Fiber-Coupled, Time-Gated Al\textsubscript{2}O\textsubscript{3}:C Radioluminescence Dosimetry Technique and Algorithm for Radiation Therapy With LINACs
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Fiber-coupled, Time-gated $\text{Al}_2\text{O}_3$:C Radioluminescence Dosimetry Technique and Algorithm for Radiation Therapy with LINACs

Sylvain Magne, Sybelle Deloule, Aimé Ostrowsky, Pierre Ferdinand

Abstract—An original algorithm for real-time In Vivo Dosimetry (IVD) based on Radioluminescence (RL) of dosimetric-grade $\text{Al}_2\text{O}_3$:C crystals is described and demonstrated in reference conditions with 12-MV photon beams from a Saturne 43 linear accelerator (LINAC), simulating External Beam Radiation Therapy (EBRT) treatments. During the course of irradiation, a portion of electrons is trapped within the $\text{Al}_2\text{O}_3$:C crystal while another portion recombines and generates RL, recorded on-line using an optical fiber. The RL sensitivity is dose-dependent and increases in accordance with the concentration of trapped electrons. Once irradiation is completed, the $\text{Al}_2\text{O}_3$:C crystal is reset by laser light (reusable) and the resultant OSL (Optically Stimulated Luminescence) is also collected back by the remote RL-OSL reader and finally integrated to yield the absorbed dose. During irradiation, scintillation and Cerenkov lights generated within the optical fiber ("stem effect") are removed by a time-discrimination method involving a discriminating unit and a fiber-coupled BGO scintillator placed in the irradiation room, next to the LINAC. The RL signals were then calibrated with respect to reference dose and dose rate data using an ionization chamber (IC). The algorithm relies upon the integral of the RL and provides the accumulated dose (useful to the medical physicist) at any time during irradiation, the dose rate being derived afterwards. It is tested with both step and arbitrary dose rate profiles, manually operated from the LINAC control desk. The doses measured by RL and OSL are both compared to reference doses and deviations are about $\pm$ 2% and $\pm$ 1% respectively, thus demonstrating the reliability of the algorithm for arbitrary profiles and wide range of dose rates. Although the calculation was done off-line, it is amenable to real-time processing during irradiation.

Index Terms— Radiation Therapy, In Vivo Dosimetry, Radioluminescence, Optically Stimulated Luminescence, Time discrimination, Alumina, Optical Fiber Sensor

I. INTRODUCTION

Cancer treatment by External Beam Radiation Therapy (EBRT) involves pulsed photon or electron beams (energy in the range 4 to 25 MeV) delivered by linear accelerators (LINACs). The objective for the radiation oncologist is to deliver the prescribed dose to the tumor while sparing healthy tissues and organs at risk to avoid undesirable complications. According to IAEA [1], the difference between planned and delivered doses must remain within $\pm 2\%$ to $\pm 3\%$. If it exceeds $\pm 5\%$, the treatment should not be initiated and the reasons for discrepancy must be investigated.

Severe accidents in radiation therapy (RT) have been associated with the incorrect use of Treatment-Planning Systems (TPS) or false dose measurement during their commissioning. In vivo Dosimetry (IVD) is an additional safeguard against set-up, dose calculation and transfer errors. It is performed invasively by inserting a suitable dosimeter probe into the patient or non-invasively by placing the dosimeters away (Electronic Portal Imaging Dosimetry - EPID) or onto the skin (point dosimeters) [2]. Since most treatments are fractionated, a deviation in the delivery of the latest dose fraction (e.g. 2 Gy) may be corrected during the next one. For this reason, IVD may be performed with passive dosimeters (mainly thermoluminescent (TLD), RadioPhotoluminescent (RPL) or Optically Stimulated Luminescence (OSL)). However, medical physicists are willing to save time in Quality Assurance (QA) program and in this respect, are looking for real-time (active) dose monitoring. Real-time dose monitoring is also mandatory for some treatments (e.g. Total Body Irradiation (TBI), Total Skin Electron Therapy (TSET)) in order to provide feedback to the physician during the course of the treatment. Since ionization chambers (IC) are usually not used on patients (on account of their size and the use of high voltage), IVD is now often performed with semiconductors (P-N junction type diodes). However, the use of diodes invokes extensive workload due to many additional correction factors (dose rate (source-to-sensor distance), angular incidence, energy etc). Moreover, the coaxial cable disturbs the dose distribution due to presence of metal and the external diameter of diode chains (e.g. 5-diode chains of IBA Dosimetry GmbH (Schwarzenbruck, Germany) or PTW...
(Freiburg, Germany) is too large (7 mm) to be inserted into urethras or esophagus for an intracavitary use for instance.

