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# Flavour physics and flavour symmetries after the first LHC phase

R. Barbieri,<sup>a</sup> D. Buttazzo,<sup>b</sup> F. Sala<sup>c</sup> and D.M. Straub<sup>d</sup>

<sup>a</sup>*Scuola Normale Superiore and INFN,  
Piazza dei Cavalieri 7, 56126 Pisa, Italy*

<sup>b</sup>*TUM Institute for Advanced Study,  
Lichtenbergstr. 2a, 85747 Garching, Germany*

<sup>c</sup>*Institut de Physique Théorique, CNRS and CEA/Saclay,  
91191 Gif-sur-Yvette, France*

<sup>d</sup>*Excellence Cluster Universe, TUM,  
Boltzmannstr. 2, 85748 Garching, Germany*

*E-mail:* [barbieri@sns.it](mailto:barbieri@sns.it), [dario.buttazzo@tum.de](mailto:dario.buttazzo@tum.de), [filippo.sala@cea.fr](mailto:filippo.sala@cea.fr),  
[david.straub@tum.de](mailto:david.straub@tum.de)

**ABSTRACT:** Based on flavour symmetries only, there are two ways to give rise to an effective description of flavour physics in the quark sector close to the CKM picture: one is based on  $U(3)_q \times U(3)_u \times U(3)_d$  (or equivalent) and the other on  $U(2)_q \times U(2)_u \times U(2)_d$  (or equivalent). In this context we analyze the current status of flavour physics measurements and we compare their impact, in the specific case of supersymmetry, with the direct searches of new particles at the LHC, present or foreseen.

**KEYWORDS:** Beyond Standard Model, Rare Decays, Supersymmetric Standard Model, CP violation

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## 1 Introduction

Which impact can flavour measurements have as a whole on the medium term future of particle physics? There are at least two different ways to try to address this question. One way is to consider the highest energies that flavour measurements can probe by taking a blind attitude on the possible structure of flavour physics: as well known these energies can extend in some cases up to  $10^{4\div 5}$  TeV. Opposite to this is the view that new flavour physics phenomena may be related to Beyond the Standard Model (BSM) physics in the TeV range, if there is any, still compatible with current LHC bounds. In this work we reexamine the latter case.

The current overall status of flavour measurements in the quark sector shows consistency with the Cabibbo-Kobayashi-Maskawa (CKM) picture of flavour physics with an uncertainty at 20 to 30% level (see below). From an effective field theory point of view the CKM picture, as embedded in the Standard Model (SM), amounts to the presence of a limited number of operators with a flavour dependence accounted for by a specific combination of CKM matrix elements. In view of this, it is interesting to consider an effective picture close enough to the CKM one, as just defined, based on symmetries and on their possible breaking pattern only, without referring to specific models or to appropriately

chosen dynamical assumptions. The well known example goes under the name of Minimal Flavour Violation (MFV) [1–3] and is based on the flavour symmetry in the quark sector of the SM

$$U(3)_q \times U(3)_u \times U(3)_d \equiv U(3)^3, \quad (1.1)$$

only broken by the Yukawa matrices transforming under this group, like spurions, as

$$Y_u = (3, \bar{3}, 1), \quad Y_d = (3, 1, \bar{3}). \quad (1.2)$$

As we are going to illustrate, at least within continuous symmetries, there seems to be effectively a single other CKM-like pattern, as arising from [4, 5]

$$U(2)_q \times U(2)_u \times U(2)_d \equiv U(2)^3, \quad (1.3)$$

broken by

$$\Delta_u = (2, \bar{2}, 1), \quad \Delta_d = (2, 1, \bar{2}), \quad \mathcal{V} = (2, 1, 1). \quad (1.4)$$

$U(2)^3$  is the flavour symmetry of the SM in the quark sector if only the top and the bottom Yukawa couplings  $y_t$  and  $y_b$  are kept. For this reason, unlike  $U(3)^3$ ,  $U(2)^3$  is an approximate symmetry of the observed quark flavour structure with all the parameters in eq. (1.4) small, at a few  $10^{-2}$  or less. While  $U(2)^3$  has been considered in the literature as a limiting cases of  $U(3)^3$  broken by the parameters in eq. (1.2) when both  $y_t$  and  $y_b$  are large [6, 7], hence large  $\tan \beta$ , this is not a logical necessity.

In a specific model of new physics at the TeV scale, there may be different ways to make it compatible with flavour physics measurements. Nevertheless, the generality of the approach described so far makes relevant to compare it with the current status of flavour physics measurements, as we do in the first part of the paper. In the second part of the paper we shall make a detailed comparison of flavour measurements with the direct searches of new particles in the case of supersymmetry, supplemented with the dynamical assumption that the stops and the sbottoms are generally lighter than squarks of the first and second generations. Within this framework, we also quantify the strong impact of the recent upper bound on the electron EDM.

## 2 Effective operators

For ease of the reader we recall the general structure of the effective operators that result in the two different CKM-like patterns.

Let us consider first the  $U(3)^3$  case, which leads to MFV. By uninfluent transformations inside the flavour symmetry group one can diagonalize the up quark mass matrix, so that the only non-trivial flavour structure comes from the diagonalization of the down quark mass matrix. It then follows, working to first order in all the flavour breaking parameters except  $y_t$ , that the only quark bilinears that are consistent with the symmetries and may produce a breaking of flavour after going to the physical quark bases are

$$\bar{Q} I_3 \gamma_\mu Q, \quad \bar{Q} I_3 Y_d (1, \sigma_{\mu\nu}) \mathcal{D} \quad (2.1)$$

where  $\mathcal{Q}$  and  $\mathcal{D}$  are triplet vectors in family space,  $I_3$  is the diagonal matrix with only the 33 element non zero and  $Y_d$  is the down Yukawa matrix. In turn, by going to the physical bases, this leads to the following set of relevant operators ( $\xi_{ij} = V_{tj}V_{ti}^*$  where  $V$  is the CKM matrix):

1.  $\Delta F = 2$ :

$$C_{LL}\xi_{ij}^2\frac{1}{2}(\bar{d}_{Li}\gamma_\mu d_{Lj})^2, \quad (2.2)$$

2.  $\Delta F = 1$ , chirality breaking ( $\alpha = \gamma, G$ ):

$$C^\alpha e^{i\chi^\alpha}\xi_{ij}(\bar{d}_{Li}\sigma_{\mu\nu}m_j d_{Rj})O_{\mu\nu}^\alpha, \quad O_{\mu\nu}^\alpha = eF_{\mu\nu}, \quad g_s G_{\mu\nu}, \quad (2.3)$$

3.  $\Delta F = 1$ , chirality conserving ( $\beta = L, R, H$ ):

$$C^\beta\xi_{ij}(\bar{d}_{Li}\gamma_\mu d_{Lj})O_\mu^\beta, \quad O_\mu^\beta = (\bar{l}_L\gamma_\mu l_L), (\bar{e}_R\gamma_\mu e_R), (H^\dagger D_\mu H). \quad (2.4)$$

In an effective Lagrangian approach, every operator is meant to be weighted by the square of an inverse mass scale  $1/\Lambda$ . The numerical coefficients  $C_{LL}, C^\alpha, C^\beta$  are of order unity and real and the only phases  $\chi^\alpha$  are made explicit in the chirality breaking operators.

The same effective operators are present in  $U(2)^3$ , except that more phases and relative factors of order unity between the third and the first two generations are introduced [4]. This comes about because of the reduced flavour group and the presence in eq. (1.4) of the doublet  $\mathcal{V}$ . It is no longer possible by transformations inside the flavour group to diagonalize the up quark mass matrix. Nevertheless, both the up and the down quark mass matrices, always working to first order in all the breaking parameters except  $y_t$ , can be diagonalized by pure transformations of the left handed fields only. Furthermore the presence of  $\mathcal{V}$ , introduces new quark bilinears other than those in eq. (2.1), that lead to a distinction between the third and the first two families other than the one contained in the CKM matrix. An example is  $\bar{Q}\mathcal{V}\gamma_\mu q_3$  with  $Q$  a doublet under  $U(2)_q$ . Consequently the explicit structure of the relevant effective operators in  $U(2)^3$  is:

1.  $\Delta B = 2, i = s, d$ :

$$c_{LL}^B e^{i\phi_B}\xi_{ib}^2\frac{1}{2}(\bar{d}_{Li}\gamma_\mu b_L)^2, \quad (2.5)$$

2.  $\Delta S = 2$ :

$$c_{LL}^K \xi_{ds}^2\frac{1}{2}(\bar{d}_L\gamma_\mu s_L)^2, \quad (2.6)$$

3.  $\Delta B = 1, i = s, d$ , chirality breaking ( $\alpha = \gamma, G$ ):

$$c^\alpha e^{i\phi^\alpha}\xi_{ib}m_b(\bar{d}_{Li}\sigma_{\mu\nu}b_R)O_{\mu\nu}^\alpha, \quad O_{\mu\nu}^\alpha = eF_{\mu\nu}, \quad g_s G_{\mu\nu}, \quad (2.7)$$

4.  $\Delta B = 1, i = s, d$ , chirality conserving<sup>1</sup> ( $\beta = L, R, H$ ):

$$c_B^\beta e^{i\phi^\beta}\xi_{ib}(\bar{d}_{Li}\gamma_\mu b_L)O_\mu^\beta, \quad O_\mu^\beta = (\bar{l}_L\gamma_\mu l_L), (\bar{e}_R\gamma_\mu e_R), (H^\dagger D_\mu H), \quad (2.8)$$

---

<sup>1</sup>There are also four-quark  $\Delta F = 1$  operators (the analogues of QCD penguins in the SM). While they are not relevant for the observables we consider below, they are relevant for mixing-induced CP asymmetries in non-leptonic penguin decays like  $B \rightarrow \phi K_S$  or  $B \rightarrow \eta' K_S$ , that can be generated in  $U(2)^3$  [8].

5.  $\Delta S = 1$ , chirality conserving:

$$c_K^\beta \xi_{ds} (\bar{d}_L \gamma_\mu s_L) O_\mu^\beta, \quad O_\mu^\beta = (\bar{l}_L \gamma_\mu l_L), (\bar{e}_R \gamma_\mu e_R), (H^\dagger D_\mu H). \quad (2.9)$$

### 3 Equivalent symmetries or symmetries that do not work

To the best of our knowledge every other symmetry inside  $U(3)^3$  either leads to one of the two patterns described above or deviates from a CKM-like picture because of the occurrence of different operators and/or of operators dependent on combinations of the CKM matrix elements different from  $\xi_{ij}$ .

