Feasibility of using a dose-area product ratio as beam quality specifier for photon beams with small field sizes

Maria Pimpinella, Claudio Caporali, Antonio Stefano Guerra, Luca Silvi, Vanessa de Coste, Assunta Petrucci, Franck Delaunay, Stéphane Dufreneix, Jean Gouriou, Aimé Ostrowsky, et al.

Feasibility of using a dose-area product ratio as beam quality specifier for photon beams with small field sizes

Maria Pimpinella[a,*], Claudio Caporali[a], Antonio Stefano Guerra[a], Luca Silvi[a], Vanessa De Coste[a], Assunta Petrucci[b], Frank Delaunay[c], Stéphane Dufreneix[c], Jean Gouriou[c], Aimé Ostrowsky[c], Benjamin Rapp[c], Jean-Marc Bordy[c], Josiane Daures[c], Maïwenn Le Roy[c], Line Sommier[c], Didier Vermesse[c]

[a] *Istituto Nazionale di Metrologia delle Radiazioni Ionizzanti, ENEA-INMRI, I-00123 Roma, Italy*
[b] *S. Filippo Neri Hospital, UOSD Fisica Sanitaria, I-00135 Roma, Italy*
[c] *CEA, LIST, Laboratoire National Henri Becquerel (LNE-LNHB), F-91191 Gif-sur-Yvette, France*

Purpose: To investigate the feasibility of using the ratio of dose-area product at 20 cm and 10 cm water depths ($DAPR_{20,10}$) as a beam quality specifier for radiotherapy photon beams with field diameter below 2 cm. *Methods:* Dose-area product was determined as the integral of absorbed dose to water (D_w) over a surface larger than the beam size. 6 MV and 10 MV photon beams with field diameters from 0.75 cm to 2 cm were considered. Monte Carlo (MC) simulations were performed to calculate energy-dependent dosimetric parameters and to study the $DAPR_{20,10}$ properties. Aspects relevant to $DAPR_{20,10}$ measurement were explored using large-area plane-parallel ionization chambers with different diameters.

Results: $DAPR_{20,10}$ was nearly independent of field size in line with the small differences among the corre-sponding mean beam energies. Both MC and experimental results showed a dependence of $DAPR_{20,10}$ on the measurement setup and the surface over which D_w is integrated. For a given setup, $DAPR_{20,10}$ values obtained using ionization chambers with different air-cavity diameters agreed with one another within 0.4%, after the application of MC correction factors accounting for effects due to the chamber size. $DAPR_{20,10}$ differences among the small field sizes were within 1% and sensitivity to the beam energy resulted similar to that of established beam quality specifiers based on the point measurement of D_w.

Conclusions: For a specific measurement setup and integration area, $DAPR_{20,10}$ proved suitable to specify the beam quality of small photon beams for the selection of energy-dependent dosimetric parameters.

1. Introduction

In recent years, the use of small beams (field sizes smaller than 2 cm × 2 cm) in routine radiotherapy techniques has increased steadily. Nevertheless, small beam dosimetry is still challenging. The determination of absorbed dose to water, D_w, in narrow photon beams is particularly demanding, if the traditional approach of measuring D_w with a point-like detector placed on the beam axis is followed. Even the use of high resolution detectors with sensitive volume of the order of tenths of mm^3 or less does not ensure a reliable D_w measurement in the absence of lateral electronic equilibrium [1]. When used in small field sizes, point-like detectors can exhibit large response variations (even more than 10%) depending on the detector material and construction details near the sensitive volume. These variations generally result in underestimation (in the case of small volume ionization chambers) or overestimation (in the case of solid state detectors) of both D_w and output factors [2,3]. As a consequence detector specific correction factors [4] are required for accurate D_w measurement in small beams. Previous work in this field has focused on the evaluation of such correction factors, either using direct Monte Carlo calculation or, experimentally, taking a given detector as reference, and results for the most widely used detectors have been reported in literature [1,5–14]. However, as no D_w primary standards exist for field sizes smaller than 2 cm, discrepancies among published data are difficult to solve [15,16]. Moreover, the positioning of point-like detectors in narrow beams is also very critical for the measurement accuracy, since errors larger than 1% can occur even for uncertainties on the detector position as low as a few tenths of mm [17].

* Corresponding author at: Istituto Nazionale di Metrologia delle Radiazioni Ionizzanti, ENEA-INMRI CR Casaccia, Via Anguillarese 301, 00123 Roma, Italy.
E-mail address: maria.pimpinella@enea.it (M. Pimpinella).

The above difficulties have raised interest in a different approach, based on measuring an integral quantity as reference quantity for small beam dosimetry, in analogy with the concept of dose-area product used for measurements in free space in diagnostic radiology [18], and extending the concept to measurements performed in a material medium like in a water phantom [19–21]. For radiotherapy dosimetry application, the dose-area product (*DAP*) is defined as:

$$DAP = \int_A D_w(x,y)\,dxdy \tag{1}$$

where A is an area, in a plane perpendicular to the beam central axis, larger than the beam size at that plane, and corresponding to the active area of the detector used for the *DAP* measurement. A proper *DAP* detector should have a flat sensitive volume with cross-sectional area larger than the radiation field. Large-area plane-parallel ionization chambers (LACs) have been shown to be adequate *DAP* detectors [22,23]. In very small field sizes, positioning a *DAP* detector on the beam central axis is less critical than positioning a point-like detector. In addition, measurement of the integral dose is expected to be less detector dependent, if compared with the point-dose measurement by point-like detectors [24]. In fact, the latter requires corrections that strongly dependent on beam shape, detector type, and off-axis position in the small field. Conversely, even in the case of a composite clinical field, Monte Carlo calculations in [24] showed that differences in response among point-like detectors substantially diminish, if the detector signal is integrated over the whole radiation field. The Laboratoire National Henri Becquerel (LNE-LNHB) recently developed a calorimeter for absolute measurement of *DAP* in small field sizes, making this quantity available for transfer from the calibration laboratory to the user's beam [25,26]. Then, in the scenario of a small beam dosimetry based on *DAP* references, defining the beam quality specifier in terms of DAP to link the calibration to the user's beam becomes an attractive possibility.

In the present paper, the feasibility of expressing the photon beam quality in terms of a *DAP* ratio is explored for field diameters below 2 cm. Specifically the ratio of *DAP* at 20 cm and 10 cm water depths

$$DAPR_{20,10} = \frac{\int_A D_{w,20cm}(x,y)\,dxdy}{\int_A D_{w,10cm}(x,y)\,dxdy} \tag{2}$$

is considered in analogy with the traditional $TPR_{20,10}$ beam quality index [27] based on point-dose measurement. We thoroughly investigated the properties of $DAPR_{20,10}$ in 6 MV and 10 MV small photon beams both by Monte Carlo calculation and experimentally, using LACs with different air-cavity diameters and characteristics. Two types of Linacs with different collimator systems were used. The aim of this work was: a) to verify the ability of $DAPR_{20,10}$ to discriminate between qualities of small beams for the purpose of selecting energy-dependent dosimetric data (i.e. ionization chamber calibration coefficient, correction factors); b) to establish appropriate measurement conditions and procedures for the experimental determination of $DAPR_{20,10}$ as a beam quality specifier.

2. Materials and methods

Monte Carlo simulations of 6 MV and 10 MV clinical photon beams were performed in order to investigate the dependence of $DAPR_{20,10}$ on beam energy and field size. Moreover, Monte Carlo calculation was applied to evaluate the influence on $DAPR_{20,10}$ of the area over which *DAP* is integrated (i.e. the detector active area). Measurement setups with fixed source-to-surface distance (SSD) or with fixed source-to-detector distance (SDD) were considered. Additionally, the water-to-air stopping power ratio, $s_{w,air}$, the most important energy-dependent parameter affecting ionization chamber response, was calculated at reference depth as a function of the beam energy and field size, to assess whether the $s_{w,air}$ values are correlated with the corresponding $DAPR_{20,10}$ values. Finally, ratios of ionization signals at 20 cm and 10 cm water depths were measured under various experimental conditions (beam energies, field sizes and measurement setups) by means of LACs with different active areas, and experimental results were compared to those obtained by Monte Carlo calculation.

2.1. Accelerators and photon beams

Accelerators used in this work were a Varian DHX clinical accelerator available at San Filippo Neri Hospital in Rome and a General-Electric (GE) Saturne 43 clinical accelerator at LNE-LNHB. Since reproducibility of jaw positioning was not good enough for small beams (in some cases measurement reproducibility was larger than 1%), only beams shaped by fixed cones were considered for *DAPR* measurement.

The Varian DHX accelerator produces 6 MV and 10 MV photon beams and it is equipped with Radionics stereotactic collimators. These are tapered conical collimators using Cerrobend (27% lead, 50% bismuth, 13% tin and 10% cadmium) as collimating material. A Cerrobend cylinder with central conical opening is inserted into a stainless steel cylindrical housing with length of 12.5 cm and outer diameter of 7.5 cm. Using such cones and a constant 7 cm × 7 cm secondary collimator (e.g. linac jaws) setting, circular beams with diameters of 2.00 cm, 1.50 cm and 1.25 cm at the isocenter are produced. The beams shaped by the stereotactic collimators were used for investigating the properties of $DAPR_{20,10}$ by Monte Carlo simulations and measurements.

For the Saturne 43 accelerator, specifically designed external collimators made of tungsten alloy (D185) with a length of 10 cm and a conically-shaped hole were added to produce 6 MV beams with diameters of 2 cm, 1 cm and 0.75 cm at the reference plane. The alignment was checked optically with a telescope. The entry and exit apertures of the collimator had to be centred on the same axis and the radial dose distribution was checked with EBT3 films. Two additional monitor ionization chambers were mounted on the external collimator in front of the beam defined by the linac jaws. For the three small beams, $DAPR_{20,10}$ was experimentally determined setting an SDD of 100 cm and integrating the absorbed dose over a detector surface of 3 cm diameter.