IVD is also provided by luminescence dosimetry techniques involving fiber-coupled organic scintillators [3]-[4], doped silica glass [5] or carbon-doped aluminum oxide (Al2O3:C) crystals [6]-[7]. They are all plagued with light perturbations (so-called “stem effect”) due to Cerenkov and scintillation processes that occur within the light guide [8]. Since this amount of stem light is not controlled, it must be removed from the useful luminescent signal. With optical fibers (refractive index ~ 1.5), the Cerenkov effect occurs for electron energies higher than 180 keV and is therefore ubiquitous in any treatments involving LINACs.

As far as low-frequency pulsed sources are concerned, the time-discrimination (or time-resolved gating) method provides an efficient way to get rid of the stem effect since its decay time is usually less than 1 µs in PMMA and silica fibers [8]. However, this method is difficult to implement with short-lived scintillators (< 10 ns), e.g. plastic scintillators. The Radioluminescence (RL) from Al2O3:C crystals also features a "fast" component (330 nm, decay time less than 7 ns) associated to F+-center [9] that cannot be distinguished from the stem effect. Fortunately, the dominant RL component of Al2O3:C is a “slow” one (410 nm, decay time ~ 33 ns) associated to F-centers. Most LINACs used in Medical Physics operate at Pulse Repetition Rates (PRR) in the range [100 Hz - 300 Hz] and each pulse lasts several microseconds. Therefore, the slow RL component of Al2O3:C crystals persists long after the LINAC pulse and is easily discriminated against stem light.

Most time-discrimination demonstrations [5]-[7] involve simple, medium bandpass (MHz) and low-cost transistor-based electronics. They are triggered by the gate synchronization signal of the LINAC, provided early before the pulse is emitted in order to efficiently switch off the perturbation. However, access to the LINAC electronics is rarely allowed in hospitals for safety or conformity reasons. Recently, another discrimination detection scheme made use of a fiber-optic-coupled scintillator that detects ambient scattered radiation [10]-[11] to remove the stem light from the luminescence of a copper-doped fused quartz fiber (RL decay times ~ 52 µs and 104 µs). The RL reader operates in an autonomous way regardless of LINAC electronics thanks to an additional fast detection unit (e.g. photo-multiplier) that provides a gating signal in phase with LINAC pulses.

Dosimetric-grade Al2O3:C crystals provide both active (real-time) and integrator modes of operation. During irradiation, the radioluminescence (RL) spontaneously emitted by Al2O3:C crystals may be monitored to provide real-time estimation of the accumulated dose. Al2O3:C crystals usually exhibit higher light yields than organic scintillators [12] and so small volumes (< mm²) may be used in the purpose of highly spatially accurate IVD. However, as OSL material, the RL behavior of a Al2O3:C crystal is strongly dependent on trap concentrations (dosimetric and deep traps) owing to charge transfer and retrapping. This has two important consequences.

First, pristine crystals are usually pre-irradiated before use, in order to fill deep traps. Once filled up, electron occupancy within deep traps reaches a state of equilibrium between the amount of charges brought and released by irradiation (i.e. photoelectric and Compton effects) and those released by light, as recently shown by Damkjaer et al. [13].

Second, the estimation of the dose rate from the luminescent signal is not straightforward as the RL sensitivity of Al2O3:C crystals is strongly dose-dependent. Indeed, as irradiation advances, the concentration of trapped electrons increases and the RL signal increases accordingly. This dose-dependency is usually considered as a pernicious effect compromising its use as real-time dosimeter. In this work, we show that this may be easily overcome by the use of a convenient algorithm that directly provides the accumulated dose from which the dose rate may be derived afterwards if necessary.

A previous algorithm was proposed by Andersen et al. to correct for sensitivity changes of Al2O3:C [7]. This algorithm processes iteratively on dose increments ΔD as irradiation advances assuming that the RL sensitivity only depends on dose. Actually, the RL signal depends both on dose and dose rate and so this previous algorithm lacks to take into account the dose rate explicitly. In this paper, we describe an original, integral-based, algorithm in the purpose of retrieving the accumulated dose from the integral of the RL of Al2O3:C crystals. It is easy to use, performs well under a large range of dose rate values, and processes continuously. It is tested in reference conditions with 12-MV photon beams from a Saturne 43 LINAC, simulating EBRT treatments.

Following the demonstration of Tanyi et al. [10]-[11], we implemented a time-discrimination method involving a logic gate (inserted into the RL-OSL reader) and a dedicated discriminating unit that detects ambient scattered radiation in the irradiation room, next to the LINAC. This configuration enables our RL reader to work in an autonomous way, eliminating the need to access to the LINAC control desk.