A case that gives rise to MFV other than  $U(3)^3$  is

$$U(2)_q \times U(2)_u \times U(3)_d \equiv U(2)^2 \times U(3), \quad (3.1)$$

broken by

$$\Delta_u = (2, \bar{2}, 1), \quad \Delta_d = (2, 1, \bar{3}), \quad \tilde{\Delta}_d = (1, 1, \bar{3}). \quad (3.2)$$

That this be true simply follows from the fact that here as well one can diagonalize the up quark mass matrix by transformations inside the symmetry group and that the quark bilinears capable of producing a flavour breaking are the same as in eq. (2.1). Needless to say, here as in all previous cases, the directions of breaking specified by eq. (3.2) are as important as the symmetry itself. Once they are specified, there is no need to view  $U(2)^2 \times U(3)$  as a limiting case of  $U(3)^3$  broken by the parameters in eq. (1.2), due to the large  $y_t$  [6].

To maintain a CKM-like picture it is essential that one keeps some distinction between left and right fermions. Nevertheless one can for example reduce the  $U(2)^3$  group to

$$U(2)_q \times SU(2)_R \times U(1)_u \times U(1)_d \quad (3.3)$$

broken by

$$\tilde{\Delta}_u = (2, 2)_{(-1,0)}, \quad \tilde{\Delta}_d = (2, 2)_{(0,-1)}, \quad \tilde{\mathcal{V}} = (2, 1)_{(0,0)}. \quad (3.4)$$

Here  $SU(2)_R$  acts as a doublet on the first two generations of right handed up-type quarks, of  $U$ -charge 1, and, independently, on the first two generations of right handed down-type quarks, of  $D$ -charge 1. The distinction between  $\tilde{\Delta}_u$  and  $\tilde{\Delta}_d$  introduced by the  $U(1)$  factors is needed to prevent non CKM-like chirality breaking operators. To first order in these small breaking parameters, it is easy to see that this case leads to the same pattern as  $U(2)^3$ . Other symmetries that lead to the same pattern are conceivable.

We do not see how to obtain a different quasi-CKM picture of flavour physics by pure symmetry. An example that does not work but is nevertheless interesting is [9]

$$U(1)_{\tilde{B}_1} \times U(1)_{\tilde{B}_2} \times U(1)_{\tilde{B}_3} \times U(3)_d, \quad (3.5)$$

where  $\tilde{B}_i$  acts on  $\mathcal{Q}_i, u_i$  as baryon number, broken by

$$\Delta_1 = \bar{3}_{(-1,0,0)}, \quad \Delta_2 = \bar{3}_{(0,-1,0)}, \quad \Delta_3 = \bar{3}_{(0,0,-1)}. \quad (3.6)$$

Since the up quark mass matrix is diagonal to start with, the unitary matrix  $V$  that diagonalizes  $Y_d = VY_d^D U$  on the left is the CKM matrix. However the quark bilinear  $\bar{Q}_i c_i \gamma_\mu Q_i$ , invariant under the transformation (3.5), reduces in the physical basis for the down quarks to

$$((c_3 - c_1)\xi_{ij} + (c_2 - c_1)V_{cj}V_{ci}^*)(\bar{d}_{Li}\gamma_\mu d_{Lj}) \quad (3.7)$$

which is not CKM-like unless  $|c_2 - c_1| \ll |c_3 - c_1|$ . For  $|c_2 - c_1| = O(1)$  this extra term would lead, from its effects on  $\Delta S = 2$  transitions, to a bound on the scale  $\Lambda$  in the  $10^3$  TeV range. Similar considerations hold for the case analogous to (3.5) in which the right handed up-quarks  $u_i$  are interchanged with the the right handed down-quarks  $d_i$ , leading to a severe bound on  $\Lambda$ , in the hundreds of TeVs, from  $D^0$ - $\bar{D}^0$  mixing. Eqs. (3.5, 3.6) and the case with  $u_i$  reversed with  $d_i$  are, respectively, examples of models of alignment in the up and down sector. While alignment models can be successful in specific contexts, they appear not to work in the framework considered here.

## 4 Status of MFV and $U(2)^3$ in meson mixings

To determine the allowed room for new physics in meson mixings, a global fit of the CKM matrix has to be performed. In view of recent improved measurements, in particular the mixing induced CP asymmetry in  $B_s \rightarrow J/\psi\phi$  and  $B_s \rightarrow J/\psi f_0$  decays at LHCb that measures the  $B_s$  mixing phase, as well as recent progress in the determination of relevant hadronic parameters from lattice QCD, we update the fits in our previous work [4] for MFV and  $U(2)^3$ . In past years, the SM CKM fit has exhibited a sizable tension between the observables  $|\epsilon_K|$ ,  $S_{\psi K_S} = \sin(2\beta)$  and  $\Delta M_s/\Delta M_d$  [4, 5, 10, 11] that could be solved in  $U(2)^3$  models, but not in MFV. To reassess the status of this tension, we first perform a global CKM fit within the Standard Model.

### 4.1 Standard Model CKM fit

We perform global fits of the CKM matrix using a Bayesian approach. We construct a likelihood from the experimental inputs listed in table 1 and treat all the hadronic parameters listed there as nuisance parameters to be marginalized over. From the full fit to all the relevant constraints, we obtain<sup>2</sup>

$$A = 0.823 \pm 0.014, \quad \bar{\rho} = 0.142 \pm 0.020, \quad \bar{\eta} = 0.341 \pm 0.012 \quad (\text{full fit}). \quad (4.1)$$

To identify a possible tension between  $S_{\psi K_S}$  and  $\epsilon_K$ , we perform two additional fits, leaving one of the two constraints out of the fit and thereby finding a “fit prediction” valid within the SM. We find

$$A = 0.815 \pm 0.015, \quad \bar{\rho} = 0.157 \pm 0.024, \quad \bar{\eta} = 0.369 \pm 0.028, \quad S_{\psi K_S} = 0.734 \pm 0.045 \quad (\text{no } S_{\psi K_S}) \quad (4.2)$$

$$A = 0.813 \pm 0.017, \quad \bar{\rho} = 0.147 \pm 0.019, \quad \bar{\eta} = 0.336 \pm 0.014, \quad \frac{|\epsilon_K|}{10^{-3}} = (1.97 \pm 0.23) \quad (\text{no } \epsilon_K). \quad (4.3)$$

---

<sup>2</sup>The fitted value of  $\lambda$  is given by the input value of  $|V_{us}|$  to an excellent precision.

$ V_{ud} $	$0.97425(22)$	[12]	$f_K$	$(156.3 \pm 0.8) \text{ MeV}$	[12]
$ V_{us} $	$0.2249(8)$	[12]	$\hat{B}_K$	$0.766 \pm 0.010$	[12]
$ V_{cb} $	$(40.9 \pm 1.0) \times 10^{-3}$	[13]	$\kappa_\epsilon$	$0.94 \pm 0.02$	[14]
$ V_{ub} $	$(3.75 \pm 0.46) \times 10^{-3}$	[13]	$f_{B_s} \sqrt{\hat{B}_s}$	$(262 \pm 10) \text{ MeV}$	[15]
$\gamma_{\text{CKM}}$	$(70.1 \pm 7.1)^\circ$	[13]	$\xi$	$1.225 \pm 0.031$	[15]
$ \epsilon_K $	$(2.229 \pm 0.010) \times 10^{-3}$	[16]	$\eta_{tt}$	$0.5765(65)$	[17]
$S_{\psi K_S}$	$0.679 \pm 0.020$	[18]	$\eta_{ct}$	$0.496(47)$	[19]
$\Delta M_d$	$(0.510 \pm 0.004) \text{ ps}^{-1}$	[18]	$\eta_{cc}$	$1.87(76)$	[20]
$\Delta M_s/\Delta M_d$	$(34.69 \pm 0.31)$	[18]			
$\phi_s$	$0.01 \pm 0.07$	[21]			

**Table 1.** Experimental inputs (left) and theoretical nuisance parameters (right) used in the  $\Delta F = 2$  fits.

Comparing to the experimental values in table 1, we find that the input value and fitted value for  $S_{\psi\phi}$  as well as the input value and fitted value for  $|\epsilon_K|$  both deviate by  $1.1\sigma$ . We conclude that the data still prefer a negative contribution to the  $B_d$  mixing phase  $\phi_d = 2\beta + \phi_d^\Delta$  and/or a positive contribution to  $|\epsilon_K|$ , but the significance of this tension has decreased compared to the past. The main reasons for this change are the larger uncertainty in the QCD correction of the charm quark contribution to  $\epsilon_K$  [20] as well as the significant upward shift in the central value of the kaon bag parameter from an average of lattice calculations [12]. This conclusion is in line with recent fits by the UTfit collaboration [22] and is also in agreement with fits by the CKMfitter collaboration [23].

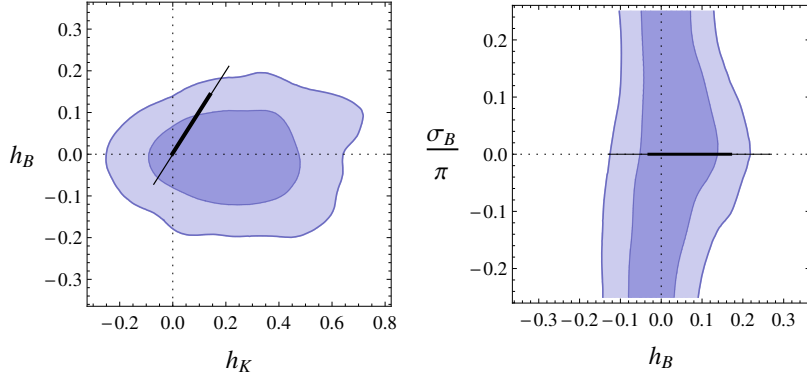
#### 4.2 $U(2)^3$ and MFV fits

In any new physics theory, contributions to the meson-antimeson mixing amplitudes in the  $K$ ,  $B_d$  and  $B_s$  systems can be written as

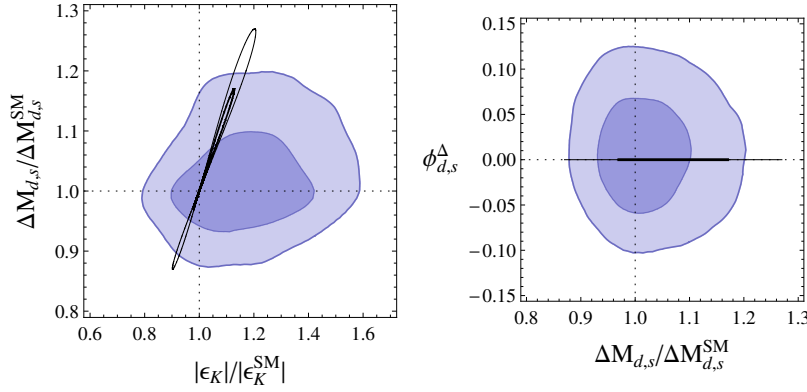
$$M_{12}^K = (M_{12}^K)_{\text{SM}} (1 + h_K e^{2i\sigma_K}), \quad M_{12}^{d,s} = (M_{12}^{d,s})_{\text{SM}} (1 + h_{d,s} e^{2i\sigma_{d,s}}). \quad (4.4)$$

Minimally broken  $U(2)^3$  makes the prediction  $\sigma_K = 0$ ,  $h_d = h_s \equiv h_B$ , and  $\sigma_d = \sigma_s \equiv \sigma_B$ , while MFV implies  $\sigma_K = \sigma_d = \sigma_s = 0$  and  $h_d = h_s = h_K \equiv h$ . In both cases, the correlation between  $B_d$  and  $B_s$  mixing implies that the ratio of mass differences  $\Delta M_s/\Delta M_d$ , which has a smaller theory uncertainty than the individual mass differences, is not modified. In the  $U(2)^3$  case, one has in addition a correlated shift in the mixing induced CP asymmetries  $S_{\psi K_S}$  and  $S_{\psi\phi}$ , while these observables are SM-like in MFV. We have seen that the data prefers a positive  $h_K$  as well as a positive contribution to the  $B_d$  mixing phase, while a new physics contribution to the  $B_s$  mixing phase is constrained already rather strongly. To quantify the impact on the parameter space of  $U(2)^3$  and MFV, we have performed two CKM fits, in the first case varying the  $U(2)^3$  parameters  $h_K$ ,  $h_B$  and  $\sigma_B$  in addition to the CKM Wolfenstein parameters and nuisance parameters and in the second case varying the single new parameter  $h$  present in MFV.





