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## Fault Injection to Reverse Engineer DES-like Cryptosystems

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- In contradiction with Kerckhoffs' principle [?], private algorithms are still used.
- Creating a strong new cryptosystem from scratch is not easy.
- These algorithms respect some properties identical to algorithm which has gained one's spurs.
- When the goal of an attacker is to retrieve information on a private algorithm, his attack is termed reverse engineering.
- Pseudo DES with customized s-boxes.
- Even if an algorithm is securely designed, it may be vulnerable to physical attacks as fault injection attacks.
- The fault injection attacks consist in disrupting the circuit behaviour.
- FIRE Fault Injection for Reverse Engineering.


## Plan



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## DES Data Encrytption Standard

- Established by the NIST [?]
- A symmetric cryptosystem, specifically a 16 -round Feistel cipher.
- Starts by $I P$, a permutation of 64 bits and finishes by its inverse $I P^{-1}$.
- The round function $F$ on 32 bits consists in 4 steps.
- Expansion $E$ which maps 32 bits in 48 bits by duplicating half of the bits.
- $\oplus$ with the 48 bits of round key $K_{j}$, $j \in \llbracket 1,16 \rrbracket$.
- 8 S-boxes $S_{i}$ : boolean functions $6 \rightarrow 4$
- Permutation $P$ of 32 bits.


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## S-boxes

- S-boxes $S_{i}, i \in \llbracket 1,8 \rrbracket$ substitute a 6 -bits input $m_{i}$ for a 4 -bits output $y_{i}$.
- $S_{i}\left(m_{i}\right)=y_{i}$
- S-boxes are represented with a table of 4 lines and 16 columns.
- Let $m_{i}$ be one input, the first and the last bit establish the line number. The bits in the middle establish the column number. To sum up $m_{i}$ defines the position in the s-box of a cell and $y_{i}$ defines the value in the same cell.



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## First FIRE attack [?]

- A single bit fault occurs in $R 15$.
- $C$ and $C^{*}$ are known thus $L 16, R 16, L 16^{*}$ and $R 16^{*}$ can be obtained with $I P$.
- $m=E(R 15) \oplus K 16=E(L 16) \oplus K 16$
$m^{*}=E\left(R 15^{*}\right) \oplus K 16=E\left(L 16^{*}\right) \oplus K 16$
- L15 is unknown, the s-boxes outputs $y$ and $y^{*}$ cannot be retrieved.
$y=P^{-1}(R 16 \oplus L 15)$
$y^{*}=P^{-1}\left(R 16^{*} \oplus L 15\right)$
- $\Delta_{y}=y \oplus y^{*}=P^{-1}\left(R 16 \oplus R 16^{*} \oplus L 15 \oplus L 15\right)=$ $P^{-1}\left(R 16 \oplus R 16^{*}\right)$
- $S_{i}\left(m_{i}\right) \oplus S_{i}\left(m_{i}^{*}\right)=\Delta_{y_{i}}$

- S-boxes are defined up to a translation.
- They finish with an exhaustive search.



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## The Attack Path

- A single-bit fault is injected in $R 14$.
- The fault is more propagated than in $R 15$, i.e. more bits in the s-boxes inputs of the last round are faulted.
- In $R 15$ two s-boxes can have faulty inputs i.e 1 or 2 different impacted s-boxes.
- In $R 14$ all s-boxes can have faulty inputs i.e $1,2,3,4,5,6,7$ or 8 different impacted s-boxes.

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## Propagation of the faulty bits

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(2) After S-boxes of round 15 , the numbers of faulty bits can be equal at 8 .
(3) Finally thank to the $E$ in round 16 , the numbers of faulty bits can be equal at 16 .
(3) The permutation $P$ dispatches the faulty bits and the 8 s-boxes can have faulty inputs.


## Inputs are known

- As in [?] $R 16, L 16, R 16^{*}$ and $L 16^{*}$ are known.

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## Inputs are known

- As in [?] R16, L16, R16* and $L 16^{*}$ are known.
$\Rightarrow$ Thus the inputs of s-boxes $m$ and $m^{*}$ are known.


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## Differential outputs are unknown

- As in [?] $R 16, L 16, R 16^{*}$ and $L 16^{*}$ are known.
$\Rightarrow$ the inputs of s-boxes $m$ and $m^{*}$ are known.
- $R 14^{*}=L 15^{*} \neq L 15$.
$\Rightarrow \Delta_{y}=P^{-1}\left(R 16 \oplus R 16^{*} \oplus L 15 \oplus L 15^{*}\right)$ is unknown.


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- We can known the differential at the outputs s-boxes in round 15.
- Finally we have only two possible fault values in R14*.
- This uncertainty in taken in account in $\Delta_{y}$.



## S-box properties

We can consider two properties of s-boxes justified by Brickell in [?].
(1) Changing 1 input bit of an s-box results in changing at least 2 output bits.
(2) Each line of an s-box is a permutation of the integers 0 to 15 .


## FIRE DES

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Statistics about the number of faults necessary to succeed an attack (estimated from 1000 attacks)

| statistic <br> tool | without <br> P 1 and P2 | with <br> P 1 and P2 |
| :---: | :---: | :---: |
| mean | 423.07 | 234.76 |
| standard derivation | 63.30 | 34.08 |
| median | 413 | 231 |
| minimum | 313 | 168 |
| maximum | 654 | 394 |

## Exhaustive search

The results are for 100 attacks with different numbers of faults

| Number <br> of faults | Average of number <br> of s-boxes which <br> are retrieved <br> up to a translation | Median of maximal <br> number of guesses <br> to define s-boxes <br> up to a translation | Maximum number <br> of guesses <br> to totaly <br> define s-boxes |
| :---: | :---: | :---: | :---: |
| 120 | 0.04 | $4.549 \cdot 10^{42}$ | $2^{174}$ |
| 140 | 0.89 | $9.5105 \cdot 10^{14}$ | $2^{82}$ |
| 160 | 2.76 | 62208 | $2^{47}$ |
| 180 | 4.53 | 16 | $2^{36}$ |
| 200 | 6.06 | 8 | $2^{35}$ |
| 220 | 6.93 | 4 | $2^{33}$ |
| 240 | 7,5 | 0 | $2^{32}$ |



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## Bibliographie

## Bibliographie I

## Thank you for your attention

Do you have any questions?