2.2. Monte Carlo simulations

2.2.1. Varian DHX accelerator

The BEAMnrc code [28] of the EGSnrc Monte Carlo system version V4-r2-4 [29] was used for simulating the 6 MV and 10 MV photon beams produced by the Varian DHX accelerator (Fig. 1). First, square photon beams shaped by the jaws were simulated with the purpose of validating the accelerator model by comparing the calculated and measured dose distributions. The mean energy of the initial electron beam was tuned by comparing calculated and measured percentage depth dose (PDD) curves for the 10 cm × 10 cm field size. A circular, Gaussian spatial distribution was assumed for the electron beam incident on the target. The full width at half maximum (FWHM) of the Gaussian distribution was determined by comparing simulated and measured total scatter factors for the 1 cm × 1 cm field size, according to the procedure proposed by Francescon et al. [30]. Then, the 6 MV and 10 MV stereotactic beams shaped by the Radionics cones were simulated and the corresponding phase-space files (PSFs) generated. To extend the range of beam sizes studied, square fields (side 1.6 cm, 1.0 cm, 0.8 cm and 0.5 cm at the isocenter) defined by the linac jaws were also simulated. The BEAMDP program [31] was used to analyse the phase-space files and to derive the photon beam energy spectra.

The values of the EGSnrc simulation parameters are summarized in table 1. For the BEAMnrc simulations, cutoff energies were set to 10 keV for photons (PCUT) and 700 keV for electrons (ECUT, electron rest mass included). The range rejection (RR) and the directional bremsstrahlung splitting (DBS) techniques were applied to improve the calculation efficiency of photon beam simulations [32,33]. The RR

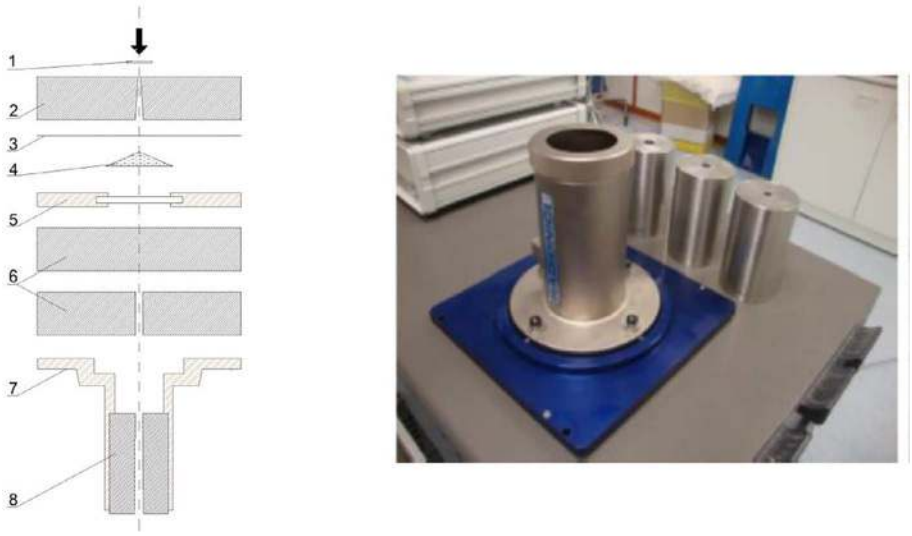

Fig. 1. Sketch of the Varian DHX accelerator model used for the simulation of stereotactic photon beams shaped by Radionics cones used as tertiary collimators: 1- target, 2- static collimators, 3- vacuum window, 4- flattening filter, 5- monitor chamber, 6- jaws, 7- stereotactic cone holder (Aluminum), 8- stereotactic Cerrobend cone. Features of the stereotactic collimators (holder and cones) are shown by the picture on the right.

Table 1
Settings of radiation transport parameters for EGSnrc simulations.

Parameter	Setting value
PCUT (keV)	10
ECUT (keV)	700 (BEAMnrc simulations) 521 (DOSRZnrc, DOSXYZnrc, SPRRZnrc simulations)
Electron step algorithm	PRESTA-II
Boundary crossing algorithm	EXACT
Photon cross sections	XCOM

parameter ESAVE, defined as the threshold energy below which secondary electrons having ranges shorter than the nearest region boundary are stopped, was set to 2 MeV, but RR was not applied in the accelerator target. For the DBS technique, a splitting value of 1000 was used with a splitting field size extending at least 2 cm beyond the beam edge at 100 cm source distance. PSFs were scored in air at 80 cm, 90 cm and 100 cm distance from the target and used as source inputs into the EGSnrc/DOSXYZnrc, EGSnrc/DOSRZnrc and EGSnrc/SPRRZnrc user codes [34] for calculating dose profiles (PDD curves, cross-plane and in-plane profiles), *DAP* and $s_{w,air}$ values, respectively. For these calculations, the simulation parameters were the same as for the BEAMnrc simulations except for the electron cutoff energy which was set to 521 keV (electron rest mass included). To investigate the field size dependency of the beam energy distribution in water, a water phantom was included in the BEAMnrc simulations at a source distance of 90 cm. Phase-space files were generated at 10 cm and 20 cm depths in water, and analysed.

2.2.2. Saturne 43 accelerator

For the Monte Carlo simulation of the GE Saturne 43 beams, two different Monte Carlo codes, EGSnrc [29] and PENELOPE [35], were used. The beam radial anisotropy was measured using EBT3 films and the PDD curves, to be used for verification of the simulation results, were measured using ionization chambers. A PTW 31014, an Exradin A1SL and a homemade plane-parallel ionization chamber were used. The Monte Carlo beam parameters (energy and spot size of the initial electron beam) were defined for the 2 cm beam diameter. Then, the same beam parameters were applied for the 1 cm and 0.75 cm beam diameters and the simulation results compared with measurements. The beam parameters chosen for a parallelized version of PENELOPE 2006 with the MPI library [35,36] and EGSnrc version V4-r2-4 simulations were rather different. For the PENELOPE calculations, the electron energy spectrum was Gaussian (6.25 MeV, standard deviation of 450 keV) and the electrons reached the target uniformly on a disc-shaped focal spot of 1 mm diameter. For the EGSnrc calculations, the electron energy spectrum was not Gaussian but based on a more representative spectrum [37] and the electrons reached the target with a Gaussian spatial distribution (FWHM of 1 mm) and a maximum angular spread around the Z axis of 0.2°. The EGSnrc parameters were almost identical to those described in the previous section, except for the DBS splitting parameter set to 1500. The PENELOPE simulation parameters are summarized in Table 2. The C1 parameter is linked to the average angular deflection produced by multiple elastic scattering along a path length equal to the mean free path between two hard elastic events. The C2 parameter is the maximum average fractional energy loss between two consecutive hard elastic events. The WCC and WCR parameters are the cutoff energy losses for hard inelastic collisions and hard bremsstrahlung emission respectively. DSMAX is the maximum mean free path between two hard elastic events. For variance reduction, oriented splitting for bremsstrahlung events in the target (i.e. when a particle exits a specific area, the particle is split into several equivalent particles distributed around a circle of radius defined by current particle position) and an additional splitting using the cylindrical symmetry before reaching the jaws were used. This is based on the activation of forced bremsstrahlung emission for primary electrons whose direction is within a cone with a specific half angle. When this occurs, the number of secondary bremsstrahlung photons that are emitted from primary electrons is increased. For dose calculations, another splitting is done just before the water-phantom entrance surface.

Table 2
PENELOPE simulation parameters in the accelerator head and in water.

Parameter	Setting value
C1/C2	0.05/0.05
Cutoff energies (keV): electrons / photons / positrons	500/10/500 (accelerator head) 50/10/50 (water phantom)
Wcc/Wcr (keV)	10/10 (accelerator head) 5/5 (water phantom)
DSMAX	1/20th of the smallest dimension for the target 1/10th of the thickness for other elements
Oriented splitting	Splitting number 100 Cone half-angle 4°
Cylindrical symmetry splitting	Splitting number 20
Phantom splitting	Splitting number 20

2.2.3. Calculation of water-to-air stopping power ratios

The EGSnrc/SPRRZnrc user code [34] was applied to calculate $s_{w,air}$ for all the beams used in this work. The SPRRZnrc code calculates $s_{w,air}$ using an *on-the-fly* technique to score the energy deposition in a cavity filled with the transport medium (i.e. water) and then deriving the energy deposition in the cavity when filled with air [34]. Compared to off-line $s_{w,air}$ calculation based on scoring the electron fluence spectrum in water, the *on-the-fly* technique avoids possible effects on the calculation results due to the actual number of energy bins used in the spectrum.

A water phantom with 20 cm radius and 30 cm height was considered and $s_{w,air}$ values were calculated at 10 cm and 20 cm depths in water, using cylindrical scoring regions centred on the beam axis with radii in the range 0.1–5 cm, and a height of 2 mm. Values of $s_{w,air}$ obtained with a scoring region radius of 1 mm are related to D_w point measurement. Scoring regions larger than the stereotactic field sizes were considered more appropriate to evaluate $s_{w,air}$ values related to the *DAP* quantity as defined in this work.