**Figure 1.** Results of the  $U(2)^3$  CKM fit. The dark and light regions correspond to 68% and 95% probability, respectively. The segments show the corresponding results for MFV, the thick and thin lines corresponding to 68% and 95% probability.



**Figure 2.** Results of the  $U(2)^3$  CKM fit. The dark and light regions correspond to 68% and 95% probability, respectively. The black regions show the corresponding results for MFV, the thick and thin lines corresponding to 68% and 95% probability.

The fit results for  $U(2)^3$  are shown in figure 1. It shows a preference for  $h_K > 0$  caused by the  $\epsilon_K$  tension, while there is no clear preference for a non-zero value of the CP-violating phase  $\sigma_B$ . This is due to the limited allowed room for new physics in the phase  $\phi_s$ , which precludes a sizable negative contribution to the  $B_d$  mixing phase, that would otherwise be preferred. The fit result in the MFV case is  $h = 0.07 \pm 0.10$  and is shown in the same figure as a black line. Here, the preference for a positive  $h$  is much milder, since a positive contribution to  $\epsilon_K$  would also imply a positive contribution to  $\Delta M_d$ , which is not preferred by the data.

The parameters  $h_K$ ,  $h_B$  and  $\sigma_B$  can also be related to measurable quantities by means of the relations

$$\frac{\Delta M_{d,s}}{\Delta M_{d,s}^{\text{SM}}} = |1 + h_B e^{2i\sigma_B}|, \quad \phi_{s,d}^{\Delta} = \arg(1 + h_B e^{2i\sigma_B}), \quad \frac{|\epsilon_K|}{|\epsilon_K^{\text{SM}}|} \approx 1 + \frac{|\epsilon_K^{tt,\text{SM}}|}{|\epsilon_K^{\text{SM}}|} h_K \quad (4.5)$$

where we used the conventions

$$\phi_s = -2|\beta_s| + \phi_s^\Delta, \quad S_{\psi K_S} = \sin(2\beta + \phi_d^\Delta). \quad (4.6)$$

The best-fit results for these observable quantities are shown in figure 2, again showing the result for the MFV fit as black lines.<sup>3</sup>

The correspondence between the phenomenological  $h$  parameters in eq. (4.4) and the coefficients  $C$  in eqs. (2.2) and (2.5), (2.6) is given by

$$h \approx C \left[ \frac{3.1 \text{ TeV}}{\Lambda} \right]^2, \quad (4.7)$$

so that, for  $C = 1$ , the current measurements are probing scales of about 4 to 7 TeV.

With similar coefficients, the  $\Delta F = 1$  operators in section 2 are at present generally less constrained than the  $\Delta F = 2$  operators discussed in this section.<sup>4</sup> We shall nevertheless elaborate on them, making this statement more precise, in the specific case of supersymmetry, dealt with in the rest of the paper.

## 5 Status of flavour physics in SUSY $U(2)^3$

As seen in the previous section, in minimally broken  $U(2)^3$  models the data still allow for a 20% enhancement of  $\Delta M_{d,s}$ , a 60% enhancement of  $\epsilon_K$  and a contribution to the  $B_{d,s}$  mixing phases of  $\pm 0.1$  rad. In supersymmetry, whether such values can be reached — i.e. whether  $\Delta F = 2$  observables still present a relevant constraint — depends crucially on the direct bounds on sparticle masses set by the LHC experiments. In this section, we first carefully derive all the relevant SUSY contributions to meson mixing, then discuss the LHC bounds on sparticle masses, and finally perform a numerical analysis of the allowed  $\Delta F = 2$  effects in SUSY  $U(2)^3$ . The supersymmetric spectrum that we have in mind is motivated by naturalness with, as its main feature, first and second generation squarks heavier than all other supersymmetric particles.

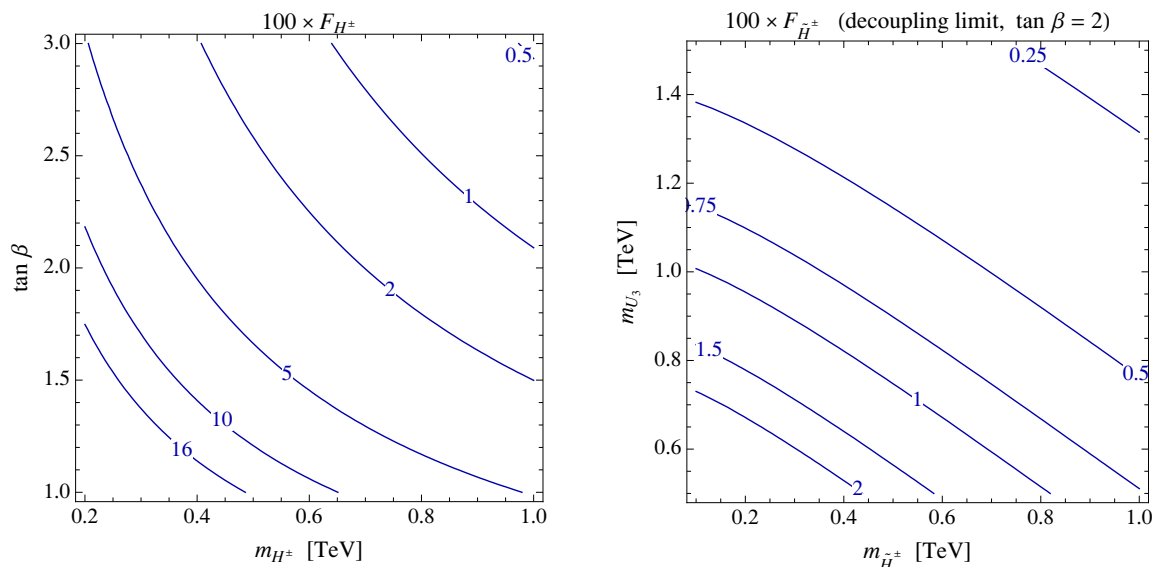
### 5.1 Anatomy of SUSY contributions to meson mixing

The dominant contributions to  $\Delta F = 2$  observables in SUSY  $U(2)^3$  come from gluino, Wino, Higgsino and charged Higgs diagrams.<sup>5</sup> Previously [5], only gluino contributions were considered for simplicity but this approximation becomes questionable in view of the stringent LHC bounds on the gluino mass. Instead, we discuss all the relevant contributions in turn.

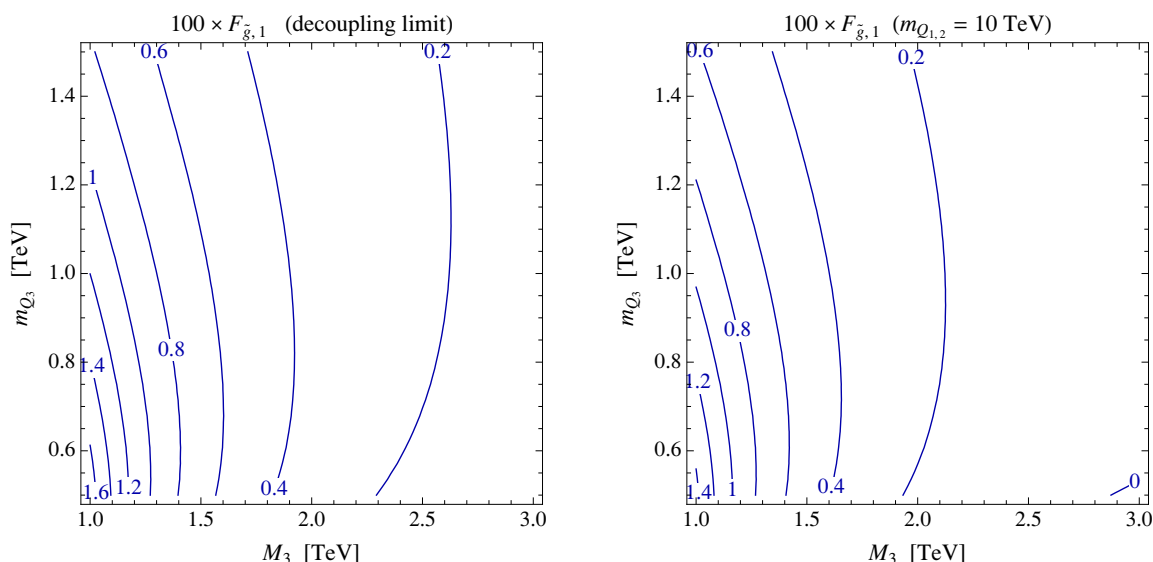
<sup>3</sup>In the left plot, the line spreads to a narrow region due to the uncertainty on the ratio  $|\epsilon_K^{tt,SM}|/|\epsilon_K^{SM}|$  in eq. (4.5).

<sup>4</sup>A possible exception is the  $\epsilon'/\epsilon$  constraint on the operators  $(\bar{s}_L \gamma_\mu d_L)(\bar{q}_R \gamma_\mu q_R)$  and  $(\bar{s}_L^\alpha \gamma_\mu d_L^\beta)(\bar{q}_R^\beta \gamma_\mu q_R^\alpha)$  [24]. In the case of supersymmetry that we will analyse, however, all contributions to such operators are further suppressed by the heaviness of the first generation squarks and/or by powers of small Yukawa couplings.

<sup>5</sup>Bino and mixed gluino-neutralino diagrams are typically subleading, but will be taken into account in the numerical analysis of section 5.3.