II. THEORY

The kinetic model of Pagonis et al. provides theoretical grounds for understanding of the RL behavior in Al2O3:C [14]. In this model, two electron trapping states (dosimetric and deep traps) and two recombination hole centers (radiative and non-radiative) are involved. Dosimetric traps are bleached by light whereas deep traps are not. Pagonis et al. did not take into account shallow traps (i.e. low-energy traps) and also made the assumption that deep traps are empty (i.e. the material was previously annealed at high temperature). Following these authors, we note M₁ and M₂ as the concentrations of radiative and non-radiative hole centers respectively (with instantaneous occupancy m₁ and m₂ and trapping probability coefficients B₁ and B₂), N₁ and N₂ the concentrations of dosimetric and deep traps (with instantaneous occupancy n₁ and n₂) respectively.

However, our experimental conditions do not match previous assumptions. Since alumina crystals are pre-irradiated before
use, deep traps are filled and consequently the value of \( n_{20} \) is presumably close to \( N_2 \) (saturation) while other traps are considered as nearly empty. Moreover, it is worthwhile noticing that the RL behavior also depends on predose [15]. As a consequence, we consider the following initial conditions instead (at time \( t = 0 \)): \( m_{10} \ll M_1 \), \( m_{20} = 0 \), \( n_{10} \sim N_2 \), \( n_{10} = 0 \).

The RL light arises from recombination of free electrons traveling within the conduction band (CB) onto radiative recombination centers \( M_1 \) and is given by

\[
RL(t) \propto A_{n_1}m_1n_1
\]  

(1)

where \( n_1 \) is the concentration of electrons within CB released at the rate of production of electron-hole pairs \( X \) (proportional to dose rate) and \( A_{n_1} \) is the recombination probability coefficient on radiative hole centers. Expressions for \( m_1 \) and \( n_1 \) may be found in [14].

After simplification (granted initial conditions), one may find that the RL is ruled by the following time-equation

\[
RL(t) = AX + BX^2t
\]  

(2)

where the coefficients \( A \) and \( B \) are given by

\[
A = \frac{A_{n_1}m_{10}}{A_{n_1}N_1} \quad ; \quad B = \frac{A_f}{D_s}
\]  

(3)

where \( A_{n_1} \) is the trapping probability coefficient onto dosimetric trap \( N_1 \) and \( D_s \) is a specific dose value (in Gray) that mainly depends on \( m_{10} \) according to

\[
D_s = Cm_{10}\left(1 + \frac{B_sM_1}{B_1M_1}\right)
\]  

(4)

where \( C \) is an experimental dose parameter \( (J.m^2.kg^{-1}). \)

Eq (2) shows that the experimental behavior of RL in Al\(_2\)O\(_3\):C may be explained by usual rate equations. Since the electron concentration \( n_1 \) in CB is proportional to dose rate while the occupancy \( n_1 \) is proportional to accumulated dose (prior to saturation), Equation 2 may be rewritten to yield the general form

\[
RL(t) = \alpha . D(t) + \beta . D(t) . D(t)
\]  

(5)

where \( D(t) \) is the dose rate, \( D(t) \) is the accumulated dose since previous laser reset, \( \alpha \) (Cts/Gy) and \( \beta \) (Cts/Gy\(^2\)) are calibration parameters.

Equation (5) may also be written under an integral form as

\[
I(t) = \int_0^t RL(\tau) d\tau = \alpha . D(t) + \frac{\beta}{2} . D(t)^2
\]  

(6)

This equation is applicable up to a dose of about 7 Gy for the crystals tested (Landauer Inc.). For higher dose, a third-order term is used to account for saturation of the dose response. \( D(t) \) is then calculated by solving equation (6), as follows

\[
D(t) = D_s\left(-1 + \sqrt{1 + \frac{2 \beta}{\alpha^2} J(t)}\right)
\]  

(7)

where \( D_s \) is a specific dose value, related to calibration parameters by

\[
D_s = \frac{A}{B} = \frac{\alpha}{\beta}
\]  

(8)

For small values of \( I(t)/\alpha D \), with respect to unity, Equation (7) reduces to

\[
D(t) \approx I(t)/\alpha
\]  

(9)

Conversely, for high values of \( I(t)/\alpha D \) with respect to unity, Equation (7) reduces to

\[
D(t) \approx \sqrt{2I(t)/\beta}
\]  

(10)

For early irradiation times \((D(t) < D_s)\), only the \( \alpha \)-coefficient matters while the \( \beta \)-coefficient takes on for longer times \((D(t) > D_s)\).

