seen on Figs. 6 or 7, assuming a plasma temperature of 20 eV, in SCO-RCG or FAC calculations the copper absorption peaks at about 95 eV in detailed mode and 80 eV in SOSA mode. The maximum absorption observed on shot 96 is between 90 and 97 eV. For shot 109 the maximum is less clearly defined, nevertheless it is not located close to 80 eV. This shows that the detailed computations are in better agreement with the measurements than the SOSA computations. The contribution of various transitions proposed in Fig. 8 suggests that this maximum absorption is mostly due to the 3p-3d and 3d-4f transitions.

One notes that the absolute value of transmission calculated with SCO-RCG is similar to the measured one except in the low-energy region. The variation of the transmission is less in the measured spectra — it varies only between 0.3 and 0.6 — than in computations. The structures associated to inner M-shell transitions, in particular at 92 eV or 97 eV, agree in position. Above 120 eV, where transitions 3–4 and 3–5 are dominant, the overall agreement is fair. The red curve  $T = 20$  eV shows transmission variations much greater than observed, while the purple curve is closer to shot 96 data. This indicates that gradients are probably important in this experiment. In view of the limited amount of data available and of the difficulty in calibrating the transmission measurements, we consider these results as really encouraging.

## 7. Conclusion

In this paper we have described and analyzed XUV spectra recorded

### Appendix A. X-ray measurements

The experimental set-up we use allows a simultaneous detection of the plasma transmission in XUV and X-ray ranges. Since X-ray results have been studied several times by our group in the past [17,18,23,26], the results in this range will be given less attention here. The measurements analyzed here have been performed with a backlighter delay of 1.5 ns, vs 1 ns for shots analyzed in the main text. As predicted by the hydro analysis

on the LULI 2000 facility by creating plasmas from metal targets with the indirect drive scheme. Most of this campaign has been devoted to copper samples for which XUV measurements are rather scarce. In order to get rid of the cavity self-emission, a time dependent detection was used. Using the hybrid code SCO-RCG, the detailed code HULLAC, and the code FAC in detailed or configuration average mode, we have been able to describe various properties of the XUV absorption in copper at few tens of eV. The importance of various transitions has been analyzed showing the dominant contribution of 3p-3d and 3d-4f transitions in the 80–110 eV range, and of bound-free processes above. It turns out that the relativistic-configuration average mode (SOSA) is not adequate to describe the main absorption region, since it produces a SOSA red shift of about 10 eV with respect to the detailed calculation. The configuration interaction effects have been investigated using the HULLAC code, and shown to be moderate except in the wings of the 3-3 structure, close to 60 and 105 eV. The comparison of calculations with the LULI campaign in the 60–160 eV range shows a semi-quantitative agreement. While the average absorption level is correctly reproduced, discrepancies are visible in the low-energy region. A preliminary analysis indicates that gradients may be important, e.g., in the 100–160 eV range. Discrepancies in the low energy part of the spectrum may also be related to uncertainties in the calibration procedure of the transmission. In the forthcoming campaign, we intend to improve this calibration procedure and to investigate gradients effects with more care.

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presented above, one may expect temperatures and densities lower than in shots 96 or 109.

As seen on Fig. 1, since the absorbed signal and the unabsorbed signal can be recorded during the same shot but at different angles, a calibration procedure must be used. It consists in measuring the signal on both spectrometers when no sample or cavity is present. Details about this procedure may be found in our previous paper [17].

A single spectrum is shown on Fig. A.14. Structures attributed to 2p-3d and 2p-4d transitions are visible. A simple computation based on the detailed atomic code FAC [33] roughly agrees with recorded spectrum assuming  $T \simeq 15\text{--}20$  eV,  $\rho \simeq 10$  mg/cm<sup>3</sup> as can be seen on Fig. A.15. A FAC computation in UTA mode is presented in Fig. A.15, for plasma temperatures of 15 or 20 eV, and 10 mg/cc density. Only transitions  $2p^6 \rightarrow 2p^5nd$  with  $n \leq 5$  were considered. The effect of a  $3p^5$  and  $4l$  spectator electron was included as well as bound-free transitions. Carbon absorption was not included in this basic computation. We note an acceptable agreement on the position of the 2p-3d and 2p-4d structures, though as in Ref. [17] the transmission associated to bound-free processes below 930 eV and above 1070 eV is much lower in the experiment than in the computation. Though a complete explanation is still to come, we attribute this discrepancy to issues in the calibration procedure.

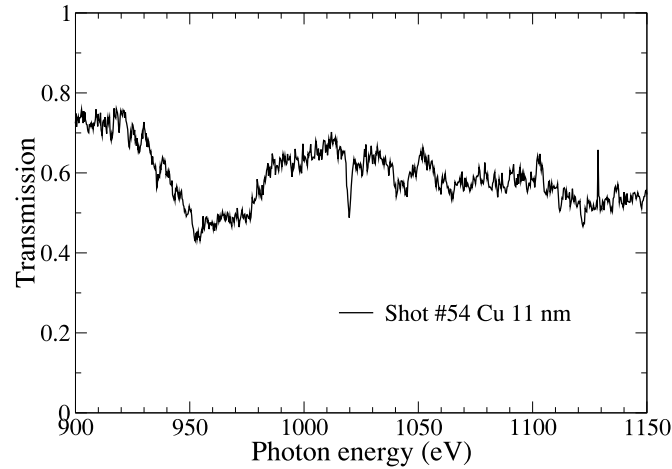


Fig. A14. Measurement of copper absorption in X-ray range (shot 54). The copper areal mass is 14  $\mu\text{g}/\text{cm}^2$ .