**Figure 3.** Charged Higgs and Higgsino contributions to  $\Delta F = 2$  observables.



**Figure 4.** “33” gluino contribution to meson mixings in the decoupling limit (left), and with degenerate first two generation squarks at 10 TeV (right).

**Charged Higgs and Higgsino contributions** Being proportional to the Yukawa couplings, they enter the  $K$ ,  $B_d$  and  $B_s$  mixing amplitudes universally and aligned in phase with the SM, just as in the case of  $U(3)^3$  (MFV). One can write

$$[h_K]_{H^\pm, \tilde{H}^\pm} = [h_B]_{H^\pm, \tilde{H}^\pm} \equiv F_{H^\pm} + F_{\tilde{H}^\pm}. \quad (5.1)$$

The functions  $F_{H^\pm}$  and  $F_{\tilde{H}^\pm}$  are shown in figure 3 as functions of the charged Higgs or Higgsino and right-handed stop masses,  $m_{H^\pm}$ ,  $m_{\tilde{H}^\pm}$  and  $m_{U_3}$ .

**Gluino contributions.** For the discussion of the relevant effects, it is useful to group the contributions with different squark flavours into “33”, “12”, and “12,3” contributions [9]. In the decoupling limit for the first two generation squarks considered in [5], the “12” and “12,3” contributions vanish and the “33” contribution only depends on the left-handed sbottom mass  $m_{Q_3}$ . Beyond this limit, there are three potentially relevant additional effects,

- for first and second generation squarks in the few TeV range, the “33” contribution has a non-negligible dependence on the first two generation squark masses (see figure 4), in particular when the gluino mass  $M_3 \gg m_{Q_3}$  since there is a numerical cancellation in the loop function of the leading contribution;
- since the first two generation squark masses are not exactly degenerate, there is a non-zero effect in the “12” and “12,3” contributions (see figure 5) that depends on an additional free  $O(1)$  parameter and is numerically relevant for  $K$  mixing;
- although right-handed flavour violation is strongly suppressed in minimally broken  $U(2)^3$ , it turns out that the contribution to the LR operator is not negligible in  $B_s$  mixing (see figure 6 left). We explicitly checked that all the non-gluino LR contributions are instead negligible.

The first and third points have also been discussed in [25]. The gluino contributions to the meson mixing amplitudes can thus be written as

$$[h_K]_{\tilde{g}} = |\xi_L|^4 F_{\tilde{g},1} + |\xi_L|^2 \delta_{12} F_{\tilde{g},2} + |\delta_{12}|^2 F_{\tilde{g},3}, \quad (5.2)$$

$$[h_d e^{2i\sigma_d}]_{\tilde{g}} = |\xi_L|^2 e^{2i\gamma_L} F_{\tilde{g},1}, \quad (5.3)$$

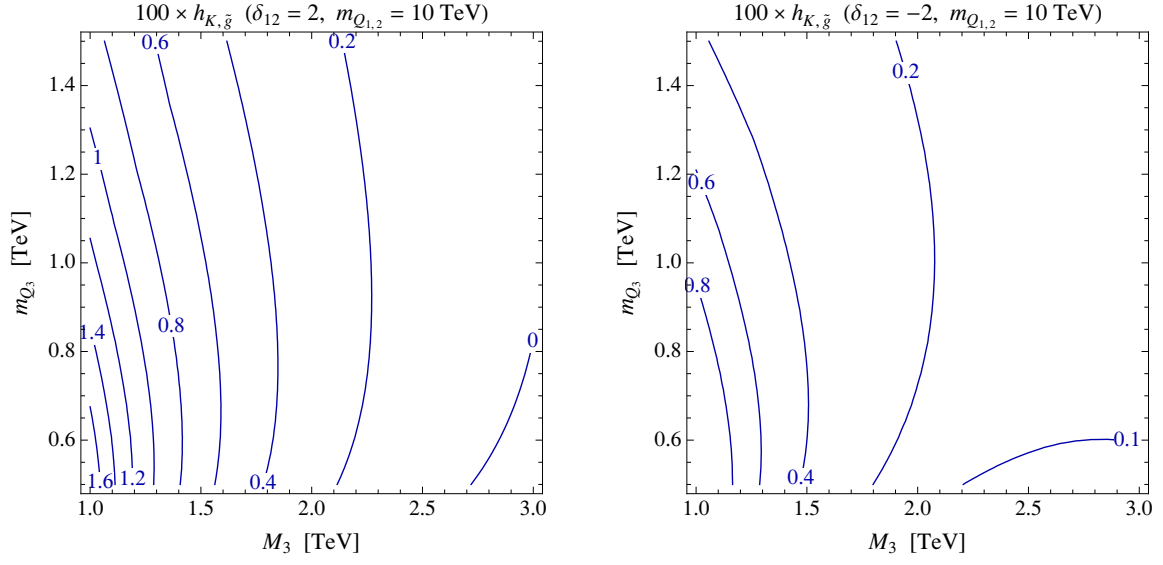
$$[h_s e^{2i\sigma_s}]_{\tilde{g}} = |\xi_L|^2 e^{2i\gamma_L} F_{\tilde{g},1} + |\xi_L \xi_R| e^{i(\gamma_L + \gamma_R)} F_{\tilde{g},4}, \quad (5.4)$$

where  $\xi_{L,R}$  and  $\delta_{12}$  are free  $O(1)$  parameters and  $\gamma_{L,R}$  are CP-violating phases [5, 8]. Note that the parameters  $\xi_R$  and  $\delta_{12}$  control effects that are of second order in the breaking parameters in eq. (1.4). Explicit analytic expressions for the loop-functions  $F_{\tilde{g},i}$  are given in the appendix.

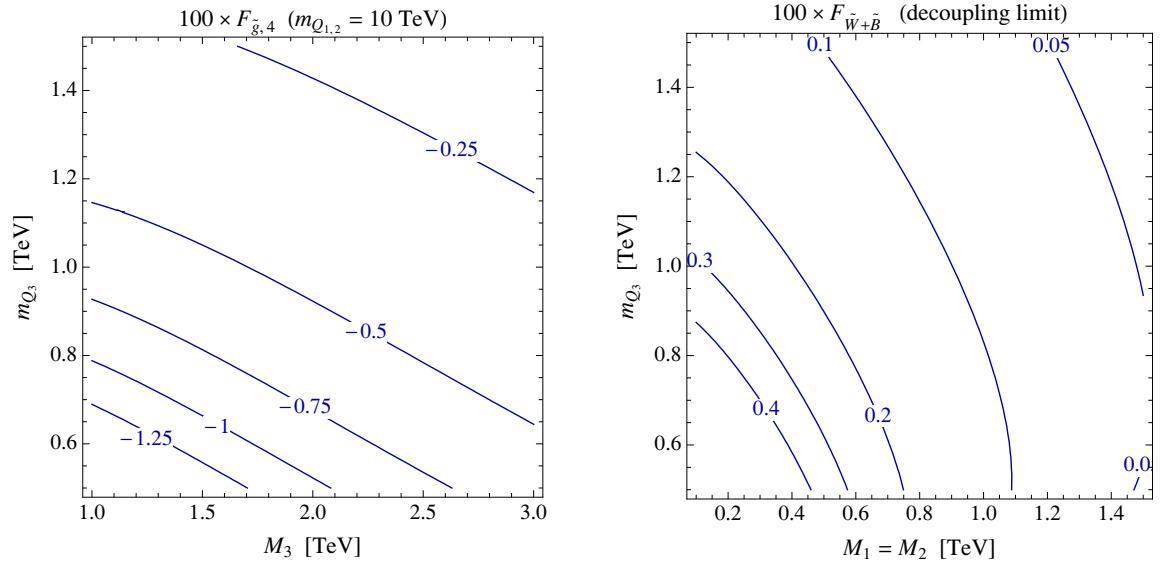
**Wino contributions** They are analogous to the gluino contributions discussed above. While they are parametrically suppressed by smaller gauge couplings compared to the gluino contributions, this can be compensated in practice by the much weaker bound on the Wino mass compared to the gluino mass. Bino and mixed Wino-Bino contributions are analogous, although further suppressed by powers of  $\sin \theta_w$  and thus negligible.

## 5.2 LHC mass bounds

To address the question of how large the effects in flavour physics can still be after the first LHC phase, we need to impose the bounds on sparticle masses resulting from various LHC searches. While a full analysis of this question is beyond the scope of the present study, experimental analyses of simplified models provide a rough indication of the exclusion ranges [26–49]. Throughout, we assume a neutralino LSP, decoupled first and second generations squarks, and decoupled sleptons.



**Figure 5.** Effect of the splitting between the first two generation squarks on the gluino contribution to  $h_K$ . Left:  $\delta_{12} = 2$  ( $m_{Q_1} > m_{Q_2}$ ). Right:  $\delta_{12} = -2$  ( $m_{Q_1} < m_{Q_2}$ ). The average heavy mass is 10 TeV and  $\xi_L = 1$ .



**Figure 6.** Left: Contribution of the LR gluino operator to  $B_s$  mixing; the first two generation squark masses are set to 10 TeV. Right: Wino contribution to meson mixings in the decoupling limit for the first two generations of squarks.

In the case of the gluino, searches for gluino pair production with four top quarks in the final state rule out a gluino below 1.4 TeV for LSP masses below 700 GeV if the mass difference between the gluino and the LSP is larger than  $2m_t$  [26–34]. If the mass difference is smaller than that, searches for events with light quark jets and missing energy rule out an LSP below 400 GeV [49].

Stops below about 700 GeV are ruled out for LSP masses below 200 GeV, unless the mass difference between the stop and LSP is below 200 GeV; in that case, there is still some room for a light stop [32, 35–41]. Similarly, sbottom squarks are excluded below 650 GeV for an LSP below 250 GeV [33, 40, 42].

We find no relevant bound on charginos and neutralinos, among those of [43–48], given our assumptions of heavy sleptons and a neutralino LSP. Notice also that we ignore the exclusion in the  $m_A$ - $\tan\beta$  plane from negative Higgs boson searches at LEP [50]. Despite being specific to the MSSM, it was cast for  $M_{\text{SUSY}} = 1$  TeV, and in the region of low  $\tan\beta$  where it is relevant a larger value of  $M_{\text{SUSY}}$  is required to reproduce the measured value of the Higgs mass [51].