Once the dose data are calculated by Equation (7), the dose rate data are estimated using Equation (5), to yield

\[
D(t) = \frac{RL(t)}{\alpha + \beta . D(t)}
\]  

(11)

The calibration of the RL signal is usually done at constant dose rate \( D \) (i.e. step profile). In this case, the equation (5) reduces to

\[
RL(t) = \alpha . D + \beta \left(D/t\right)^2
\]  

(12)
III. EXPERIMENT

A. Experimental scheme

The RL/OSL sensor used for the demonstration was already used in an earlier study [16]. It consists of a polymer package rigidly fixed onto flexible opaque tubing that protects a small alumina crystal (~ 1 mm$^3$) affixed on the extremity of a silica optical fiber (SpecTran HCP600, $\Theta = 0.6$ mm) that carries the light from the sensor up to the reader placed in the control room. The Al$_2$O$_3$:C crystals used in this study were purchased from Landauer Inc. [17]. The sensor was predosed (~ 250 Gy) so as to fill deep traps and to stabilize the dose response.

The scheme of the RL-OSL reader is depicted in fig. 1. It is essentially the same as the one already described in an earlier work [18] except that a logic gate is inserted in-between the amplifier-discriminator (A-D) and the counter. This logic gate is a simple bipolar (NPN) transistor (BC 546) that inhibits the transmission of the pulses exiting the A-D towards the counter when the input gating signal is low and let them through when the input gating signal is high (base-emitter forward-biased).

After each irradiation and RL recording, the sensor is stimulated by laser light (Diode-pumped solid-state DPSS @ 532 nm) to empty dosimetric traps. The OSL produced is recorded on-line (i.e. without disconnecting the sensor) and provides absorbed dose data that are compared to reference dose data provided by the IC. The OSL/FO sensor is then reused for another irradiation.

The input gating signal serves to trigger the logic gate and to disable the acquisition during the emission of the pulse. A gating signal is already available from the control desk of the LINAC of the CEA-LNHB. In hospitals however, access to the control desk is restricted due to security/conformity reasons. Therefore, following [10]-[11], we developed and tested an independent discriminating unit associated to a fiber-coupled BGO scintillator (Bismuth Germanate, length: 10 mm, surface: 1.5 x 1.5 mm$^2$) placed next to the LINAC (but away from the patient) as shown in Fig. 3.

The ratio of ambient dose rate vs direct dose rate is less than $10^{-3}$ (~ mGy/min). The light from the BGO scintillator is converted by the discriminating unit into a TTL signal, synchronous with the LINAC pulse pattern, eventually sent to the logic gate. BGO was chosen on account of its high density (7.13 g.cm$^{-3}$) resulting in a small-size detector. The decay time of the BGO luminescence is about 0.3 µs, lower than the pulse duration of the LINAC (several µs). Its peak wavelength is 480 nm, thus compatible with the multialkali photocathode of the R928 PhotoMultiplier Tube (PMT, Hamamatsu) used in the discriminating unit. The BGO sensor was packaged within a brass cylinder (external diameter: 12 mm, length: 30 mm) that provides electronic equilibrium (thickness ~ 3 mm for a 12-MV photon beam), light tightness and mechanical connection to a fiber-optic cable (3M TECS48, $\Theta = 1$ mm, length = 20 meters).
B. Time discrimination of stem effect

The electronic layout of the discriminating unit is depicted in fig. 4.

![Diagram of the discriminating unit](image)

The light from the BGO scintillator is collected by the fiber and carried in front of the photocathode of the R928 PMT. A high voltage (1 kV) is applied to the PMT in negative polarity (anode earthed, cathode at high negative potential), loaded with 56-Ohm. The PMT provides current amplification up to \(10^6\) over a 200-MHz bandwidth (i.e., 5 ns full width at half-maximum (FWHM)), the pulse voltage is \(-80\) mV. A capacity isolates the measuring circuit from the high voltage and transmits only the pulses (high-pass filter) that are sent into an inverter amplifier (gain = -27.5) based on a high-bandwidth operational amplifier (Intersil EL8201). To avoid noise triggering, the pulses are then low-pass filtered by another capacitor (47 nF) providing a time constant of 4.7 \(\mu\)s. Consequently, only a bunch of pulses is able to build up a useful trigger signal. The other utility of the low-pass filter is to shift in time (by a time delay of about 7 \(\mu\)s) the trigger signal with respect to the LINAC pulse. Indeed, the LINAC pulse pattern may be poorly defined. For instance, the pulse pattern of the Saturne 43 LINAC of the CEA-LNHB features a smaller pre-pulse (occurring several microseconds before the real LINAC pulse) likely to randomly trigger the gate (according to detection threshold). Therefore, the value of the capacitor also has an impact on the reliability of the discrimination process since it must be high enough to ensure that the gate signal does not transit to high value before the LINAC pulse ends. In our case, since the LINAC pulse lasts 4 \(\mu\)s, the logic gate is thus activated 11 \(\mu\)s after the onset of the LINAC pulse, as confirmed from DPO recordings (Digital Phosphor Oscilloscope Tektronix TDS3014B, fig. 5). This time shift has no significant impact on RL detection since the decay time of Al\(_2\)O\(_3\)::C is 33 ms.