2.2.4. $DAPR_{20,10}$ calculations

Using the EGSnrc/DOSRZnrc user code [34], $DAPR_{20,10}$ values were determined for all the simulated Varian DHX beams as a function of the radius of the surface over which the absorbed dose is integrated. To this aim, *DAP* values were calculated at 10 cm and 20 cm depths in water as a function of the radius of the scoring region. Since the Monte Carlo scoring region corresponds to the detector active area, radii were varied from 1.5 cm to 6 cm, to match the range of radii of the available LACs. Both the SSD setup (i.e. *DAP* at 10 and 20 cm water depths determined with a fixed SSD, moving the chamber) and the SDD setup (i.e. *DAP* at 10 and 20 cm water depths determined with the detector at a fixed distance from the source, moving the phantom) were simulated. SSD values of 80 cm, 90 cm and 100 cm as well as an SDD of 100 cm were considered. $DAPR_{20,10}$ values referring to an integration surface with radius 1.5 cm were also calculated for the GE Saturne 43 6 MV beams with diameters 2 cm, 1 cm and 0.75 cm using both the EGSnrc and PENELOPE codes.

2.3. Measurements

LACs with collecting electrode diameters larger than the field size were used for measuring the ratios of ionization signals at 20 cm and 10 cm depths in water ($M(20)/M(10)$). The $M(20)/M(10)$ ratio represents the $DAPR_{20,10}$ integrated over the chamber active area, if the ionization chamber response in terms of *DAP* does not change with the water depth.

Measurements at the Varian DHX accelerator were made using two ionization chambers: a PTW type 34070 (BP_IC) and a PTW type 7862 (TC_IC) (PTW, Freiburg, Germany). The BP_IC chamber is waterproof and has a collecting electrode diameter of 8.16 cm, an inter-electrode spacing of 2 mm and PMMA entrance and exit windows of 0.4 g cm^{-2} water equivalent thickness. The T_IC chamber is a circular plane-parallel transmission chamber with thin entrance and exit windows (0.028 g cm^{-2} water equivalent thickness). The chamber sensitive volume has a diameter of 9.65 cm and an inter-electrode spacing of 2.4 mm. A PTW Unidos E Universal Dosimeter was used for *DAPR* measurements and a PTW Tandem Dual Channel Electrometer was used for scanning measurements (i.e. lateral beam profiles and depth ionization distributions).

Measurements at the GE Saturne 43 accelerator were made using the following ionization chambers: a BP_IC, a PTW type 34073 (collecting diameter of 3.96 cm) and a homemade plane-parallel ionization chamber (SV-PMMA: collecting diameter of 3 cm, inter-electrode spacing of 2 mm) [38].

The chambers were positioned in a water phantom with their reference point (i.e. the centre of the chamber at the air cavity entrance) at the measurement depth. Since both the TC_IC and the SV-PMMA chambers are not waterproof, a PMMA envelope (0.5 mm thick in front of the chamber entrance window) was used for measurements in water. Signal stability, measurement reproducibility and saturation curves were measured for all the chambers at different depths in water. Corrections for ion recombination and polarity effects were determined and applied to the chamber signal at each measurement depth.

Concerning ion recombination effects, it should be mentioned that when an ionization chamber larger than the beam is used in a linac, volume recombination is dominant in the direct irradiation field, but near the collecting electrode edge, initial recombination prevails. Examination of the Boag's theory [39] shows that the two-voltage method [27] can also be used to calculate the saturation correction for partially irradiated ionization chambers as long as the number of created charges per volume unit is homogeneous in each electric field tube of force between electrodes (homogeneous irradiation in the tube of force). This is not difficult to achieve for plane-parallel ionization chambers with a small gap between the electrodes. However, measurements showed that among the different plane-parallel ionization chambers tested, the charges measured (M) for different inter-electrode voltages (V) do not always follow Boag's theory in beams smaller than the ionization chamber. Thus the saturation correction factor was calculated using the tangent of the best fit curve $1/M = f(1/V)$ at the point corresponding to the usually applied polarizing voltage, but the two-voltage method was applied whenever measurements showed linearity of $1/M$ versus $1/V$.

2.4. Uncertainties

Uncertainties were estimated according to the guidelines of the Guide to the Expression of Uncertainties in Measurement [40] and are expressed in terms of standard uncertainties (coverage factor k = 1). According to [40] the number in parenthesis after a value is the numerical value of the uncertainty referred to the last digit(s) of the reported result.

3. Results

3.1. Monte Carlo results

3.1.1. Water-to-air stopping power ratios

Table 3 shows $s_{w,air}$ values calculated at a depth of 10 cm in water for the 6 MV and 10 MV Varian DHX beams, together with the corresponding photon fluence-weighted mean energies. Type A relative standard uncertainties were typically below 0.1%.

Significant differences in mean energy values were observed between the reference (10 cm × 10 cm) and the stereotactic beams. On the contrary, mean energy variations between small beams were always below 4% and the corresponding differences in $s_{w,air}$ values were within 0.2%. The $s_{w,air}$ values specifically calculated for the 10 MV and 6 MV stereotactic beams were up to about 0.6% and 0.3% lower than the corresponding values pertaining to the 10 cm × 10 cm field size (i.e. the

Table 3
Water-to-air stopping-power ratios, $s_{w,air}$, calculated by means of the EGSnrc/SPRRZnrc user code for the Varian DHX 6 MV and 10 MV beams at 10 cm water depth for various field sizes. Radius of the scoring region was 0.1 cm or 1.5 cm for the $s_{w,air}$ values in brackets. The standard uncertainty of $s_{w,air}$ is typically below 0.1%. The photon fluence-weighted mean energies are also reported in the 2nd and 4th column.

Field size	6 MV		10 MV	
	$\overline{E}_{z=10cm}$ (MeV)	$s_{w,air}$	$\overline{E}_{z=10cm}$ (MeV)	$s_{w,air}$
10 cm × 10 cm	1.378	1.1213 [1.1209]	2.306	1.1077 [1.1069]
ϕ = 2.00 cm	1.874	1.1188 [1.1190]	3.198	1.1034 [1.1033]
ϕ = 1.50 cm	1.924	1.1184 [1.1189]	3.282	1.1027 [1.1035]
ϕ = 1.25 cm	1.941	1.1181 [1.1187]	3.319	1.1012 [1.1035]

values currently used for radiotherapy reference dosimetry based on point measurement of D_w). These results confirm previous findings in the literature reporting differences that are smaller than 0.5% between broad (10 cm × 10 cm) and narrow 6 MV beams at reference depth [41–45]. Previous studies also indicate that differences become larger at higher energies and values up to 1.1% are reported in case of a 24 MV beam [43].

Mean energy and $s_{w,air}$ data in table 3 refer to the beam axis and it should be noted that the photon spectra vary with the radial distance from the central axis. At a given depth in water, an energy decrease is generally observed when the radial distance increases. This is especially true beyond the beam edge where contributions to the photon energy spectra come from low-energy photons generated by radiation interactions in water. For the Varian stereotactic beams, the photon fluence-weighted mean energy calculated for scoring regions with radius ranging from 0.5 cm to 5 cm varied up to about 10%. The associated effects on the $s_{w,air}$ values were up to 0.2% for the 6 MV beams and up to 0.5% for the 10 MV beams. Differences between $s_{w,air}$ values at 10 cm and 20 cm were always within 0.2%.

For the GE Saturne 43 accelerator, $s_{w,air}$ values calculated for the 6 MV beam with diameter of 2 cm, 1 cm and 0.75 cm and disc-shaped (radius 1.5 cm) scoring region at 10 cm depth in water were very close to each other (from 1.1170 to 1.1171) as well as the photon fluence-weighted mean energies (from 1.977 to 1.979 MeV). Differences from the corresponding $s_{w,air}$ values for the Varian DHX linac (table 3, values in brackets) were about -0.2%, in line with the slightly lower (around -5%) mean energies of the Varian simulated beams.

3.1.2. Calculation of $DAPR_{20,10}$

Table 4 shows $DAPR_{20,10}$ values calculated for the Varian DHX 6 MV and 10 MV small circular beams of diameters ϕ, using dose scoring regions with different radii (R). Type A relative standard uncertainties were in the range 0.15–0.3%.

The $DAPR_{20,10}$ values reported in table 4 refer to the SSD setup with SSD = 100 cm and the SDD setup with SDD = 100 cm. For both setups, the $DAPR_{20,10}$ values relevant to the same integration area were almost independent of the beam diameter, in line with the results of Monte Carlo calculations showing that the mean beam energies were almost the same (section 3.1.1). Even if an increase in the $DAPR_{20,10}$ value can be noted when the field diameter decreases, especially for the SDD setup, differences among $DAPR_{20,10}$ values were generally within the expanded type A uncertainty (coverage factor k = 3). On the other hand, data in table 4 clearly show a variation of $DAPR_{20,10}$ value with both setup and scoring region radius. Due to the different distances from the source in the SSD configuration, the scoring regions at 120 cm source distance (20 cm depth) receive less of the scattered radiation outside the beam than the equivalent scoring regions at 110 cm source distance (10 cm depth). As a consequence $DAPR_{20,10}$ values calculated for the SSD setup were always lower than those calculated for the SDD setup. Deviations about 1–2% were observed with no clear dependence on energy, field diameter, or scoring region radius.

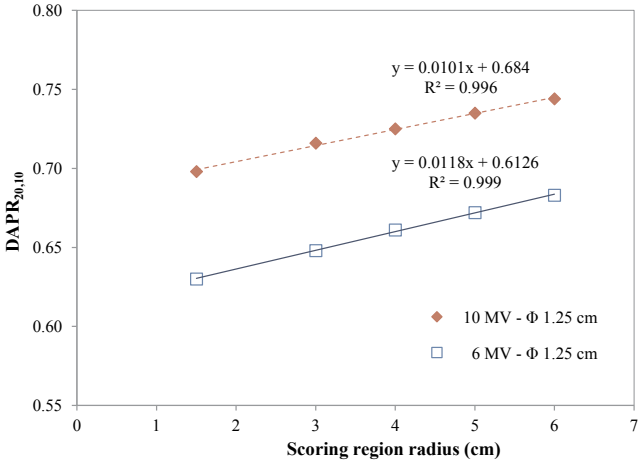

Fig. 2. Monte Carlo calculated $DAPR_{20,10}$ with SDD 100 cm as a function of the scoring region radius, R, for the 6 MV and 10 MV stereotactic beams with diameter 1.25 cm produced by the Varian DHX accelerator.