### 5.3 Numerical analysis of meson mixing

Having identified the relevant contributions and their typical size, in this section we perform a numerical scan of the SUSY  $U(2)^3$  parameter space to identify the allowed effects in the  $\Delta F = 2$  observables. To this end, we scanned the relevant parameters in the following ranges,

$$m_{Q_3}, m_{U_3}, m_{D_3} \in [0.1, 1.5] \text{ TeV}, \quad M_3 \in [0.1, 3] \text{ TeV}, \quad (5.5)$$

$$m_{Q_{1,2}}, m_{U_{1,2}}, m_{D_{1,2}} \in [10, 30] \text{ TeV}, \quad |\mu| \in [0.1, 0.75] \text{ TeV}, \quad (5.6)$$

$$|M_1|, |M_2|, M_A \in [0.1, 0.8] \text{ TeV}, \quad A_{u,t}/m_{Q_3,U_3} \in [-1, 1], \quad (5.7)$$

$$A_{d,b}/m_{Q_3,D_3} \in [-1, 1], \quad \tan\beta \in [1, 5], \quad (5.8)$$

$$|\text{all } O(1) \text{ parameters}| \in [1/3, 3]. \quad (5.9)$$

We used log priors for the masses and linear priors for the dimensionless parameters. We scanned the phases of the  $O(1)$  parameters that are allowed to be complex, but assumed  $\mu, M_1, M_2$ , and the trilinears to be real. This is motivated by the recent result on the electron electric dipole moment and the considerations developed in section 5.5.

After computing the mass spectrum, we imposed the LHC direct bounds in a simplified manner as discussed in section 5.2. The points that survive after imposing these direct constraints either have stop and sbottom masses beyond 650 GeV and gluinos beyond 1.3 TeV, or they have a partially compressed spectrum with a small mass difference between the gluino and LSP or the stop and LSP. In the scatter plots presented below, we distinguished these two classes of spectra by dark blue and light blue points, respectively.

Finally, we used `SUSY-FLAVOR 2.10` [52] to compute flavour observables. To provide a check of the numerical results we have constructed an independent program, finding very good agreement. We imposed the constraint from the branching ratio of  $B \rightarrow X_s \gamma$  at  $2\sigma$  (the points not passing this constraint are shown in light gray in the plots). The  $B_s \rightarrow \mu^+ \mu^-$  constraint is irrelevant at the low values of  $\tan\beta$  we are considering. The range  $\tan\beta = 1 \div 5$

is chosen because it makes easier to accommodate in the Next to Minimal Supersymmetric Standard Model a 125 GeV Higgs boson with stops below 1 TeV and because of the  $B \rightarrow X_s \gamma$  and electron EDM constraints discussed in the following sections.

The predictions for the  $\Delta F = 2$  observables are shown in figure 7. In all the plots, the red star shows the SM value. The dotted black line in the first two upper plots corresponds to the  $U(3)^3$  limit of a CKM-like phase in  $B_{d,s}$  and  $K$  mixing. As discussed in section 5.1, this limit is adhered to by the Higgs and Higgsino contributions. In the two lower plots, the solid black line corresponds to the  $U(2)^3$  limit of universality in  $b \rightarrow d, s$  transitions. We stress that the violation of this limit visible in the plots is not due to the uncertainty in CKM parameters — since we plot only the ratio of mass differences and the new physics contribution to the mixing phase, these uncertainties cancel out — but it is due to the contribution of the LR operator to  $B_s$  mixing discussed in section 5.1.<sup>6</sup> In all the plots, the dashed black contour is the 95% probability region allowed in the  $U(2)^3$  CKM fit of section 4.2 (cf. figure 2). For comparison, we also show as gray dashed contours the allowed regions in a more general fit not requiring universality of  $B_d$  and  $B_s$  mixing. In this case, a sizably negative value of  $\phi_d^\Delta$  is allowed because of the  $\sin(2\beta)$  tension.

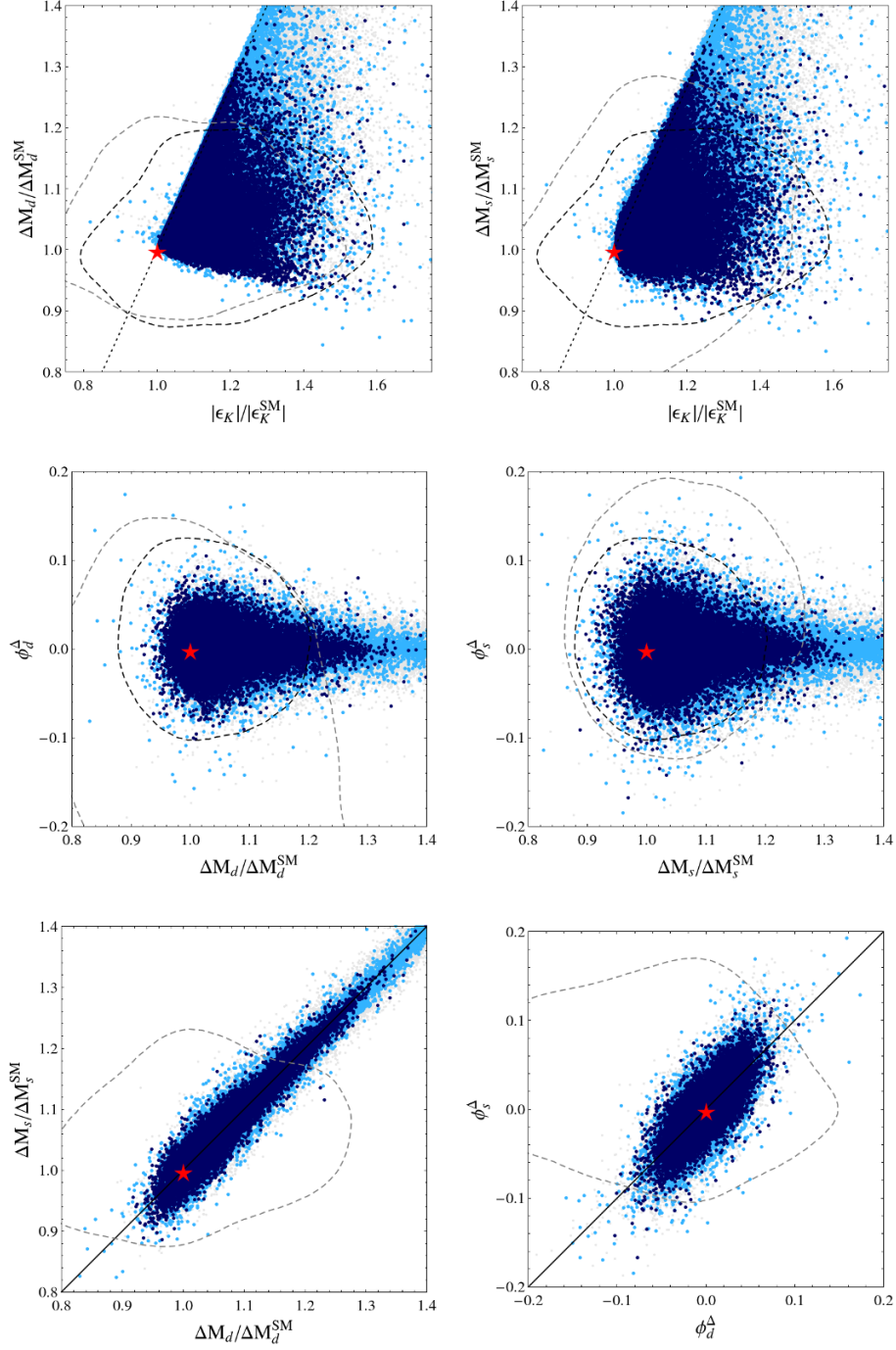
#### 5.4 Predictions for rare $B$ decays

Gluino contributions to rare  $B$  decay amplitudes have been discussed by us in ref. [8], where we showed that the main new effects in  $U(2)^3$  arise from the magnetic and chromomagnetic dipole operators. In addition to the gluino (and Wino) contributions, which are proportional to  $e^{i\gamma_L}$  and hence contribute to CP asymmetries in  $B$  decays, there are the usual MFV-like Higgsino and charged Higgs contributions to dipole operators, that are aligned in phase with the SM contribution and are mainly constrained by the branching ratio of  $B \rightarrow X_s \gamma$ . The most promising observable to probe the CP-violating contributions is the angular CP asymmetry  $A_7$  in the  $B \rightarrow K^* \mu^+ \mu^-$  decay at low dimuon invariant mass  $q^2$  [54, 55]. Correlated with this, contributions to the mixing-induced CP asymmetries in non-leptonic penguin decays like  $B \rightarrow \phi K_S$  or  $B \rightarrow \eta' K_S$  will be generated by the CP violating contribution to the chromomagnetic dipole operator [8].

Figure 8 shows numerical results for the branching ratio of  $B \rightarrow X_s \gamma$  vs. the CP asymmetry  $A_7$  integrated in  $q^2$  from 1 to 6 GeV<sup>2</sup>. The scan ranges and the colours are as in section 5.3. While the MFV-like contributions can lead to large modifications of the branching ratio that are constrained experimentally, the effects in  $A_7$  are limited due to the strong direct bounds, in particular on the gluino mass.

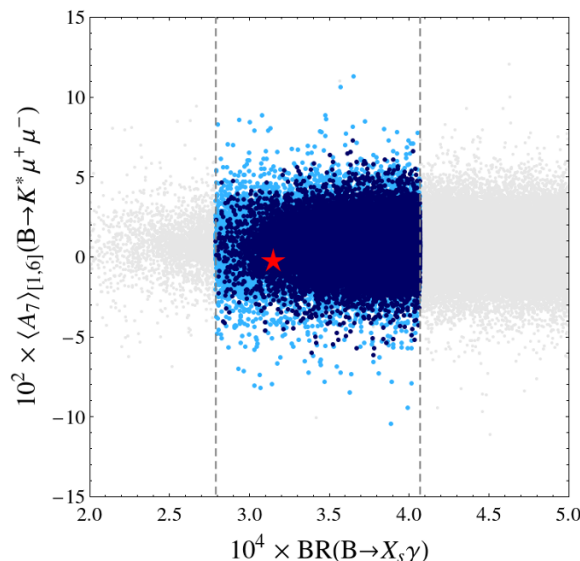
We note here that for  $\Delta B = 1$  processes, the parameter  $\tan \beta$  plays a more important role than for  $\Delta B = 2$  processes. First, this is because the dipole operators change chirality and hence in general they can receive  $\tan \beta$  enhanced contributions. Second, there are the  $B_{s,d} \rightarrow \mu^+ \mu^-$  decays which receive strongly  $\tan \beta$  enhanced contributions from scalar operators. Here, we focus on the regime  $\tan \beta \lesssim 5$ , where the branching ratios of  $B_{s,d} \rightarrow \mu^+ \mu^-$  are modified by at most 30% with respect to the SM.

<sup>6</sup>Notice that this contribution also blurs the  $V_{ub}-S_{\psi\phi}-S_{\psi K_S}$  correlation pointed out in [53].