The resulting signal is then sent through a voltage follower to a comparator (Texas Instruments TLY 3501) whose output is connected to the falling edge triggered input of a monostable multivibrator (Texas Instruments SN 74221). The comparator output is high whenever the input signal exceeds a threshold voltage set to 90 mV. At the end of the LINAC pulse, the low-pass filtered signal returns to zero, thus triggering the monostable device and setting the logic gate output to high. It is kept high for a time delay of 2.46 ms, adjusted by a RC-circuit (\(R = 15\) kOhm, \(C = 235\) nF), chosen as surface-mounted devices on account of their temperature stability. The duty factor of the discriminating unit is then either 24.6 % at 12 MV/20 MV (100 Hz) or 49.2 % at 6 MV (200 Hz).

![Diagram of the discriminating unit](image)

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It is worth noticing that the electronic circuit is powered by unipolar (0-5 V) power supply and operational amplifiers are biased in balanced configuration. Finally, the low-pass filter is a simple passive circuit but active filter circuits could have been used instead.

C. Influence of the discrimination circuit on the RL signal

The RL signal was recorded in similar conditions with gating ("gating ON") and without ("gating OFF"). The fig. 6 shows the RL signals obtained in both cases.

![Diagram of the discrimination circuit](image)

Fig. 6. Inlluence of the gating circuit on the RL signal (12-MV photon beams, PRR = 104 Hz, duty factor = 0.256) for a dose rate of about 200 MU/min. Sampling rate is 10 Hz.
As expected, when gating is on, roughly ¼ of the RL signal is actually recorded on account of the duty factor (0.256 for 12-MV photon beams under a PRR of 104 Hz). The raw time-gated RL signal corrected for duty factor influence (i.e., multiplied by 1/0.256) is found parallel to the RL signal without gating (i.e., with stem effect). The difference between both signals corresponds to a fairly large amount of discriminated stem signal (about 520 cts/0.1 s, i.e., 15% of the integrated RL at 200 UM/min). It is worth noticing that both slopes are similar (the RL curves are parallel to each other, as expected since the stem effect is proportional to dose rate).

The RL signal shown in fig. 6 is split in two contributions, a constant term proportional to dose rate and another one, function of both dose and dose rate as described by Eq. (5).

The analysis of the RL signal shows a transient behavior before it reaches permanent state (Fig. 7). It is partly due to the LINAC itself and to electron trapping by shallow traps [19], also visible at the end of the irradiation when the RL signal decays back to zero (fig. 6). From the recording of Cerenkov light from a blank fiber (without crystal), a risetime of ~0.3 s (at 90%) is measured for LINAC emission.

The evolution of the transient signal is tentatively adjusted by the following relation:

$$RL(t) = \alpha' \cdot D + (\alpha - \alpha' + \beta \cdot D_t) \left[ 1 - \exp\left( -t/\tau \right) \right] \cdot D$$  \hspace{1cm} (13)

where $\alpha' \cdot D \sim 8000 \text{ cts/s}$, $\alpha \cdot D \sim 13776 \text{ cts/s}$ and $\beta \cdot D \sim 19726 \text{ cts.Gy}^{-1}.\text{s}^{-1}$ for a dose rate of 0.0295 Gy/s. The time constant $\tau \sim 0.8$ s.

Although $\alpha'$ is poorly determined, one can see that for time $t > 3. \tau \sim 2.5$ s, equation (13) reduces to (12).

IV. CALIBRATIONS

Reference dose data are usually given in Monitor Units (MU). For the sake of a real-time experiment, the LINAC “scope” output voltage (available from the control desk) was recorded during irradiation with the help of the DPO (Tektronix TDS3014B). The “scope” voltage is proportional to the dose rate within the LINAC head and was calibrated with respect to dose rate in the water phantom with the help of an ionization chamber (IC NE 2571, $C = 23.347 \text{nF}$, sensitivity = $1.998 \times 10^{-10} \text{ C/MU}$), placed in similar reference conditions. The conversion coefficient is $8.859 \times 10^{3} \text{ Gy/MU}$ under reference conditions and with 12-MV photon beams. The voltage of the IC is obtained by applying the Coulomb law ($V = q/C$). For instance, for a dose of 100 MU (0.8859 Gy), the charge collected is $1.998 \times 10^{8} \text{ C}$ and its voltage is 0.856 V.