As shown in Table 4, $DAPR_{20,10}$ increases with the scoring region radius for both SSD and SDD setups and for all of the field sizes considered. When the radius of the scoring region increases, the relative contribution to DAP from the scattered radiation increases more at 20 cm depth than at 10 cm depth. It could be reasonably contended that if the radius of the scoring region increases, more and more of the scattered radiation will be seen and $DAPR_{20,10}$ will tend to an upper limit. However, the calculated $DAPR_{20,10}$ value increased all over the R range (1.5 cm to 6 cm) considered, with an approximately linear relation. It could be expected that, for even higher R values, $DAPR_{20,10}$ deviates from linearity to reach a limit, but this is likely to occur for R values far larger than the radius of the available LACs. As an example, $DAPR_{20,10}$ for the SDD setup is shown in Fig. 2 as a function of R for the 6 MV and 10 MV beams with field diameter 1.25 cm. The increase in the $DAPR_{20,10}$ value in the R range from 1.5 cm to 6 cm is about 1.9% per cm and 1.5% per cm for the 6 MV and 10 MV beams, respectively. These figures slightly decrease when the beam radius increases, their values being 1.7% per cm and 1.4% per cm for the beam with a diameter of

Table 4
Ratios of DAP at 20 cm and 10 cm in water calculated by Monte Carlo with different scoring region radii (R) for Varian DHX 6 MV and 10 MV circular beams with field diameter (ϕ) 2.00 cm, 1.50 cm and 1.25 cm for the SSD and SDD setups. The reported uncertainties are type A standard uncertainties (between 0.15% and 0.3%).

	$DAPR_{20,10}$–6 MV–Varian DHX					
	SSD setup (SSD = 100 cm)			SDD setup (SDD = 100 cm)		
R (cm)	ϕ = 2.00 cm	ϕ = 1.50 cm	ϕ = 1.25 cm	ϕ = 2.00 cm	ϕ = 1.50 cm	ϕ = 1.25 cm
1.5	0.617 (1)	0.621 (1)	0.622 (1)	0.628 (1)	0.629 (1)	0.630 (1)
4.0	0.646 (1)	0.644 (1)	0.643 (1)	0.654 (1)	0.657 (1)	0.661 (1)
5.0	0.658 (1)	0.657 (1)	0.658 (1)	0.664 (1)	0.668 (1)	0.672 (1)
	$DAPR_{20,10}$ –10 MV-Varian DHX					
	SSD setup (SSD = 100 cm)			SDD setup (SDD = 100 cm)		
R (cm)	ϕ = 2.00 cm	ϕ = 1.50 cm	ϕ = 1.25 cm	ϕ = 2.00 cm	ϕ = 1.50 cm	ϕ = 1.25 cm
1.5	0.682 (2)	0.688 (2)	0.691 (2)	0.697 (2)	0.698 (2)	0.698 (2)
4.0	0.713 (2)	0.709 (2)	0.708 (2)	0.723 (1)	0.724 (1)	0.725 (2)
5.0	0.724 (2)	0.722 (2)	0.722 (2)	0.732 (1)	0.734 (1)	0.735 (2)

2 cm.

Calculations performed for the square beams defined by the linac jaws confirmed that $DAPR_{20,10}$ value referred to a given integration area is almost independent of the beam size (differences were within 1% in the range of field side from 1.6 cm to 0.5 cm). On the other hand, $DAPR_{20,10}$ for the square beams was less sensitive to the radius of the scoring region than for the stereotactic beams. The $DAPR_{20,10}$ variation with R was typically 1.2% per cm. When comparing results obtained for beams with equivalent sections (i.e. circular beam with diameter 1.25 cm and square beam with side 1.1 cm) differences between $DAPR_{20,10}$ values were within the statistical uncertainty (0.1%) for a scoring region radius of 1.5 cm but around 1.5% for a scoring region radius of 6 cm.

A possible influence of the size of the water phantom on the calculated $DAPR_{20,10}$ was also considered. No appreciable effects were found for phantom radii larger than 20 cm and phantom heights above 30 cm. The maximum variations of $DAPR_{20,10}$ above these phantom size limits were lower than 0.15% and, therefore, within the statistical uncertainties.

Finally effects of electron spot size and energy of the initial electron beam on $DAPR_{20,10}$ calculation were evaluated by modifying those simulation parameters for the 6 MV beam. The FWHM of the electron spatial distribution was varied from 1.0 mm to 2.5 mm and the corresponding variations in $DAPR_{20,10}$ values were smaller than 0.3% even for the smallest beam simulated (square beam with 0.5 cm side). The initial electron beam energy was varied in the range from 5 MeV to 7 MeV for the 6 MV beam with diameter of 1.25 cm. As illustrated in Fig. 3, the calculated $DAPR_{20,10}$ values show high correlation with the initial electron beam energy whatever the scoring region radius in the range 1.5–5 cm.

Table 5 shows $DAPR_{20,10}$ values for the GE Saturne 43 accelerator calculated in the SDD setup with EGSnrc and PENELOPE using a scoring region radius of 1.5 cm. Except for the value corresponding to the beam diameter of 1 cm, results from both codes agree within one statistical standard deviation. Results are also rather close for the different beam diameters with very similar energy spectra. On the other hand, $DAPR_{20,10}$ values referring to the GE Saturne 43 accelerator are larger than those calculated for the Varian DHX accelerator (6 MV, SDD = 100 cm, R = 1.5 cm) by about 1.7%. This could be partially ascribed to the different mean energies of the simulated beams, as mentioned in Section 3.1.1.

Table 5
Ratios of *DAP* at 20 cm and 10 cm in water calculated by PENELOPE and EGSnrc Monte Carlo codes with a scoring region radius (R) of 1.5 cm for GE Saturne 43 6 MV circular beams with field diameter (ϕ) 2 cm, 1 cm and 0.75 cm for the SDD setup (SDD = 100 cm). The last line gives the ratios between the *DAP* at 20 cm and 10 cm obtained by PENELOPE and EGSnrc. The reported uncertainties are type A standard uncertainties.

	$DAPR_{20,10}$–6 MV–GE Saturne 43		
	ϕ = 2 cm	ϕ = 1 cm	ϕ = 0.75 cm
PENELOPE	0.639 (1)	0.642 (2)	0.641 (3)
EGSnrc	0.6385 (2)	0.6392 (4)	0.6404 (2)
Ratio	1.0009 (14)	1.0038 (24)	1.0011 (39)

3.2. Experimental results

All the tested ionization chambers showed signal drifts in water in a ^{60}Co beam. The drift was of 0.06% per hour for the SV-PMMA, 0.1% per hour for the BP_IC, 0.2% per hour for the T_IC and 0.4% per hour for the PTW 34073. Given the large drift, the PTW 34073 chamber was rejected for this study. The drift for the SV-PMMA ionization chamber was attributed to deformations of the PMMA waterproof box which is in contact with the front graphite electrode.

In the Varian DHX beams, the repeatability of the ionization chamber signal was better than 0.1% and the short-term reproducibility, evaluated during a measurement session, was 0.3%. The signal variability during a measurement session was mostly ascribed to the reproducibility of the beam profile, since the uncertainty component due to the chamber positioning at the measurement depth was 0.05% (positioning uncertainty was 0.1 mm). The saturation correction factor determined at various depths in water ranged from 1.001 to 1.003 for the BP_IC chamber and was around 1.001 for the TC_IC chamber, with no dependence on depth or field size. The polarity correction factor for both chambers ranged from 1.001 to 1.002.

Fig. 4 shows the normalized depth ionizing curves measured using the BP_IC chamber in the Varian 6 MV beams with reference and stereotactic field sizes. Differences along the curves referring to stereotactic beams were generally within ± 1%. Similar results were obtained for the 10 MV beams. Differences in $M(20)/M(10)$ values obtained with SSD values of 80 cm, 90 cm and 100 cm were well within 0.5% for both photon energies with no evidence of SSD dependence. However, $M(20)/M(10)$ values obtained in the SSD setups using the

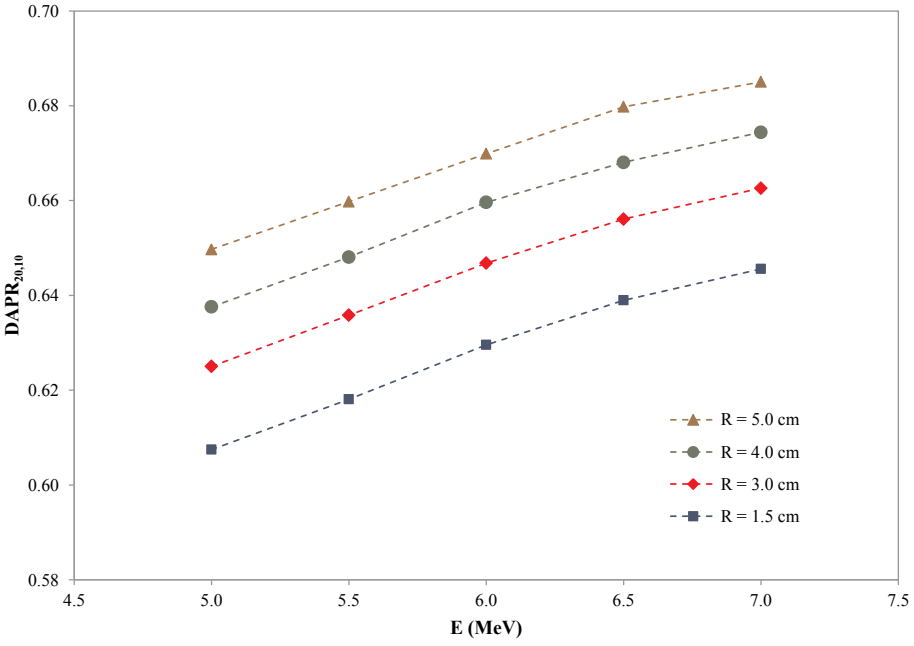

Fig. 3. Calculated $DAPR_{20,10}$ with scoring region radii (R) of 1.5 cm, 3 cm, 4 cm and 5 cm vs the initial electron beam energy used for the Monte Carlo simulation of the Varian 6 MV beam with diameter of 1.25 cm.