**Figure 7.** Correlation between  $\Delta F = 2$  observables. Dark and light blue points are allowed by all direct constraints, light blue points have a compressed spectrum (see text for details), light gray points are ruled out by  $B \rightarrow X_s \gamma$ . The red star is the SM. The black dashed line is the 95% C.L. region allowed by the global CKM fit imposing the  $U(2)^3$  relations, the gray dashed line in a generic new physics fit. The dashed lines in the first row show the MFV limit, the solid lines in the last row the  $U(2)^3$  limit.





**Figure 8.** Branching ratio of  $B \rightarrow X_s \gamma$  vs. the angular CP asymmetry  $A_7$  in  $B \rightarrow K^* \mu^+ \mu^-$ , integrated from  $q^2 = 1$  to  $6 \text{ GeV}^2$ .

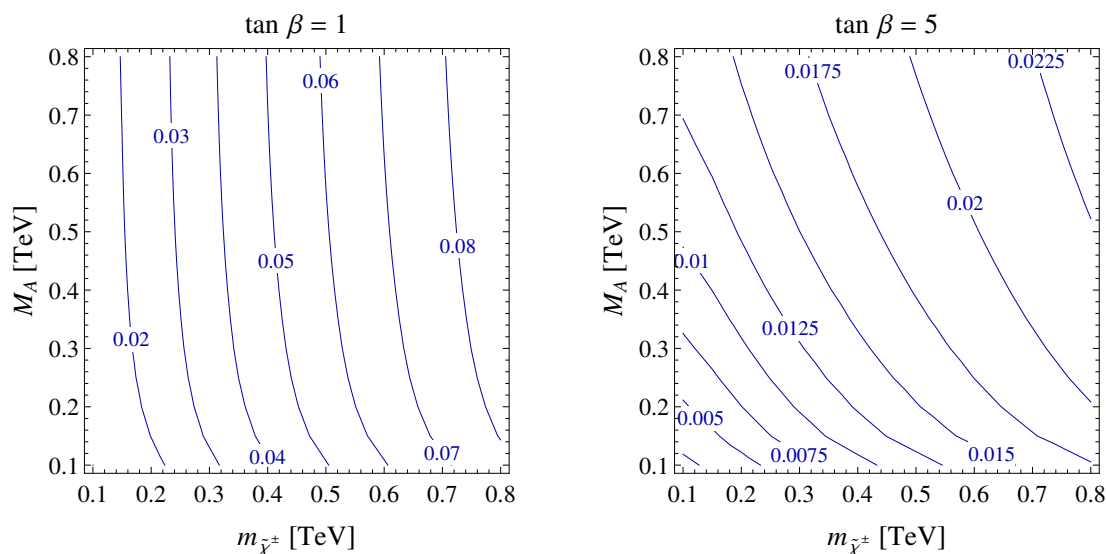
### 5.5 Electron electric dipole moment

Suppressing SUSY contributions to Electric Dipole Moments (EDM) is an additional motivation for a split squark spectrum, as it allows to have sizable CP-violating phases without excessive one-loop contributions to EDMs of first generation fermions. Recently, a new experimental bound on the electron EDM has been obtained [56],  $|d_e| < 8.7 \times 10^{-29} e \text{ cm}$ , that improves the previous bound [57] by a factor of 12. Here, we study the impact of this new bound on models with a split sfermion spectrum.

First, there is the direct one-loop contribution to the electron EDM involving charginos and sneutrinos, that decouples with the scale of the first generation sfermion masses. Updating the bound in [59], we find a lower bound on the sneutrino mass, depending on  $\tan \beta$  and the phase of the  $\mu$  term ( $\mu = |\mu| e^{i\phi_\mu}$ ),

$$m_{\tilde{\nu}_1} > 17 \text{ TeV} \times (\sin \phi_\mu \tan \beta)^{\frac{1}{2}}. \quad (5.10)$$

Second, there is a contribution from two-loop Barr-Zee type diagrams involving a chargino loop attached to the electron line by a Higgs and a gauge boson. This contribution is  $\tan \beta$  dependent and decouples with the chargino masses. We refer to [60–64] for explicit expressions for these contributions. In figure 9, we show the constraints on the phase of  $\mu$  obtained from these contributions for two different values of  $\tan \beta$ . We conclude that, even for very low  $\tan \beta$ , an  $O(1)$  phase of the  $\mu$  term is no longer viable with a natural SUSY spectrum that has Higgsinos below a TeV. We stress that this conclusion is independent of the mass of the heavy Higgses, since the light Higgs contribution does not decouple even if they are heavy, as can be seen in the upper part of the left-hand plot in figure 9.



**Figure 9.** Maximum value of the argument of the  $\mu$  term,  $\phi_\mu$ , allowed by two-loop contributions to the electron EDM, in the plane of the common chargino mass  $m_{\tilde{\chi}^\pm}$  and the pseudoscalar Higgs mass  $M_A$ .

## 6 Conclusions

The search for the production of new particles, as expected in BSM at the TeV scale, is a primary task of the next LHC phase. The exploration of most part of the sensitive region of parameter space in motivated theories is actually likely to take place in the relatively early stage of the new LHC phase. After that, whatever the findings of this exploration will be, precision measurements in flavour physics (and not only in flavour physics) may play a leading role for a sufficiently long period of time. With this in mind, we have asked which impact can flavour measurements have as a whole in the medium term future of particle physics. There is no general way to address this question. Yet the consistency of the CKM description of flavour physics with current data makes interesting to consider an effective picture close enough to the CKM one, based on symmetries and on their breaking patterns only. Under the stated assumptions we see two possible ways to go:  $U(3)^3$  (or MFV) and  $U(2)^3$  suitably broken. Needless to say we do not know the origin of these patterns at a fundamental level but we take them as a low energy property of some basic theory at an effective Lagrangian level.

Figure 1 and eq. (4.7) show that current flavour measurements probe scales up to 4 to 7 TeV, depending on the  $\Delta F = 2$  channel and with the MFV case more restricted. In  $\Delta F = 1$  channels the constraints are relatively weaker, with the single exceptions of  $B \rightarrow X_s \gamma$  and  $\epsilon'/\epsilon$ . Of the observables shown in figure 2, the measurement that should progress more is the one on  $\phi_s^\Delta$ , but an overall progress is expected on a long series of measurements in the next decade or so that should reduce the current 20% bound on  $h_B$  to about 5% [23]. In  $U(2)^3$  the bound on  $h_K$  should go down by about a factor of two,

although remaining relatively weaker than the one on  $h_B$ .

The comparison of the impact of these measurements with the direct searches of new particles can only be made in a specific context. In view of this we have chosen to consider supersymmetry with a flavour structure constrained by symmetries and with a spectrum suggested by naturalness considerations. The main feature of this spectrum, specified in eqs. (5.5), (5.6), is the heaviness of the squarks of the first two generations. Such a spectrum is at least consistent with a weakly broken  $U(2)^3$  symmetry. An interesting feature of supersymmetry and  $U(2)^3$  is that some of the virtual exchanges in flavour violating processes are effectively MFV-like whereas only Wino or gluino exchanges can produce a deviation from MFV.

A scan of the parameter space defined in eqs. (5.5)–(5.9) produces the scatter plots in figure 7, controlled by many partial analytic descriptions (see section 5.1). The ranges of parameters considered extend the regions explorable in direct searches at LHC in its second phase. While all the points are allowed by current direct searches, an important distinction is introduced between points corresponding to a “compressed” spectrum (light blue) and all other points (dark blue). Although the vast majority of the points are compatible with the constraints obtained by a general  $U(2)^3$  fit of current flavour measurements, the foreseen improvements described above may show a deviation from the SM in flavour physics, most likely corresponding to a spectrum whose lightest fragments should be visible in direct production as well in the second LHC phase. Note in the four upper figures the lines corresponding to MFV. On the contrary the oblique lines in the two lower figures show the correlations between  $s$  and  $d$  characteristic of  $U(2)^3$ , as described in eqs. (4.4), (4.5). The relatively small deviations from the perfect correlation appearing in these figures is due to the presence of second order effects in the small symmetry breaking parameters that produce a main contribution to the LR operator in  $B_s$  mixing (see section 5.1).

Everywhere in the consideration of possible supersymmetric signals we have taken  $\tan\beta$  below 5. Also because of this the current constraints on  $\Delta F = 1$  effects is dominated by the measurement of the  $B \rightarrow X_s \gamma$  rate, as shown in figure 8. Other measurements that should improve on the current situation are angular CP asymmetries and other observables in  $B \rightarrow K^{(*)} \bar{l} l$  decays and, in kaon physics, measurements of  $K \rightarrow \pi \nu \bar{\nu}$ .

A final point concerns the recently improved limit on the electron EDM. Depending on the value of  $\tan\beta$  and on the phase  $\phi_\mu$  of the  $\mu$  parameter, suitably defined, the new bound gives a severe constraint on the sneutrino mass of the first generation. More important for the considerations developed here, however, is the bound coming from two loop diagrams on the masses of the extra Higgs bosons and of charginos, illustrated in figure 9. A flavour blind phase of order one is not compatible any more with charginos below the TeV range. The separate origin of  $\phi_\mu$  from the phases appearing in the flavour violating operators in section 2 may explain the absence of signal in the EDM experiments so far. In any way this is quite a significant change with respect to the previous situation.

## Acknowledgments

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## A Loop functions for meson mixings

The relevant contributions to the meson mixings of section 5.1, coming from the box diagrams, can be expressed in terms of the Passarino-Veltman four-point loop functions at vanishing external momentum

$$D_0(m_1^2, m_2^2, m_3^2, m_4^2) = \frac{1}{i\pi^2} \int d^4p \frac{1}{(p^2 - m_1^2)(p^2 - m_2^2)(p^2 - m_3^2)(p^2 - m_4^2)}, \quad (\text{A.1})$$

$$D_2(m_1^2, m_2^2, m_3^2, m_4^2) = \frac{1}{i\pi^2} \int d^4p \frac{p^2/4}{(p^2 - m_1^2)(p^2 - m_2^2)(p^2 - m_3^2)(p^2 - m_4^2)}. \quad (\text{A.2})$$

We define the functions

$$f_\alpha(x, y, z) = c_{0,\alpha} m_\alpha^2 D_0(xm_\alpha^2, ym_\alpha^2, zm_\alpha^2, m_\alpha^2) + c_{2,\alpha} D_2(xm_\alpha^2, ym_\alpha^2, zm_\alpha^2, m_\alpha^2), \quad (\text{A.3})$$

where  $\alpha = \tilde{g}, \tilde{W}, \tilde{B}, \tilde{H}^\pm, H^\pm, W^\pm, \tilde{g}_{(\text{LR})}$ , and the coefficients  $c_{0,\alpha}, c_{2,\alpha}$  are

	$\tilde{g}$	$\tilde{W}$	$\tilde{B}$	$\tilde{H}^\pm$	$W^\pm$	$H^\pm$	$\tilde{g}_{(\text{LR})}$
$c_0$	-8/9	-1/2	-1/162	0	2	0	-56/3
$c_2$	-88/9	-5	-1/81	-4	-2	-1	32/3