A. Calibration of the LINAC "scope" output

The Saturne 43 LINAC usually operates in feedback mode ("Medical Physicist") at the nominal dose rate of 200 MU/min. This mode is more convenient for delivering a constant dose rate. For the experiment, other dose rates than the nominal one were also experimented and in this case, the LINAC operated without feedback. Typical IC and scope voltages are shown in Fig. 8 for a constant dose rate (200 MU/min). The amplitude of the scope voltage was recorded with respect to dose rate in water in reference conditions and yields the linear relationship shown in Fig. 9.

The calibration coefficient is $0.0295 \text{ Gy.s}^{-1}.\text{V}^{-1} \pm 10^{-4}$ in feedback mode (100 Hz). The scope voltage was adjusted so that a value of 1 V corresponds to a dose rate of 200 MU/min. A slight difference is observed when the LINAC operates without feedback. In this case, a scope value of 1 V corresponds to a dose rate of 0.0307 Gy/s (i.e., 4% more) due to a slight increase of both PRR (104 Hz instead of 100 Hz) and duty factor (0.256 instead of 0.246).

Once the scope voltages have been checked with respect to dose rates measured by the IC, the IC was removed from the phantom and only the RL-OSL sensor was immersed in water.
B. Calibration of RL signal with respect to dose rate

The LINAC operated without feedback. The irradiation followed a step profile and the irradiation time was adjusted so as to deliver a constant dose of ~ 2 Gy. The RL signals were recorded for several dose rate values ranging from about 21 MU/min up to 315 MU/min (as displayed in Fig. 10).

As shown in Fig. 11, the constant term grows linearly with dose rate with a coefficient $\alpha = (478 \pm 8) \times 10^3$ Cts/Gy. As expected, according to equation 12, the slope exhibits a linear dependence with the square root of the dose rate according to a coefficient $\beta \approx 820 \pm 10$ Cts/$\sqrt{\text{Gy}}$, from which we get the following value for the $\beta$-coefficient = $(672 \pm 17) \times 10^3$ Cts/Gy$^2$.

Finally, the specific dose value $D_S$ is $\sim 0.71$ Gy $\pm 0.03$ Gy for the Al$_2$O$_3$:C crystals tested.

C. Calibration of RL signal with respect to dose

The LINAC operated in the "Medical Physicist" mode (with feedback). Similarly, the RL signals were recorded for several doses (by changing the irradiation time), under a constant dose rate (step profile), as displayed in Fig. 12.

This mode of operation provides a double check of the calibration values $\alpha$ and $\beta$. However, one may argue that the integration of the experimental RL signal is not exactly equivalent to the integration of equation (12). Indeed, it is slightly underestimated on account of the transient RL behavior depicted in figure 7, that also happens on falling edge of the RL at the end of irradiation. However, in the present situation, it is not recorded (as the logic gate is turned to low value), and therefore cannot compensate for the loss of RL signal occurring at the beginning of irradiation.

Let $I_{\text{th}}$ and $I_{\text{exp}}$ be respectively the integrals of equations (12) and (13) (from $t = 0$ to $\infty$), one can find that $I_{\text{exp}}$ may be corrected for the influence of shallow traps as follows:

$$I_{\text{exp}} \approx I_{\text{exp}} + \left( \alpha - \alpha' \right) D(0) \tau + \beta D(0)^2 \tau^2$$  \hspace{1cm} (14)

At the beginning of irradiation, the accumulated dose is close to zero, so that: $\alpha D(0) = \text{RL}(0)$. Taking into account this assumption, Eq (14) can be written as:

$$I_{\text{th}} \approx I_{\text{exp}} + \left( \frac{\alpha - \alpha'}{\alpha} \right) \text{RL}(0) \tau + \beta \frac{\text{RL}(0)^2}{\alpha^2} \tau^2$$  \hspace{1cm} (15)

The value for RL(0) is actually recorded several seconds after onset on LINAC emission. Eq (15) accounts well for the observed discrepancy, predominant for short irradiation times. For instance, the signal loss is about 5000 cts (at 200 MU/min), i.e. 0.7% of the RL integral at 100 MU. Finally, $I_{\text{exp}}$ was plotted with respect to dose in Fig. 13.
The experimental data were then adjusted by Equation (6) with the values of $\alpha$ and $\beta$ previously determined and corrected for shallow trap influence (eq (15)). The residuals between experimental and theoretical data (using Eq (6)) are plotted on the upper part of the graph. A deviation of ±2% is observed between experiment and theory for small dose values as expected due to counting statistics while the deviation is less than ±1% for usual dose fractions encountered in EBRT (~1 Gy to 2 Gy). This second mode of operation demonstrates the consistency of the algorithm as it performs well in both cases (variable or constant dose rate).