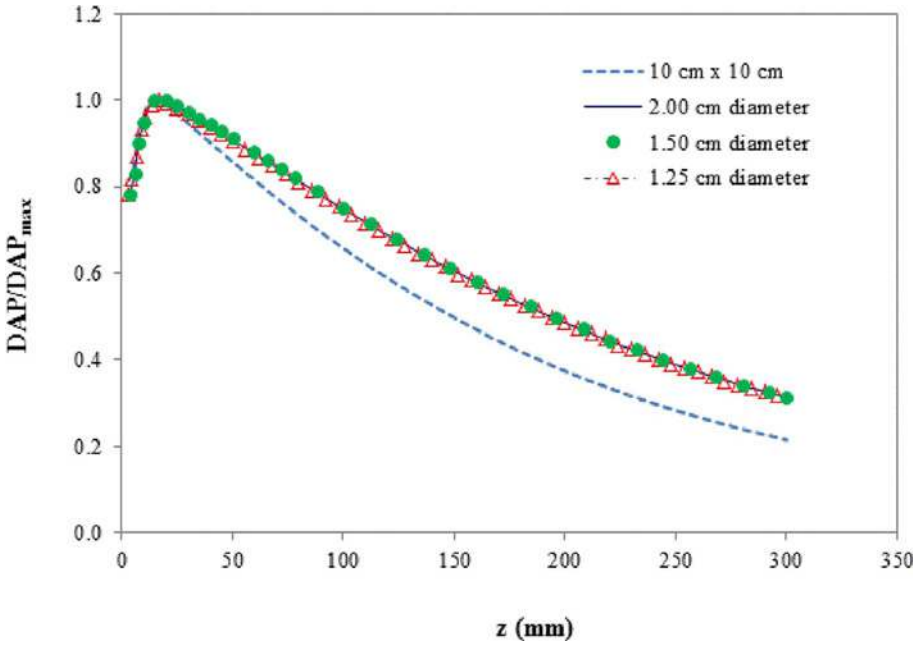

Fig. 4. Normalized depth ionization curves (SSD 100 cm) measured with a PTW 34070 ionization chamber with collecting electrode diameter of 8.16 cm at 6 MV for the reference field size (10 cm × 10 cm) and three stereotactic beams with diameter 2.00 cm, 1.50 cm and 1.25 cm at the phantom surface.

Table 6
Ratios of ionization chamber readings at 20 cm and 10 cm depths in water obtained at a fixed source to detector distance of 100 cm (SDD) for 6 MV and 10 MV stereotactic beams using a transmission chamber (T_IC) and a PTW 34070 ionization chamber (BP_IC) with collecting electrode diameter of 9.65 cm and 8.16 cm, respectively. The combined relative standard uncertainty of *M(20)/M(10)* is 0.4%.

Field diameter	M(20)/M(10), SDD = 100 cm					
	6 MV			10 MV		
	BP_IC	T_IC	BP_IC/T_IC	BP_IC	T_IC	BP_IC/T_IC
2.00 cm	0.6652	0.6723	0.990	0.7332	0.7379	0.994
1.50 cm	0.6719	0.6804	0.988	0.7386	0.7449	0.992
1.25 cm	0.6741	0.6832	0.987	0.7379	0.7469	0.988

BP_IC chamber were systematically lower than those obtained by the T_IC chamber. Differences were typically around 1.5%.$M(20)/M(10)$ measurements were also made in the SDD setup (SDD = 100 cm) and results are shown in table 6. Differences between $M(20)/M(10)$ values obtained by the BP_IC and TC_IC chambers were typically around 1%. These differences, as well as those observed for the SSD setup, can be ascribed to the different collecting electrode diameters of the two ionization chambers, in agreement with the Monte Carlo calculations which showed a dependence of $DAPR_{20,10}$ on the radius of the dose scoring region (for the SDD setup, Monte Carlo differences were in the range 0.9% to 1.2% using R = 4.08 cm and 4.825 cm).

Data in table 6 also show a tendency of $M(20)/M(10)$ ratio to increase when the field diameter decreases. At 6 MV, the values referring to 2 cm and 1.25 cm beam diameters differ from each other by 1.3% and 1.6% for the BP_IC and the T_IC chambers, respectively. The corresponding differences for the 10 MV beams are 0.7% and 1.2%. The Monte Carlo calculated differences were 1.0% and 1.2% for 6 MV, and 0.3% and 0.4% for 10 MV.

For the GE Saturne 43 accelerator, $M(20)/M(10)$ ratios measured in the SDD setup for three beam diameters (2 cm, 1 cm and 0.75 cm) with the SV-PMMA and the BP_IC chambers are shown in table 7. Differences among the measured ratios were 0.43% for the 3 cm sensitive diameter and 1.4% for the 8.16 cm sensitive diameter. The differences between the $M(20)/M(10)$ ratios measured by the two ionization chambers were larger (around 4%) than data shown in table 6 as the size difference of the collecting surfaces is larger. The results obtained with the BP_IC chamber are consistent between the two accelerators, the $M(20)/M(10)$ difference being 0.36% for the 6 MV beams with 2 cm diameter.

Table 7
M(20)/M(10) in water obtained at a fixed source to detector distance of 100 cm for 6 MV produced by the GE Saturne 43 accelerator using a home-made chamber (SV-PMMA) and a PTW 34070 chamber (BP_IC) with sensitive air cavity diameter of 3 cm and 8.16 cm, respectively.

Field diameter	6 MV–SDD = 100 cm		
	SV-PMMA	BP_IC	BP_IC/SV-PMMA
2.00 cm	0.6414 (6)	0.6676 (16)	1.041
1.00 cm	0.6433 (4)	0.6706 (16)	1.042
0.75 cm	0.6442 (6)	0.6767 (19)	1.051

In Fig. 5 the $M(20)/M(10)$ ratios measured using the SV-PMMA chamber are compared to the Monte Carlo $DAPR_{20,10}$ values calculated with a scoring region of 1.5 cm radius. While PENELOPE and EGSnrc calculations gave comparable results, the differences between the calculated and the corresponding measured $DAPR_{20,10}$ were around 0.5% and the calculated values were systematically smaller than the measured ones. The 0.5% difference is consistent with the type B uncertainty (0.55%, k = 1) associated to the ratio of *DAP* values calculated by Monte Carlo using the same integration area (see details in Appendix A).

4. Discussion

4.1. Reference integration area

In this work, the properties of $DAPR_{20,10}$ in water were studied both by Monte Carlo simulations and by measurements using large-area ionization chambers in 6 MV and 10 MV photon beams with field sizes below 2 cm. Using the Monte Carlo phase-space files describing stereotactic photon beams, $DAPR_{20,10}$ was calculated for different values of the integration area (always larger than the beam size), using both SSD and SDD setups. Calculation results showed a dependence of $DAPR_{20,10}$ on both the setup and the size of the integration area. Such dependences were experimentally confirmed by comparing ratios of ionization signals at 20 cm and 10 cm water depths obtained by means of LACs with different collecting electrode diameters. Taken together,

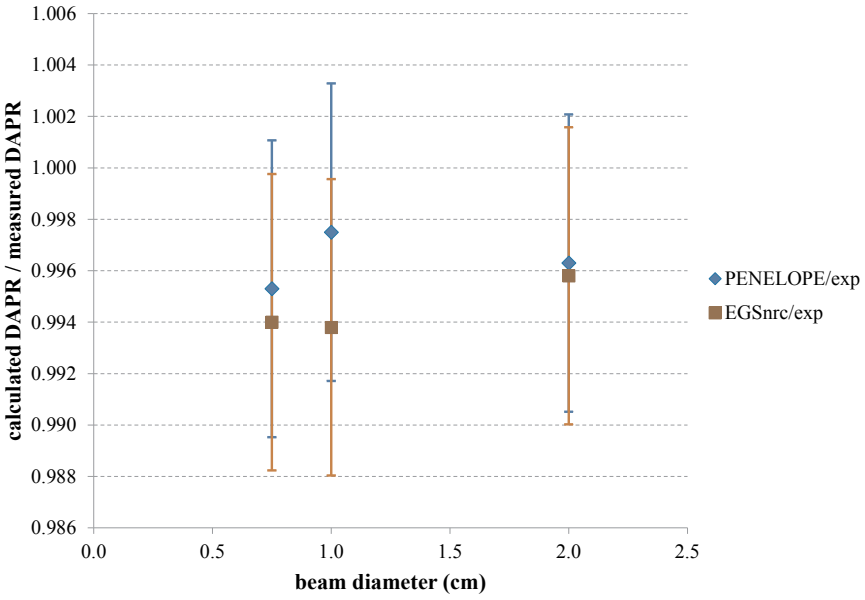

Fig. 5. Ratios of calculated $DAPR_{20,10}$ to measured *M(20)/M(10)* for a scoring region corresponding to a disc of 3 cm diameter. The uncertainties correspond to one standard deviation including the statistical and estimated (0.55%) uncertainties.