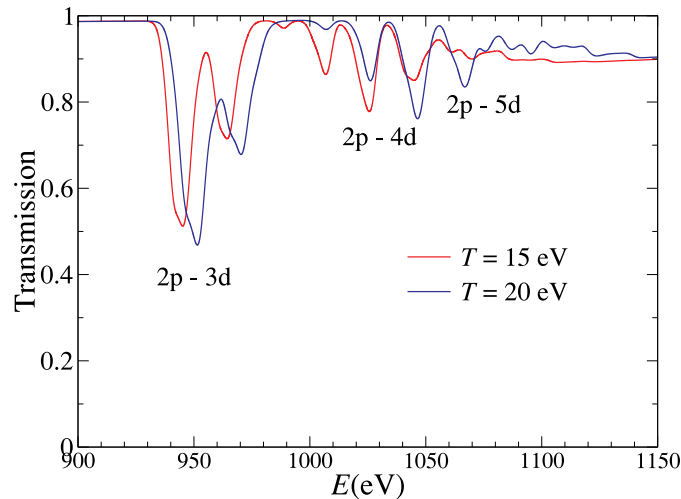
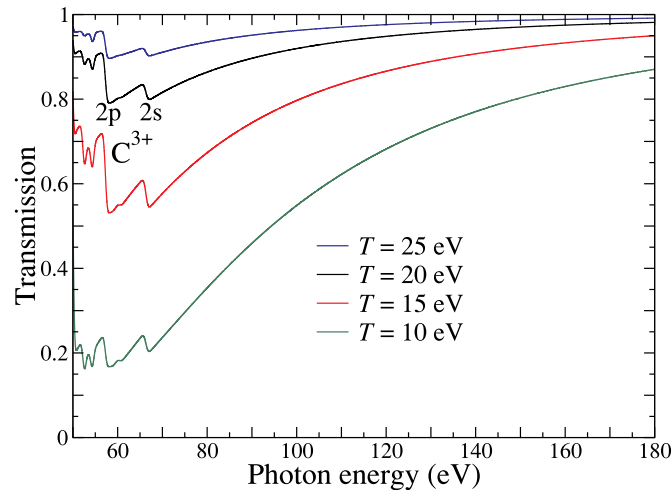


Fig. A15. Computation of copper absorption with FAC code in configuration average mode. The copper mass density is 10 mg/cm<sup>3</sup> and the areal density is 14  $\mu\text{g}/\text{cm}^2$ .

## Appendix B. XUV opacity of carbon

The transmission of a 42.4- $\mu\text{g}/\text{cm}^2$  slab of carbon computed by FAC is presented in Fig. B.16. Computations are performed in the standard relativistic configuration average (SOSA) mode provided by the code. The carbon mass density has been taken as 3 mg/cm<sup>3</sup>. A convolution by a Gaussian response file with  $E/\delta E = 70$  has been performed in order to simulate the experimental broadening. The carbon XUV opacity in the 50–180 eV range is mostly explained by L-shell photoionization. Some bound-bound processes contribute moderately to opacity below 60 eV, e.g., the peaks near 52 eV and 54 eV are attributed to 2s-5p transitions in C<sup>2+</sup> and C<sup>3+</sup>. For a temperature of 20 eV, the transmission is about 0.86 at 80-eV photon energy and 0.95 at 120 eV. However the carbon XUV opacity significantly decreases with temperature. At 15 eV, these transmission values are 0.67 and 0.87 respectively, while at 10 eV, they fall off to 0.35 and 0.68 respectively. With the SCO code [43] similar values have been obtained. This temperature dependence can be related to the charge distribution in the carbon plasma. If one ignores K-shell opening, which is unlikely at  $T \sim 20$  eV, the C<sup>4+</sup> ion does not contribute to L-shell photoionization. The C<sup>+</sup> population is very low, about 0.01 at  $T = 15$  eV. Therefore the main contribution to opacity in the 60–180 eV range comes from photoionization of C<sup>2+</sup> and C<sup>3+</sup> ions. Indeed on Fig. B.16 one observes 2p and 2s



**Fig. B16.** Carbon XUV transmission computed with FAC in UTA mode. The plasma density is  $3 \text{ mg/cm}^3$ , and the areal density is  $42.4 \text{ } \mu\text{g/cm}^2$ . The data are convolved with a Gaussian response file such as  $E/\delta E = 70$ .

thresholds of  $\text{C}^{3+}$  ion at 58 and 67 eV respectively, in agreement with NIST database (58.5 eV and 64.5 eV)[44]. The  $\text{C}^{2+}$  ionization threshold at 47.9 eV [44] is outside this plot range. Since photoionization cross-sections rapidly fall off above threshold, the carbon opacity in such conditions mostly depends on  $\text{C}^{3+}$  and on  $\text{C}^{2+}$  to a lesser extent. For instance at  $T = 20 \text{ eV}$  the Saha distribution in the UTA mode is 0.03, 0.28, 0.69 for  $\text{C}^{2+}$ ,  $\text{C}^{3+}$ ,  $\text{C}^{4+}$  populations respectively. Therefore the carbon XUV photoionization is mostly dependent on the  $\text{C}^{2+}$  and  $\text{C}^{3+}$  populations which vary significantly with plasma temperature or density. The conclusions from this study are that carbon tampers contribute to the plasma absorption — significantly at 80-eV photon energy, moderately at 120-eV photon energy — and that this contribution is strongly temperature dependent and therefore exhibits a high sensitivity to gradients.

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