Finally, the ability of the algorithm to predict the dose rate from the RL signal was tested. The RL signals shown in Fig. 13 were corrected for dose-dependency using Equation (11) and the dose rate data retrieved by this method are compared to the expected dose rate value (i.e. 0.0295 Gy/s) on Fig. 14. The uncertainty is about ±1% (for 1 s sampling time) and the statistical uncertainty improves as RL signal grows. As expected, the dose rate is slightly underestimated at early stage of irradiation due to electron retrapping by shallow traps. However, this is not detrimental for a medical use since most radiation therapy treatments actually last several minutes or so.

![Fig 14. Calculation of the dose rate from the RL data, corrected for dose-dependency using Equation (11) and using the same calibration coefficients as in Fig. 13. Sampling rate is 1 Hz.](image)

**D. Calibration of OSL signal with respect to dose**

The RL-OSL sensor also provides an OSL dose measurement in addition to both scope and MU values given by the LINAC software. The OSL were also recorded with respect to dose during the same set of experiment in "Medical Physicist" mode (i.e. calibration of RL signal with respect to dose) and shown in Fig. 15. After background subtraction, the OSL signals were integrated and the result is plotted with respect to dose in the inset of Fig. 15.

The dose response of Al$_2$O$_3$:C crystals follows a second-order polynomial equation according to [16]:

$$D(Gy) = D_m \left(1 - \sqrt{1 - \frac{2\text{OSL}}{D_m s}}\right)$$  \hspace{1cm} (16)

where OSL is the integrated OSL signal and $D_m$ is a crystal-dependent dose parameter ($D_m = 13.67 \text{ Gy}$ [16]).

In this experiment, the slope $s$ was $5.1 \times 10^6 \text{ cts/Gy}$ and the uncertainty in OSL dose measurement is typically ±1% [18].

![Fig 15. Dose calibration of the OSL signal (sampling rate: 1 Hz). Same experiment as Fig. 12.](image)

**V. DOSE AND DOSE RATE MONITORING IN ARBITRARY CASE**

In real medical configuration, dose and dose rates are likely to change depending on treatment configuration, e.g. during Intensity-Modulated Radiation Therapy (IMRT) with Multi-Leaf Collimators (MLC). The algorithm was therefore tested for arbitrary dose rate profiles. A set of 6 experiments was performed as described in Table 1. The LINAC operated without feedback, manually controlled from the control desk (potentiometer). Fig. 16 shows the raw RL signals recorded at sampling rate of 10 Hz. RL signals were then run-averaged at 1-s sampling time and for each profile, dose and dose rate data were calculated using Equations (7) and (11) respectively. Reference dose and dose rate profiles were also calculated from the scope voltage and displayed for comparison. Fig. 17 compares experimental dose profiles vs reference dose profiles and Fig. 18 compares experimental dose rate profiles vs reference dose rate profiles. The absorbed doses measured by RL and OSL were compared to reference dose from MU values and from integrals of scope voltage (Table 1). The uncertainty in MU and scope values are about ±1% and ±0.5% respectively.

<table>
<thead>
<tr>
<th>Profile</th>
<th>Reference dose (Gy)</th>
<th>Measured dose (Gy)</th>
<th>Deviations vs dose MU (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>From MU</td>
<td>From scope</td>
<td>RL</td>
<td>OSL</td>
</tr>
<tr>
<td>#1</td>
<td>1.59</td>
<td>1.58</td>
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<tr>
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</tr>
<tr>
<td>#6</td>
<td>1.07</td>
<td>1.07</td>
<td>1.08</td>
</tr>
</tbody>
</table>

Tab. 1. Dose rate profiles of six experiments and comparison of absorbed dose data obtained. Data are rounded to two digits after point value. Deviations between total doses (i.e. $[\text{dose}_{\text{MU}} - \text{dose}_{\text{RL}}]/\text{dose}_{\text{MU}}$) are also quoted in Table 1.
Fig 16. Raw RL signals recorded with respect to time for each of the 6 irradiation profiles. Sampling rate is 10 Hz (upper graph: #1, #2 and #3, lower graph: #4, #5, #6).

Fig 17. Accumulated dose with respect to time, as calculated from the integral of RL data (Fig. 16) using equation (7), for each of the 6 irradiation profiles (dots). The $\alpha$ and $\beta$ values are respectively about $4.1 \times 10^3$ Cts/Gy and $6.68 \times 10^3$ Cts/Gy. Also shown is the reference dose calculated from the integral of scope voltage (continuous lines). Sampling rate is 1 Hz.

Fig 18. Dose rate with respect to time, as calculated from RL data (Fig. 16) using equation (11), for each of the 6 irradiation profiles (dots). Also shown is the reference dose rate calculated from the scope voltage (continuous lines). Sampling rate is 1 Hz.