these results indicate that a reference setup and a reference integration area must be defined to obtain a $DAPR_{20,10}$ parameter useful as beam quality specifier. Then, to allow measurement of such beam quality specifier by means of a generic LAC, correction factors are required to convert the $M(20)/M(10)$ measured values to the values 'as they would be' if they were measured, under the same experimental conditions, by a chamber with collecting electrode area equal to the reference area. Different computational or experimental methods can be used for determining such correction factors. In this work, a method based on Monte Carlo simulations was applied. Accordingly, for a given ionization chamber with collecting electrode radius R_{IC}, the correction factor for the small field size *fs* is defined as

$$k^{fs}_{R_{ref},R_{IC}} = \frac{[DAP_{R_{ref}}(20)/DAP_{R_{ref}}(10)]^{fs}}{[DAP_{R_{IC}}(20)/DAP_{R_{IC}}(10)]^{fs}} \quad (3)$$

where R_{ref} is the radius of the reference integration area. Then the value of $DAPR_{20,10}$ to be used as beam quality index is obtained as

$$DAPR^{R_{ref}}_{20,10} = \left[\frac{M_{R_{IC}}(20)}{M_{R_{IC}}(10)}\right]^{fs} k^{fs}_{R_{ref},R_{IC}} \quad (4)$$

Using the *DAP* values calculated by Monte Carlo at 20 cm and 10 cm depths as a function of the radius of the integration area, $k^{fs}_{R_{ref},R_{IC}}$ correction factors can be determined for any ionization chamber radius. It should be noted that Eq. (4) is derived under the assumption that the ionization chamber response in terms of *DAP* does not change with water depth (i.e. $M_{R_{IC}}(20)/M_{R_{IC}}(10) = DAP_{R_{IC}}(20)/DAP_{R_{IC}}(10)$). Although results in section 3.1.1 showed that the $s_{w,air}$ variation with depth is marginal, changes in the chamber response due to perturbation effects cannot be excluded in principle. The agreement between the calculated $DAPR_{20,10}$ and the measured $M(20)/M(10)$ ratios shown in Fig. 5 supports the above assumption for the SV-PMMA chamber. The assumption was further verified for the BP_IC chamber by Monte Carlo simulation. The ionization chamber was modelled according to the manufacturer's drawings and the chamber response in terms of *DAP* was calculated as

$$r(d) = \frac{DAP_{air,IC}(d)}{DAP_w(d)} \quad (5)$$

where *d* is the water depth, $DAP_{air,IC}$ (*d*) is the average absorbed dose in the air cavity integrated over the ionization chamber (IC) active area and $DAP_w(d)$ is the integral of D_w, in homogeneous water, over the cross-sectional area of a water voxel equal to the IC active volume. Circular beams with diameter 2.0 cm and 1.25 cm and square beams with side 1.0 cm and 0.5 cm were considered. Calculation results showed variations below 0.2% in *r(d)* with depth, thereby supporting the validity of Eq. (4).

Considering that the absolute measurement of *DAP* at LNE-LNHB refers to an integration area with radius 1.5 cm [25,26] the same area is tentatively assumed in this work as reference for the $DAPR^{R_{ref}}_{20,10}$ measurement. Accordingly, $k^{fs}_{R_{ref},R_{IC}}$ correction factors with R_{ref} = 1.5 cm were determined for the BP_IC and T_IC ionization chambers and applied to the ratios $M(20)/M(10)$ measured in the Varian DHX beams with SDD 100 cm. Differences between $DAPR^{R_{ref}}_{20,10}$ values obtained by the two ionization chambers do not exceed 0.4%, while differences between the measured $M(20)/M(10)$ values were up to 1.3% (see data in Table 8 and Table 6).

The ratio between the $M(20)/M(10)$ measured with a BP_IC chamber and the SV-PMMA chamber (whose area corresponds to the area chosen as reference) is equal to 1.041 for the Saturne 43 accelerator (data in table 7 – 6 MV, 2 cm field diameter). The equivalent calculated ratio for the Varian DHX beam, obtained from data in tables 6 and 8, is very close (1.043) indicating that the correction factor is nearly independent of those linac types and those collimating systems. Using the $k^{fs}_{R_{ref},R_{IC}}$ factor calculated for the Varian beam with diameter of 2 cm, $DAPR^{R_{ref}}_{20,10}$ values obtained by the BP_IC and the SV-PMMA chambers are in agreement within 0.2%. However, a different rate of $DAPR_{20,10}$ change with scoring region radius was found for beams shaped by the linac jaws compared to those shaped by cones (see Section 3.1.2). Thus, $k^{fs}_{R_{ref},R_{IC}}$ correction factors should be calculated specifically for each individual collimator system.

Table 8
$DAPR^{R_{ref}}_{20,10}$ values referred to a reference area with diameter 3 cm (R_{ref} = 1.5 cm) obtained applying Monte Carlo correction factors to the ratio of ionization signals at 20 cm and 10 cm water depths.

Field diameter	6 MV			10 MV		
	BP_IC	T_IC	BP_IC/T_IC	BP_IC	T_IC	BP_IC/T_IC
2.00 cm	0.638	0.637	1.001	0.706	0.703	1.004
1.50 cm	0.643	0.641	1.002	0.712	0.710	1.003
1.25 cm	0.642	0.642	1.002	0.710	0.711	0.999

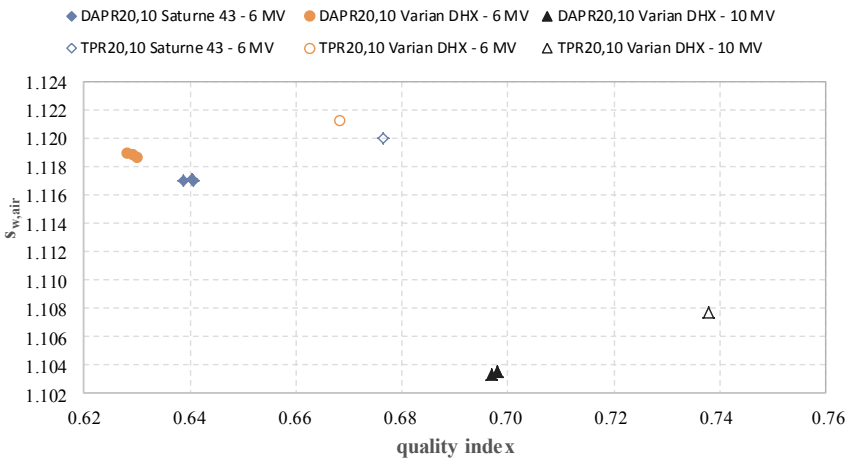

Fig. 6. Water-to-air stopping power ratio as a function of the beam quality index ($DAPR_{20,10}^{R_{ref}}$ or $TPR_{20,10}$). The stopping power ratios corresponding to $DAPR_{20,10}^{R_{ref}}$ values (filled symbols) are calculated for the reference area (R = 1.5 cm) while the stopping powers corresponding to $TPR_{20,10}$ values (unfilled symbol) are calculated for a small volume on the beam axis.

4.2. $DAPR_{20,10}$ as beam quality specifier

Data in Table 8 show that the maximum variation in the $DAPR_{20,10}^{R_{ref}}$ value for the Varian DHX stereotactic beams is below 0.8% and 1% for 6 MV and 10 MV, respectively. Similarly, data in Table 7 show that the $DAPR_{20,10}^{R_{ref}}$ values measured by means of the SV-PMMA chamber in the GE Saturne 43 6 MV beams with diameters 2 cm, 1 cm and 0.75 cm differ from one another by less than 0.5%. Data summarized in Table 7 and Table 8 indicate a tendency of the $DAPR_{20,10}^{R_{ref}}$ value to increase when the field size decreases, in line with the slight increase of the mean photon energy shown by Monte Carlo simulations. However, the differences observed among field sizes are not statistically significant, particularly for the data in Table 8 obtained applying $k_{R_{ref},R_{IC}}^{fs}$ correction factors affected by a relative large type B uncertainty. Indeed, according to Eq. (3), $k_{R_{ref},R_{IC}}^{fs}$ factors were determined using ratios of *DAP* calculated by Monte Carlo for which a type B uncertainty of 0.55% is estimated (see Appendix A). A conservative estimate of the type B uncertainty of $k_{R_{ref},R_{IC}}^{fs}$ is therefore set to 0.8% (k = 1). Concerning dosimetric data, results in section 3.1.1 showed that changes in photon spectra among small fields have negligible effects (around 0.2%) on $s_{w,air}$ value. Moreover, simulations of the BP_IC chamber response in terms of DAP revealed that effects due to the field size are within 0.5%. On the basis of these results, for a given nominal energy, the same beam quality index can be associated to the small beams, for any field diameter from 2 cm to 0.75 cm.

The sensitivity of $DAPR_{20,10}$ to the beam energy was demonstrated by Monte Carlo results in section 3.1.2 (data in Fig. 3). Additionally, data in table 8 indicate a change of about 10% in the experimental $DAPR_{20,10}^{R_{ref}}$ value from 6 MV to 10 MV beams. Such a change is similar to that obtained for the beam quality specifiers currently used for radiotherapy photon beams (i.e. $TPR_{20,10}$ defined for the 10 cm × 10 cm reference field). This is also shown in Fig. 6 where the $s_{w,air}$ calculated for the beams used in this work are reported as a function of both $TPR_{20,10}$ and $DAPR_{20,10}^{R_{ref}}$. Thus, given a reference integration area, $DAPR_{20,10}$ determined in SDD setup appears suitable for specifying the photon beam quality for fields with diameter from 2 cm to 0.75 cm, since it combines field size independence with good sensitivity to beam energy. Further investigation would be desirable to extend these results to even smaller beams.