Writing for convenience  $f_\alpha(x, y) \equiv f_\alpha(x, y, 1)$ , the contributions to the gluino-induced mixing amplitudes, defined as in (5.2)–(5.4), then read

$$F_{1,\tilde{g}} = \frac{1}{S_0} \frac{m_W^2}{M_3^2} \frac{\alpha_3^2}{\alpha_2^2} K_1 \left( f_{\tilde{g}}(x_3, x_3) + f_{\tilde{g}}(x_1, x_1) - 2f_{\tilde{g}}(x_1, x_3) \right), \quad (\text{A.4})$$

$$F_{2,\tilde{g}} = \frac{1}{S_0} \frac{m_W^2}{M_3^2} \frac{\alpha_3^2}{\alpha_2^2} \left| \frac{\xi_2}{\xi_3} \right| K_2 \left( f_{\tilde{g}}(x_1, x_1) + f_{\tilde{g}}(x_3, x_2) - f_{\tilde{g}}(x_2, x_1) - f_{\tilde{g}}(x_3, x_1) \right), \quad (\text{A.5})$$

$$F_{3,\tilde{g}} = \frac{1}{S_0} \frac{m_W^2}{M_3^2} \frac{\alpha_3^2}{\alpha_2^2} \left| \frac{\xi_2}{\xi_3} \right|^2 K_3 \left( f_{\tilde{g}}(x_2, x_2) + f_{\tilde{g}}(x_1, x_1) - 2f_{\tilde{g}}(x_2, x_1) \right), \quad (\text{A.6})$$

$$F_{4,\tilde{g}} = \frac{1}{S_0} \frac{m_W^2}{M_3^2} \frac{\alpha_3^2}{\alpha_2^2} \frac{y_s}{y_b} K_4 \left( f_{\tilde{g}_{(\text{LR})}}(x_3, x_3) + f_{\tilde{g}_{(\text{LR})}}(x_1, x_1) - 2f_{\tilde{g}_{(\text{LR})}}(x_3, x_1) \right), \quad (\text{A.7})$$

where  $x_i = (m_{Q_i, U_i, D_i}/M_3)^2$ ,  $\xi_a^{ij} = V_{ai}^* V_{aj}$ , and  $S_0 \simeq 2.31$  is the corresponding SM loop function evaluated at  $\mu = m_t$ . The factors  $K_i$  include the effect of the running and operator

mixings [9, 65], as well as the hadronic matrix elements of the relevant operators [15, 66], normalised to the SM LL contribution. Analogous expressions hold for the other gaugino contributions. For the charged Higgs and Higgsino contributions (5.1) one obtains

$$F_{H^\pm} = \frac{1}{S_0} \frac{m_t^4}{m_W^2 m_{H^\pm}^2} K_1 \left( \frac{1}{t_\beta^4} f_{H^\pm}(x_t, x_t) + \frac{1}{t_\beta^2} f_{W^\pm}(x_t, x_t, x_{H^\pm}) \right), \quad (\text{A.8})$$

$$F_{\tilde{H}^\pm} = \frac{1}{S_0} \frac{m_W^2}{\mu^2} \frac{y_t^4}{g_2^4} \frac{1}{s_\beta^4} K_1 f_{\tilde{H}^\pm}(x_3, x_3). \quad (\text{A.9})$$

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## References

- [1] R.S. Chivukula and H. Georgi, *Composite Technicolor Standard Model*, *Phys. Lett. B* **188** (1987) 99 [[INSPIRE](#)].
- [2] L.J. Hall and L. Randall, *Weak scale effective supersymmetry*, *Phys. Rev. Lett.* **65** (1990) 2939 [[INSPIRE](#)].
- [3] G. D'Ambrosio, G.F. Giudice, G. Isidori and A. Strumia, *Minimal flavor violation: An Effective field theory approach*, *Nucl. Phys. B* **645** (2002) 155 [[hep-ph/0207036](#)] [[INSPIRE](#)].
- [4] R. Barbieri, D. Buttazzo, F. Sala and D.M. Straub, *Flavour physics from an approximate  $U(2)^3$  symmetry*, *JHEP* **07** (2012) 181 [[arXiv:1203.4218](#)] [[INSPIRE](#)].
- [5] R. Barbieri, G. Isidori, J. Jones-Perez, P. Lodone and D.M. Straub,  *$U(2)$  and Minimal Flavour Violation in Supersymmetry*, *Eur. Phys. J. C* **71** (2011) 1725 [[arXiv:1105.2296](#)] [[INSPIRE](#)].
- [6] T. Feldmann and T. Mannel, *Large Top Mass and Non-Linear Representation of Flavour Symmetry*, *Phys. Rev. Lett.* **100** (2008) 171601 [[arXiv:0801.1802](#)] [[INSPIRE](#)].
- [7] A.L. Kagan, G. Perez, T. Volansky and J. Zupan, *General Minimal Flavor Violation*, *Phys. Rev. D* **80** (2009) 076002 [[arXiv:0903.1794](#)] [[INSPIRE](#)].
- [8] R. Barbieri, P. Campli, G. Isidori, F. Sala and D.M. Straub,  *$B$ -decay  $CP$ -asymmetries in SUSY with a  $U(2)^3$  flavour symmetry*, *Eur. Phys. J. C* **71** (2011) 1812 [[arXiv:1108.5125](#)] [[INSPIRE](#)].
- [9] R. Barbieri, E. Bertuzzo, M. Farina, P. Lodone and D. Zhuridov, *Minimal Flavour Violation with hierarchical squark masses*, *JHEP* **12** (2010) 070 [Erratum *ibid.* **1102** (2011) 044] [[arXiv:1011.0730](#)] [[INSPIRE](#)].
- [10] E. Lunghi and A. Soni, *Possible Indications of New Physics in  $B_d$  -mixing and in  $\sin(2\beta)$  Determinations*, *Phys. Lett. B* **666** (2008) 162 [[arXiv:0803.4340](#)] [[INSPIRE](#)].
- [11] A.J. Buras and D. Guadagnoli, *Correlations among new  $CP$ -violating effects in  $\Delta F = 2$  observables*, *Phys. Rev. D* **78** (2008) 033005 [[arXiv:0805.3887](#)] [[INSPIRE](#)].
- [12] S. Aoki et al., *Review of lattice results concerning low energy particle physics*, [arXiv:1310.8555](#) [[INSPIRE](#)].

- [13] A. Bevan et al., *Standard Model updates and new physics analysis with the Unitarity Triangle fit*, *Nucl. Phys. Proc. Suppl.* **241-242** (2013) 89 [[INSPIRE](#)].
- [14] A.J. Buras, D. Guadagnoli and G. Isidori, *On  $\epsilon_K$  beyond lowest order in the Operator Product Expansion*, *Phys. Lett. B* **688** (2010) 309 [[arXiv:1002.3612](#)] [[INSPIRE](#)].
- [15] ETM collaboration, N. Carrasco et al., *B-physics from  $N_f = 2$  tmQCD: the Standard Model and beyond*, *JHEP* **03** (2014) 016 [[arXiv:1308.1851](#)] [[INSPIRE](#)].
- [16] PARTICLE DATA GROUP collaboration, J. Beringer et al., *Review of Particle Physics (RPP)*, *Phys. Rev. D* **86** (2012) 010001 [[INSPIRE](#)].
- [17] A.J. Buras, M. Jamin and P.H. Weisz, *Leading and Next-to-leading QCD Corrections to  $\epsilon$  Parameter and  $B^0 - \bar{B}^0$  Mixing in the Presence of a Heavy Top Quark*, *Nucl. Phys. B* **347** (1990) 491 [[INSPIRE](#)].
- [18] HEAVY FLAVOR AVERAGING GROUP collaboration, Y. Amhis et al., *Averages of B-Hadron, C-Hadron and tau-lepton properties as of early 2012*, [arXiv:1207.1158](#) [[INSPIRE](#)].
- [19] J. Brod and M. Gorbahn,  *$\epsilon_K$  at Next-to-Next-to-Leading Order: The Charm-Top-Quark Contribution*, *Phys. Rev. D* **82** (2010) 094026 [[arXiv:1007.0684](#)] [[INSPIRE](#)].
- [20] J. Brod and M. Gorbahn, *Next-to-Next-to-Leading-Order Charm-Quark Contribution to the CP-violation Parameter  $\epsilon_K$  and Delta  $M_K$* , *Phys. Rev. Lett.* **108** (2012) 121801 [[arXiv:1108.2036](#)] [[INSPIRE](#)].
- [21] LHCb collaboration, *Measurement of CP-violation and the  $B_s^0$  meson decay width difference with  $B_s^0 \rightarrow J/\psi K^+ K^-$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  decays*, *Phys. Rev. D* **87** (2013) 112010 [[arXiv:1304.2600](#)] [[INSPIRE](#)].
- [22] UTfit collaboration, *Updates on the Unitarity Triangle fit within and beyond the SM*, Talk at the UK Flavour Workshop, September 6th, 2013, Durham, UK and updates at [www.utfit.org](#).
- [23] J. Charles et al., *Future sensitivity to new physics in  $B_d, B_s$  and  $K$  mixings*, *Phys. Rev. D* **89** (2014) 033016 [[arXiv:1309.2293](#)] [[INSPIRE](#)].
- [24] R. Barbieri, D. Buttazzo, F. Sala and D.M. Straub, *Less Minimal Flavour Violation*, *JHEP* **10** (2012) 040 [[arXiv:1206.1327](#)] [[INSPIRE](#)].
- [25] G. Blankenburg and J. Jones-Perez, *RGE Behaviour of SUSY with a  $U(2)^3$  symmetry*, *Eur. Phys. J. C* **73** (2013) 2289 [[arXiv:1210.4561](#)] [[INSPIRE](#)].
- [26] ATLAS collaboration, *Search for new phenomena using final states with large jet multiplicities and missing transverse momentum with ATLAS in  $20 \text{ fb}^{-1}$  of  $\sqrt{s} = 8 \text{ TeV}$  proton-proton collisions*, [ATLAS-CONF-2013-054](#) (2013).
- [27] ATLAS collaboration, *Search for strong production of supersymmetric particles in final states with missing transverse momentum and at least three b-jets using  $20.1 \text{ fb}^{-1}$  of  $pp$  collisions at  $\sqrt{s} = 8 \text{ TeV}$  with the ATLAS Detector*, [ATLAS-CONF-2013-061](#) (2013).
- [28] ATLAS collaboration, *Search for strongly produced superpartners in final states with two same sign leptons with the ATLAS detector using  $21 \text{ fb}^{-1}$  of proton-proton collisions at  $\sqrt{s} = 8 \text{ TeV}$* , [ATLAS-CONF-2013-007](#) (2013).
- [29] CMS collaboration, *Search for gluino mediated bottom- and top-squark production in multijet final states in  $pp$  collisions at  $8 \text{ TeV}$* , *Phys. Lett. B* **725** (2013) 243 [[arXiv:1305.2390](#)] [[INSPIRE](#)].