The relative uncertainties of both RL and OSL dose measurements are respectively about $\pm 2\%$ and $\pm 1\%$. OSL measurements are more accurate than RL measurements. This might be due to the large difference in the integrals. For instance, the OSL integral is about $4.1 \times 10^6$ cts for 100 MU whereas the RL integral barely amounts one fourth of this value ($\sim 0.8 \times 10^6$ cts) for the same MU value. Therefore, it is no surprise that the expected experimental uncertainty due to counting statistics of RL measurements is less than that of OSL.

VI. CONCLUSION

An original algorithm for IVD accurately dealing with the dose-dependency of the RL of dosimetric-grade alumina crystals ($\text{Al}_2\text{O}_3$:C) is described and tested under constant and arbitrary dose rate conditions with 12-MV LINAC photon beams, simulating EBRT treatments.

The rate-equation model [14] accounts well for the time-equation of the RL signal and was adapted to our experimental conditions. It involves two calibration parameters ($\alpha$ and $\beta$) that rule the luminescence of $\text{Al}_2\text{O}_3$:C, respectively related to scintillation and dose-dependent part of the RL. The ratio $\alpha/\beta$ is a specific dose value $D_s$ ($\sim 0.71$ Gy) that is presumably attributed to initial occupancy of radiative hole centers. Practically, it serves as a criterion distinguishing prominence of each RL contribution (scintillation dominates for $D(t) < D_s$, while the dose-dependent RL part dominates for $D(t) > D_s$).

This algorithm directly provides the accumulated dose at any time during irradiation from the integral of the RL data (it is worth reminding that the main parameter of interest for the medical physicist is the accumulated dose rather than the dose rate). The dose rate is inferred afterwards from RL data using a dose-dependent coefficient. After irradiation, the $\text{Al}_2\text{O}_3$:C crystal is reset by laser light and the stimulated OSL is also recorded to provide additional dose data, compared to Monitor Units values.

As proof-of-principle experiment, irradiations of a fiber-coupled RL-sensor were performed under reference conditions in a water phantom. The large field size ($10 \times 10$ cm$^2$) produces a large amount ($\sim 15\%$ of the integrated RL at 200 UM/min) of Cerenkov radiation and scintillation in the fiber that superimposes over the useful RL signal (so called "stem effect"). Fortunately, the beam size is smaller in most medical situations, making this configuration conservative. The stem light is removed with the help of a logic gate inserted within the RL-OSL reader, activated by a trigger signal in phase with LINAC pulses. The trigger signal is provided by a dedicated discriminating unit that detects the light from a fiber-coupled BGO scintillator placed next to the LINAC. This configuration enables our RL fiber optic reader to work in an autonomous way, eliminating the need to access to the LINAC control desk often unavailable in hospitals due to safety/conformity reasons. Since a time delay of 7 $\mu$s is used (for a LINAC pulse of 4 $\mu$s) and at least several microseconds are required for the measurement, the maximum PRR allowed is thus of the order of 10 kHz or so with this setup. It may thus be used for a large
panel of LINACs (especially those used for Medical Physics) except quasi-CW ones.

The algorithm was first calibrated with step irradiation profiles. The RL-sensor was first calibrated with respect to dose rate (the dose being kept constant). Although this calibration is already self-sufficient (providing both $\alpha$ and $\beta$ coefficients), a complementary calibration of the RL signal is proposed with respect to dose (at constant dose rate), based on the integral of the RL signal, corrected from shallow trap influence. Both calibration procedures lead to similar results and practically, the correction for shallow trap influence may be neglected since it is often less than measurement uncertainty.

The dose rate may be recovered after dose calculation, and we show that the uncertainty is about $\pm 1\%$ (for 1 s sampling rate). It is slightly under-estimated during the first seconds of irradiation due to electron retrapping by shallow traps (time constant $\sim 0.8$ s at room temperature). However, in practice, this is not detrimental for a medical use since most radiation therapy treatments actually last several minutes or so.

Finally, the algorithm was tested using six different dose rate profiles, manually operated from the LINAC control desk. For each profile, dose and dose rate data were calculated from RL signals using the values $\alpha$ and $\beta$ obtained by calibration. Reference dose and dose rate profiles were also calculated from the scope voltage and displayed for comparison. Finally, the absorbed doses measured by RL and OSL were compared to dose calculated from MU values and deviations lies within $\pm 1\%$ for OSL and within $\pm 2\%$ for RL.

This work demonstrates the reliability of this integral-based algorithm that performs well for any profile (step or arbitrary) and a wide range of dose rates. Although the calculation was done off-line, it is amenable to a real-time processing during irradiation. For the sake of demonstration, only one sensor was used but this measurement protocol may be extended to a plurality of sensors (e.g. a dosimetric catheter including a chain of $\mathrm{Al}_2\mathrm{O}_3$:C crystals for intracavitary IVD [20]), connected to a multichannel RL-OSL/FO reader.

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REFERENCES