5. Conclusions

Results of this work show that a ratio of *DAP* that is useful as beam quality specifier for small beams is obtained for the reference condition that combines the SDD setup (SDD = 100 cm) and the integration surface with radius R_{ref} = 1.5 cm ($DAPR_{20,10}^{R_{ref}}$). In beams with diameter below 2 cm, $DAPR_{20,10}^{R_{ref}}$ is independent of field size and its sensitivity to the beam energy is similar to that of currently used beam quality specifiers defined for the 10 cm × 10 cm field size (i.e. $TPR_{20,10}$). Measuring $DAPR_{20,10}^{R_{ref}}$ in small beams can be achieved using large-area plane-parallel ionization chambers with cross-sectional area larger than the beam size. If the air cavity radius differs from R_{ref}, Monte Carlo correction factors accounting for effects due to the chamber size are required. Specific correction factors should be calculated for any nominal beam energy and collimator system. Since Monte Carlo calculations could be problematic at clinical level, an investigation on alternative practical methods for determining the above correction factors is worthwhile.

Conflicts of interest

None.

Acknowledgments

This work is supported by the EMRP joint research project MetrExtRT which has received funding from the European Union on the basis of Decision No 912/2009/EC. The EMRP is jointly funded by the EMRP participating countries within EURAMET and the European Union.

The computing resources and the related technical support used for this work at ENEA have been provided by CRESCO/ENEAGRID High Performance Computing infrastructure and its staff [46]. CRESCO/ENEAGRID High Performance Computing infrastructure is funded by ENEA, the Italian National Agency for New Technologies, Energy and Sustainable Economic Development and by Italian and European research programs, see http://www.cresco.enea.it/english for information.

Appendix A. Accuracy in *DAPR* calculation

The accuracy of Monte Carlo calculation of absorbed dose in regions extending laterally beyond the edge of the radiation was evaluated by comparing the results of simulations with the PENELOPE and EGSnrc codes, as well as via calculations and measurements of the mean absorbed doses in the core of two graphite calorimeters in small 6 MV beams produced by the GE Saturne 43 accelerator. Specifically a graphite calorimeter (GR11) with a core of 30 mm diameter and 3 mm thickness and a graphite calorimeter (GR10) with a core diameter of 6 mm and 6 mm thickness

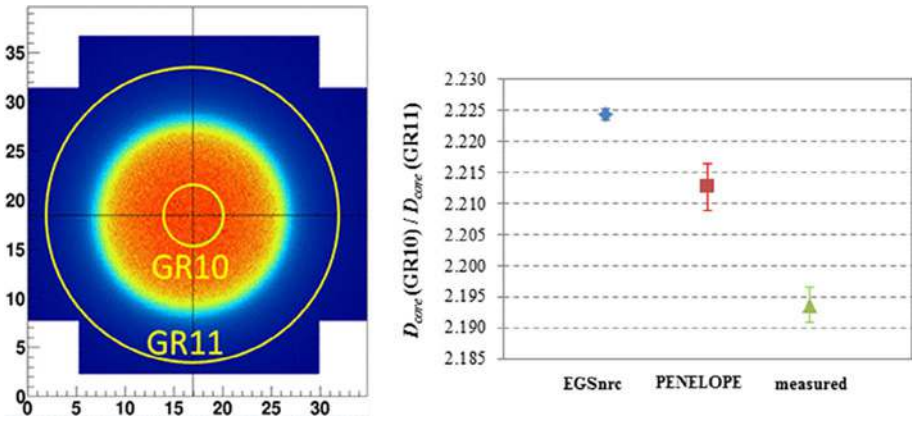

Fig. A1. Left hand side, representation of the core diameters for the GR11 and GR10 calorimeters (yellow circles) in a 2 cm diameter beam (measured with EBT3 films) and right hand side, $D_{core}(GR10)/D_{core}(GR11)$ ratios measured and calculated with EGSnrc and PENELOPE (error bars are type A uncertainties at one standard deviation).

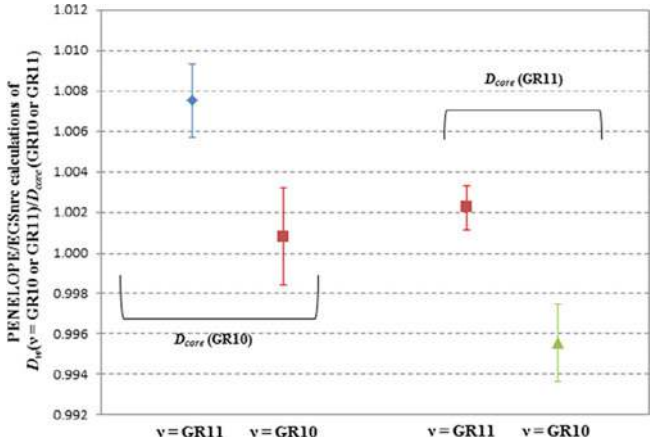

Fig. A2. $(D_w(\upsilon)/D_{core})_{PENELOPE}$ / $(D_w(\upsilon)/D_{core})_{EGSnrc}$ for cores and volumes of water υ corresponding to the GR10 and GR11 calorimeter cores (error bars are type A uncertainties at one standard deviation).

were used [26,47]. The GR11 calorimeter was designed for absolute measurements of *DAP* in field sizes smaller than 2 cm [26] and the size of the calorimeter core is the result of a compromise between two conflicting options: enlarging it to cover the greatest possible part of the scattered beam and reducing it to increase the measured temperature elevation in the core. On the other hand, the size of the GR10 calorimeter ensures that the core is widely within the field size for the largest circular beam (2 cm diameter) considered in this work. The GR10 and GR11 calorimeters were modelled and irradiations in a graphite phantom were simulated with both PENELOPE and EGSnrc codes.

For the beam with 2 cm diameter, the mean absorbed dose in the core (D_{core}) was calculated for both the GR10 and GR11 calorimeters and the ratio $D_{core}(GR10)/D_{core}(GR11)$ obtained by means of PENELOPE and EGSnrc codes are compared to the measured value in Fig. A1. A difference of 0.9% was found between the value calculated using PENELOPE and the measured value with a corresponding type A uncertainty (k = 1) of 0.2%. The corresponding difference was of 1.4% for EGSnrc calculations with a corresponding type A uncertainty (k = 1) of 0.15%. To explain such large differences between calculation and measurement, additional simulations were done to calculate, in a water phantom, the mean absorbed dose in water in a volume υ around the reference point corresponding to the calorimeter core volumes ($D_w(\upsilon \equiv core)$). The $D_w(\upsilon)/D_{core}$ ratios pertaining to the GR11 and GR10 calorimeter cores calculated by PENELOPE and EGSnrc are compared in Fig. A2 for the beam with diameter of 2 cm. Results obtained by means of the two Monte Carlo codes are in agreement (differences of 0.1% and 0.2% with type A uncertainties (k = 1) of 0.25% and 0.1%, respectively) for the ratios $D_w(\upsilon \equiv GR10)/D_{core}(GR10)$ and $D_w(\upsilon \equiv GR11)/D_{core}(GR11)$, that is when the scoring region is the same in both water and graphite. For $D_w(\upsilon \equiv GR10)/D_{core}(GR11)$ or $D_w(\upsilon \equiv GR11)/D_{core}(GR10)$, the differences are much larger, i.e. 0.4% and 0.8% with type A uncertainties (k = 1) of 0.3% and 0.2% respectively.

The above results indicate that Monte Carlo calculation of absorbed dose is more critical outside the beam field (out-scattered part) than inside and that differences between results obtained using different Monte Carlo codes can be significant. However, when the volume of water (υ) for the mean absorbed dose to water corresponds to the volume of the calorimeter core, the two codes are in agreement when calculating $D_w(\upsilon \equiv core)/D_{core}$. In this case, the increase of correlation in the calculation of the ratios seems to reduce the problem scale, although the related type B uncertainty should be enlarged (0.55%, $k = 1$), compared to the value of 0.2% that is typically adopted when the irradiated surface is well inside the beam. When the volumes involved in the dose ratio are really different (as in the case of the GR10 and GR11 calorimeter core volumes), a type B uncertainty of 0.8% (k = 1) should be used. This figure reflects the 1.4% maximum difference observed between measured and calculated dose ratios in terms of standard uncertainty of a rectangular distribution.

References

[1] Benmakhlouf H, Sempau J, Andreo P. Output correction factors for nine small field detectors in 6 MV radiation therapy photon beams: A PENELOPE Monte Carlo study. Med Phys 2014;41:041711.

[2] Bouchard H, Kamio Y, Palmans H, Seuntjens J, Duane S. Detector dose response in megavoltage small photon beams. I. Theoretical concepts. Med Phys 2015;42:6033–47.