- [30] CMS collaboration, *Search for supersymmetry in pp collisions at  $\sqrt{s} = 8$  TeV in events with a single lepton, large jet multiplicity and multiple b jets*, [arXiv:1311.4937](#) [[INSPIRE](#)].
- [31] CMS collaboration, *Search for new physics in events with same-sign dileptons and jets in pp collisions at  $\sqrt{s} = 8$  TeV*, *JHEP* **01** (2014) 163 [[arXiv:1311.6736](#)] [[INSPIRE](#)].
- [32] CMS collaboration, *Search for supersymmetry using razor variables in events with b-jets in pp collisions at 8 TeV*, [CMS-PAS-SUS-13-004](#) (2013).
- [33] CMS collaboration, *Search for supersymmetry in pp collisions at  $\sqrt{s} = 8$  TeV in events with three leptons and at least one b-tagged jet*, [CMS-PAS-SUS-13-008](#) (2013).
- [34] CMS collaboration, *Search for supersymmetry in pp collisions at  $\sqrt{s} = 8$  TeV in events with two opposite sign leptons, large number of jets, b-tagged jets, and large missing transverse energy*, [CMS-PAS-SUS-13-016](#) (2013).
- [35] ATLAS collaboration, *Search for direct production of the top squark in the all-hadronic ttbar + etmiss final state in 21 fb<sup>-1</sup> of p-p collisions at  $\sqrt{s}=8$  TeV with the ATLAS detector*, [ATLAS-CONF-2013-024](#) (2013).
- [36] ATLAS collaboration, *Search for direct top squark pair production in final states with one isolated lepton, jets and missing transverse momentum in  $\sqrt{s} = 8, \text{TeV}$  pp collisions using 21 fb<sup>-1</sup> of ATLAS data*, [ATLAS-CONF-2013-037](#) (2013).
- [37] ATLAS collaboration, *Searches for direct scalar top pair production in final states with two leptons using the transverse mass variable and a multivariate analysis technique in  $\sqrt{s} = 8$  TeV pp collisions using 20.3 fb<sup>-1</sup> of ATLAS data*, [ATLAS-CONF-2013-065](#) (2013).
- [38] ATLAS collaboration, *Search for direct top squark pair production in final states with two leptons in  $\sqrt{s} = 8$  TeV pp collisions using 20fb<sup>-1</sup> of ATLAS data*, [ATLAS-CONF-2013-048](#) (2013).
- [39] ATLAS collaboration, *Search for pair-produced top squarks decaying into a charm quark and the lightest neutralinos with 20.3 fb<sup>-1</sup> of pp collisions at  $\sqrt{s} = 8$  TeV with the ATLAS detector at the LHC*, [ATLAS-CONF-2013-068](#) (2013).
- [40] ATLAS collaboration, *Search for direct third-generation squark pair production in final states with missing transverse momentum and two b-jets in  $\sqrt{s} = 8$  TeV pp collisions with the ATLAS detector*, *JHEP* **10** (2013) 189 [[arXiv:1308.2631](#)] [[INSPIRE](#)].
- [41] CMS collaboration, *Search for top-squark pair production in the single-lepton final state in pp collisions at  $\sqrt{s} = 8$  TeV*, *Eur. Phys. J. C* **73** (2013) 2677 [[arXiv:1308.1586](#)] [[INSPIRE](#)].
- [42] CMS collaboration, *Search for supersymmetry in hadronic final states with missing transverse energy using the variables AlphaT and b-quark multiplicity in pp collisions at 8 TeV*, *Eur. Phys. J. C* **73** (2013) 2568 [[arXiv:1303.2985](#)] [[INSPIRE](#)].
- [43] ATLAS collaboration, *Search for direct production of charginos and neutralinos in events with three leptons and missing transverse momentum in 21 fb<sup>-1</sup> of pp collisions at  $\sqrt{s} = 8$  TeV with the ATLAS detector*, [ATLAS-CONF-2013-035](#) (2013).
- [44] ATLAS collaboration, *Search for direct-slepton and direct-chargino production in final states with two opposite-sign leptons, missing transverse momentum and no jets in 20/fb of pp collisions at  $\sqrt{s} = 8$  TeV with the ATLAS detector*, [ATLAS-CONF-2013-049](#) (2013).
- [45] ATLAS collaboration, *Search for electroweak production of supersymmetric particles in final states with at least two hadronically decaying taus and missing transverse momentum with the ATLAS detector in proton-proton collisions at  $\sqrt{s} = 8$  TeV*, [ATLAS-CONF-2013-028](#) (2013).

- [46] ATLAS collaboration, *Search for chargino and neutralino production in final states with one lepton, two b-jets consistent with a Higgs boson and missing transverse momentum with the ATLAS detector in 20.3 fb<sup>-1</sup> of  $\sqrt{s} = 8$  TeV pp collisions*, [ATLAS-CONF-2013-093](#) (2013).
- [47] CMS collaboration, *Search for electroweak production of charginos, neutralinos and sleptons using leptonic final states in pp collisions at 8 TeV*, [CMS-PAS-SUS-13-006](#) (2013).
- [48] CMS collaboration, *Search for new physics in events with same-sign dileptons and b jets in pp collisions at  $\sqrt{s} = 8$  TeV*, [JHEP 03 \(2013\) 037](#) [Erratum *ibid.* **1307** (2013) 041] [[arXiv:1212.6194](#)] [[INSPIRE](#)].
- [49] ATLAS collaboration, *Search for squarks and gluinos with the ATLAS detector in final states with jets and missing transverse momentum and 20.3 fb<sup>-1</sup> of  $\sqrt{s} = 8$  TeV proton-proton collision data*, [ATLAS-CONF-2013-047](#) (2013).
- [50] ALEPH, DELPHI, L3, OPAL, LEP WORKING GROUP FOR HIGGS BOSON SEARCHES collaboration, S. Schael et al., *Search for neutral MSSM Higgs bosons at LEP*, [Eur. Phys. J. C 47 \(2006\) 547](#) [[hep-ex/0602042](#)] [[INSPIRE](#)].
- [51] A. Djouadi and J. Quevillon, *The MSSM Higgs sector at a high  $M_{SUSY}$ : reopening the low  $\tan\beta$  regime and heavy Higgs searches*, [JHEP 10 \(2013\) 028](#) [[arXiv:1304.1787](#)] [[INSPIRE](#)].
- [52] A. Crivellin et al., *SUSY<sub>FLAVOR</sub> v2: A Computational tool for FCNC and CP-violating processes in the MSSM*, [Comput. Phys. Commun. 184 \(2013\) 1004](#) [[arXiv:1203.5023](#)] [[INSPIRE](#)].
- [53] A.J. Buras and J. Girrbach, *On the Correlations between Flavour Observables in Minimal  $U(2)^3$  Models*, [JHEP 01 \(2013\) 007](#) [[arXiv:1206.3878](#)] [[INSPIRE](#)].
- [54] C. Bobeth, G. Hiller and G. Piranishvili, *CP Asymmetries in  $\bar{B} \rightarrow \bar{K}^* (\rightarrow \bar{K} \pi) \bar{\ell} \ell$  and Untagged  $\bar{B}_s, B_s \rightarrow \phi (\rightarrow K^+ K^-) \bar{\ell} \ell$  Decays at NLO*, [JHEP 07 \(2008\) 106](#) [[arXiv:0805.2525](#)] [[INSPIRE](#)].
- [55] W. Altmannshofer et al., *Symmetries and Asymmetries of  $B \rightarrow K^* \mu^+ \mu^-$  Decays in the Standard Model and Beyond*, [JHEP 01 \(2009\) 019](#) [[arXiv:0811.1214](#)] [[INSPIRE](#)].
- [56] ACME collaboration, J. Baron et al., *Order of Magnitude Smaller Limit on the Electric Dipole Moment of the Electron*, [Science 343 \(2014\) 269](#) [[arXiv:1310.7534](#)] [[INSPIRE](#)].
- [57] J.J. Hudson et al., *Improved measurement of the shape of the electron*, [Nature 473 \(2011\) 493](#) [[INSPIRE](#)].
- [58] B.C. Regan, E.D. Commins, C.J. Schmidt and D. DeMille, *New limit on the electron electric dipole moment*, [Phys. Rev. Lett. 88 \(2002\) 071805](#) [[INSPIRE](#)].
- [59] R. Barbieri, P. Lodone and D.M. Straub, *CP Violation in Supersymmetry with Effective Minimal Flavour Violation*, [JHEP 05 \(2011\) 049](#) [[arXiv:1102.0726](#)] [[INSPIRE](#)].
- [60] D. Chang, W.-Y. Keung and A. Pilaftsis, *New two loop contribution to electric dipole moment in supersymmetric theories*, [Phys. Rev. Lett. 82 \(1999\) 900](#) [Erratum *ibid.* **83** (1999) 3972] [[hep-ph/9811202](#)] [[INSPIRE](#)].
- [61] G.F. Giudice and A. Romanino, *Electric dipole moments in split supersymmetry*, [Phys. Lett. B 634 \(2006\) 307](#) [[hep-ph/0510197](#)] [[INSPIRE](#)].
- [62] Y. Li, S. Profumo and M. Ramsey-Musolf, *Higgs-Higgsino-Gaugino Induced Two Loop Electric Dipole Moments*, [Phys. Rev. D 78 \(2008\) 075009](#) [[arXiv:0806.2693](#)] [[INSPIRE](#)].



- [63] J.R. Ellis, J.S. Lee and A. Pilaftsis, *Electric Dipole Moments in the MSSM Reloaded*, *JHEP* **10** (2008) 049 [[arXiv:0808.1819](#)] [[INSPIRE](#)].
- [64] S. Abel, S. Khalil and O. Lebedev, *EDM constraints in supersymmetric theories*, *Nucl. Phys. B* **606** (2001) 151 [[hep-ph/0103320](#)] [[INSPIRE](#)].
- [65] D. Becirevic et al.,  *$B_d - \bar{B}_d$  mixing and the  $B_d \rightarrow J/\psi K_s$  asymmetry in general SUSY models*, *Nucl. Phys. B* **634** (2002) 105 [[hep-ph/0112303](#)] [[INSPIRE](#)].
- [66] ETM collaboration, V. Bertone et al., *Kaon Mixing Beyond the SM from  $N_f=2$  tmQCD and model independent constraints from the UTA*, *JHEP* **03** (2013) 089 [Erratum *ibid.* **1307** (2013) 143] [[arXiv:1207.1287](#)] [[INSPIRE](#)].