[3] Scott AJD, Kumar S, Nahum AE, Fenwick JD. Characterizing the influence of

detector density on dosimeter response in non-equilibrium small photon fields. Phys Med Biol 2012;57:4461–76.
[4] Alfonso R, Andreo P, Capote R, Saiful Huq M, Kilby W, Kjäll P, et al. A new formalism for reference dosimetry of small and nonstandard fields. Med Phys 2008;35:5179–86.
[5] Azangwe G, Grochowska P, Georg D, Izewska J, Hopfgartner J, Lechner W, et al. Detector to detector corrections: a comprehensive experimental study of detector specific correction factors for beam output measurement for small radiotherapy beams. Med Phys 2014;41:072103.
[6] Czarnecki D, Zink K. Monte Carlo calculated correction factors for diodes and ion chambers in small photon fields. Phys Med Biol 2013;58:2431–44.
[7] Francescon P, Kilby W, Noll JM, Masi L, Satariano N, Russo S. Monte Carlo simulated corrections for beam commissioning measurements with circular and MLC shaped fields on the CyberKnife M6 System: a study including diode, microchamber, point scintillator, and synthetic microdiamond detectors. Phys Med Biol 2017;62:1076–95.
[8] Lechner W, Palmans H, Sölkner L, Grochowska P, Georg D. Detector comparison for small field output factor measurements in flattening filter free photon beams. Radiother Oncol 2013;109:356–60.
[9] Masi L, Russo S, Francescon P, Doro R, Frassanito MC, Fumagalli ML, et al. CyberKnife beam output factor measurements: a multi-site and multidetector study. Phys Med 2016;32:1647–9.
[10] O'Brien DJ, León-Vintró L, McClean B. Small field detector correction factors for silicon-diode and diamond detectors with circular 6 MV fields derived using both empirical and numerical methods. Med Phys 2016;43:411–23.
[11] Papaconstadopoulos P, Tessier F, Seuntjens J. On the correction, perturbation and modification of small field detectors in relative dosimetry. Phys Med Biol 2014;59:5937–52.
[12] Ralston A, Tyler M, Liu P, McKenzie D, Suchowerska N. Over-response of synthetic microDiamond detectors in small radiation fields. Phys Med Biol 2014;59:5873–81.
[13] Underwood TSA, Rowland BC, Ferrand R, Vieillevigne L. Application of the Exradin W1 scintillator to determine Ediode 60017 and microDiamond 60019 correction factors for relative dosimetry within small MV and FFF fields. Phys Med Biol 2015;60:6669–83.
[14] Huet C, Moignier C, Barraux V, Loiseau C, Sebe-Mercier K, Batalla A, et al. Study of commercial detector responses in non-equilibrium small photon fields of a 1000 MU/min CyberKnife system. Phys Med 2016;32:818–25.
[15] Andreo P, Palmans H, Marteinsdóttir M, Benmakhlouf H, Carlsson-Tedgren Å. On the Monte Carlo simulation of small-field micro-diamond detectors for megavoltage photon dosimetry. Phys Med Biol 2016;61:L1–10.
[16] Marinelli M, Prestopino G, Verona C, Verona-Rinati G. Experimental determination of the PTW 60019 microDiamond dosimeter active area and volume. Med Phys 2016;43:5205.
[17] Charles PH, Cranmer-Sargison G, Thwaites DI, Crowe SB, Kairn T, Knight RT, et al. A practical and theoretical definition of very small field size for radiotherapy output factor measurements. Med Phys 2014;41:041707–41708.
[18] International Atomic Energy Agency. Dosimetry in diagnostic radiology: an International Code of Practice; IAEA Technical Report Series. Vol. 457. Vienna: IAEA; 2007.
[19] Djouguela A, Harder D, Kollhoff R, Ruhmann A, Willborn KC, Poppe B. The dose-area product, a new parameter for the dosimetry of narrow photon beams. Z Med Phys 2006;16:217–27.
[20] Duane S, Graber F, Thomas RAS. International Symposium on Standards, Applications and Quality Assurance in Medical Radiation Dosimetry; Application of Dose Area Product and DAP Ratio to Dosimetry in IMRT and Small Field External Beam Radiotherapy. IAEA-CN-182 Paper No 222. Vienna: IAEA; 2010.
[21] Le Roy M, Dufreneix S, Daures J, Delaunay F, Gouriou J, Ostrowsky A, et al. Establishment of dosimetric references in terms of dose-area product for small sizes MV X-ray beams. Phys Med 2015;31(S2):e52–3.
[22] Sánchez-Doblado F, Hartmann GH, Pena J, Roselló JV, Russiello G, Gonzales-Castaño DM. A new method for output factor determination in MLC shaped narrow beams. Phys Med 2007;23:58–66.
[23] Pimpinella M, De Coste V, Guerra AS, Silvi L, Petrucci A, Barile S. Measurements of Dose.area-product ratio in small radiotherapy photon beams using two types of large-area plane-parallel ionization chambers. Phys Med 2015;31(s2):e53.
[24] Underwood TSA, Winter HC, Hill MA, Fenwick JD. Detector density and small field dosimetry: integral versus point dose measurement schemes. 2013;40. 082102-1-15.
[25] Dufreneix S, Ostrowsky A, Le Roy M, Sommier L, Gouriou J, Delaunay F, et al. Using a dose-area product for absolute measurements in small fields: a feasibility study. Phys Med Biol 2016;61:650–62.
[26] Dufreneix S, Bordy J M, Daures J, Delaunay F and Ostrowsky A. Construction of a large graphite calorimeter for measurements in small fields used in radiotherapy. 16th International Congress of Metrology; 2013; 05006 doi: http://dx.doi.org/10.1051/metrology/201305006.
[27] Andreo P, Burns DT, Hohlfeld K, Huq MS, Kanai T, Laitano F. Absorbed dose determination in external beam radiotherapy: an international code of practice for dosimetry based on standards of absorbed dose to water. IAEA Technical Report Series No 398. Vienna, Austria: International Atomic Energy Agency; 2000.
[28] Rogers DWO, Faddegon BA, Ding GX, Ma C-M, We J, Mackie TR. BEAM: a Monte Carlo code to simulate radiotherapy treatment units. Med Phys 1995;22:503–4.
[29] Kawrakow I, Mainegra-Hing E, Rogers DWO, Tessier F, Walter BRB. The EGSnrc Code System: Monte Carlo simulation of electron and photon transport; NRC Report No. PIRS-701. Ottawa, Canada: National Research Council of Canada (NRC); 2013.
[30] Francescon P, Cora S, Cavedon C. Total scatter factors of small beams: a multi-detector and Monte Carlo study. Med Phys 2008;35:504–13.
[31] Ma C-M, Rogers DWO. BEAMDP as a General-Purpose Utility; NRC Report PIRS-0509(E) revA. Ottawa, Canada: National Research Council of Canada (NRC); 2013.
[32] Rogers DWO, Walter B, Kawrakow I. BEAMnrc user manual. NRC Report PIRS-509(A) revL. Ottawa, Canada: National Research Council of Canada (NRC); 2013.
[33] Kawrakow I, Rogers DWO, Walter BRB. Large efficiency improvements in BEAMnrc using directional bremsstrahlung splitting. Med Phys 2004;31:2883–98.
[34] Rogers DWO, Kawrakow I, Seuntjens JP, Walter BRB. NRCC user codes for EGSnrc. NRC Report PIRS-702. Ottawa, Canada: National Research Council of Canada (NRC); 2013.
[35] Salvat F, Fernandez-Varea JM, Sempau J. A code system for Monte Carlo Simulation of Electron and Photon Transport; Workshop Proc 2006. Barcelona, Spain: Nuclear Energy Agency; 2006.
[36] Tola F, Poumarede B, Habib B and Gmar M. Optimization of Monte Carlo codes PENELOPE 2006 and PENFAST by parallelization and reduction variance implementation; Second European Workshop on Monte Carlo Treatment Planning. Cardiff, October 19–21 2009, Workshop MCTP; 2009.
[37] Constantin M, Perl J, LoSasso T, Salop A, Whittum D, Narula A, et al. Modeling the truebeam linac using a CAD to Geant4 geometry implementation: dose and IAEA-compliant phase space calculations. Med Phys 2011;38:4018–24.
[38] Dufreneix S. Etablissement de références dosimétriques dans les faisceaux de rayons × de hautes énergies et de très petites sections ($< 1\ cm^2$) pour la radiothérapie. Physique Médicale [physics.med-ph]. Université Paris Sud – Paris XI, 2014. Français. < NNT: 2014PA112416 > . < tel-01127240 > https://tel.archives-ouvertes.fr/tel-01127240.
[39] Boag JW. Ionization chambers. In: Kase KR, Bjanrngard BE, Attix FH, editors. The dosimetry of ionizing radiation. Vol. 2. New York: Academic press; 1987. p. 169–243.
[40] JCGM 2008 Evaluation of measurement data - Guide to the expression of uncertainty in measurement JCGM; 2008: 1–134.
[41] Eklund K, Ahnesjö A. Fast modelling of spectra and stopping power ratio using differentiated fluence pencil kernels. Phys Med Biol 2008;52:4231–47.
[42] Araki F. Monte Carlo study of a CyberKnife stereotactic radiosurgery system. Med Phys 2006;33:2955–63.
[43] Sánchez-Doblado F, Andreo P, Capote R, Leal A, Perucha M, Arráns R, et al. Ionization chamber dosimetry of small photon fields: a Monte Carlo study on stopping-power ratios for radiosurgery and IMRT beams. Phys Med Biol 2003;48:2081–99.
[44] Verhaegen F, Das IJ, Palmans H. Monte Carlo dosimetry study of a 6 MV stereotactic radiosurgery unit. Phys Med Biol 1998;43:2755–68.
[45] Andreo P, Brahme A. Stopping power data for high-energy photon beams. Phys Med Biol 1986;31:839–58.
[46] Ponti G, et al. The role of medium size facilities in the HPC ecosystem: the case of the new CRESCO4 cluster integrated in the ENEAGRID infrastructure; Proceedings of the International Conference on High Performance Computing and Simulation (HPCS); 2014. art. no. 6903807:1030–33.
[47] Daures J, Ostrowsky A, Rapp B. Small section graphite calorimeter (GR-10) at LNE-LNHB for measurements in small beams for IMRT. Metrologia 2012;49:S174–8.